

# TorchSpatial: A Location Encoding Framework and Benchmark for Spatial Representation Learning

NeurIPS 2024

*Nemin Wu\**, *Qian Cao\**, *Zhangyu Wang*, *Zeping Liu*, *Yanlin Qi*, *Jielu Zhang*, *Joshua Ni*, *X. Angela Yao*,  
*Hongxu Ma*, *Lan Mu*, *Stefano Ermon*, *Tanuja Ganu*, *Akshay Nambi*, *Ni Lao*, *Gengchen Mai*†

*\* Both authors contributed equally to this research*  
*† Corresponding author*



UNIVERSITY OF  
GEORGIA



SPATIALLY  
EXPLICIT AI



TEXAS

The University of Texas at Austin

# Motivation

Spatial representation learning (SRL) is a set of techniques learning neural spatial representations from spatial data in their native formats while avoiding manual feature engineering or data conversion.

- 1. Lack of a community-shared framework** for SRL model development
- 2. Lack of benchmarks** to systematically evaluate the location encoders' impact on model performance
- 3. Lack of evaluations on the geographic bias** of geo-aware AI approaches

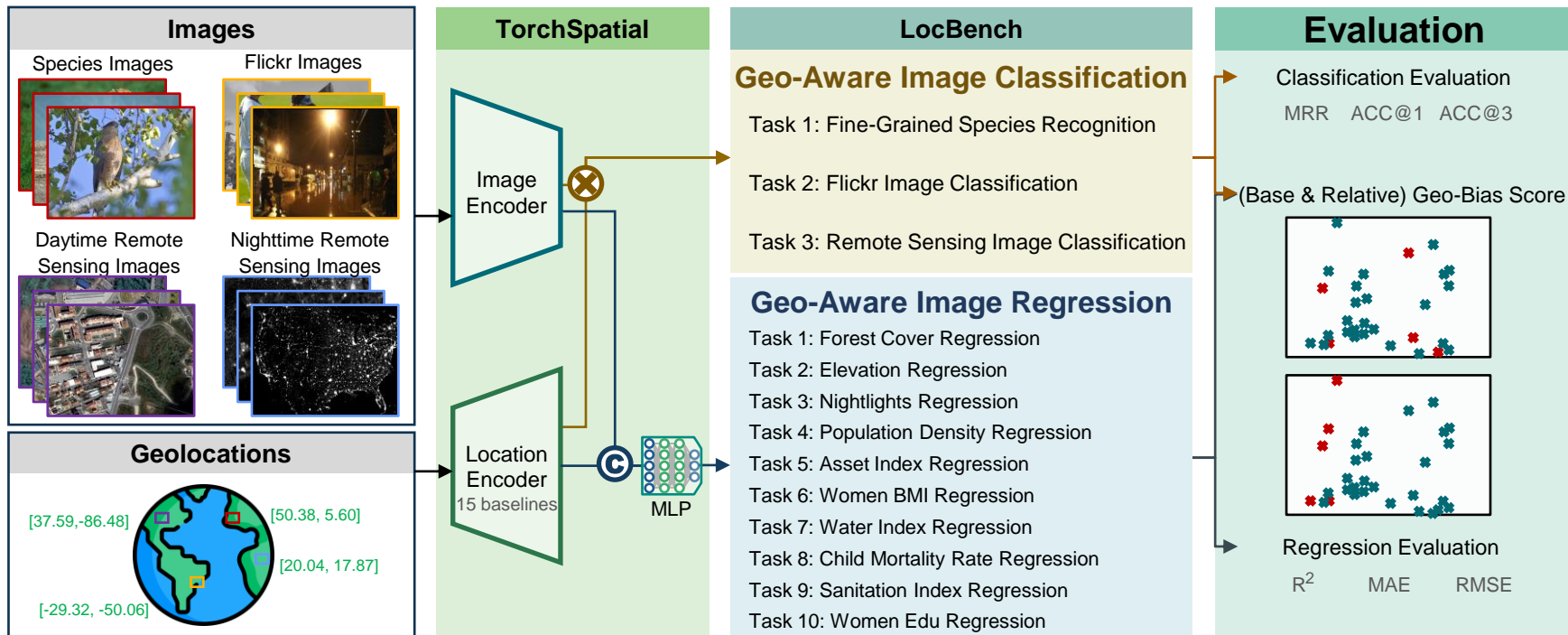


# TorchSpatial

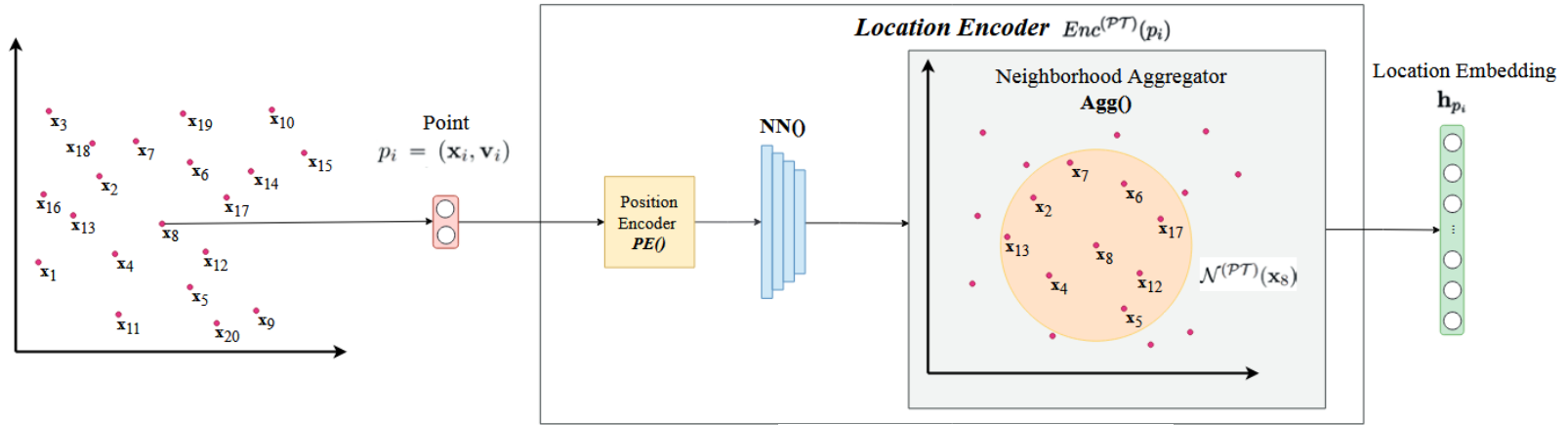
- **A model framework** that consolidates **15 location encoders** and necessary model building blocks for future location encoders.
- **A benchmark** which contains 7 geo-aware image classification and 10 image regression datasets.
- **A set of evaluation metrics** to quantify location encoders' overall model performance and their **geographic bias**.



# TorchSpatial Framework



# TorchSpatial Framework – Location Encoder



$$Enc(\mathbf{x}) = NN(PE(\mathbf{x}))$$

$\mathbf{x} \in \mathbb{R}^L$  ( $L = 2, 3$ ) : input location

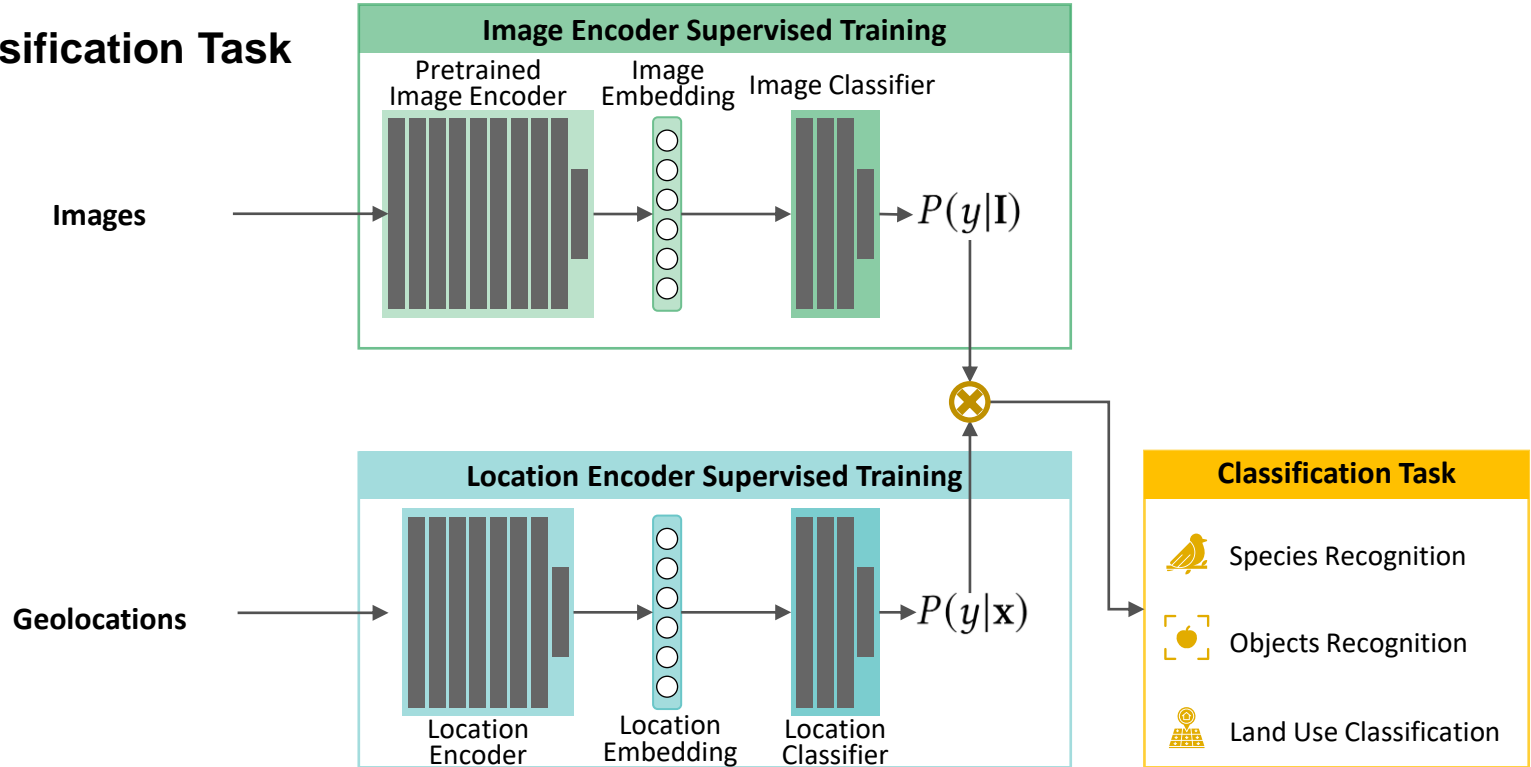
$PE(\mathbf{x}) \in \mathbb{R}^W$  : position encoder

$NN(\cdot) : \mathbb{R}^W \rightarrow \mathbb{R}^d$  : learnable neural nets

Mai, Gengchen, et al. "A review of location encoding for GeoAI: methods and applications." *International Journal of Geographical Information Science*

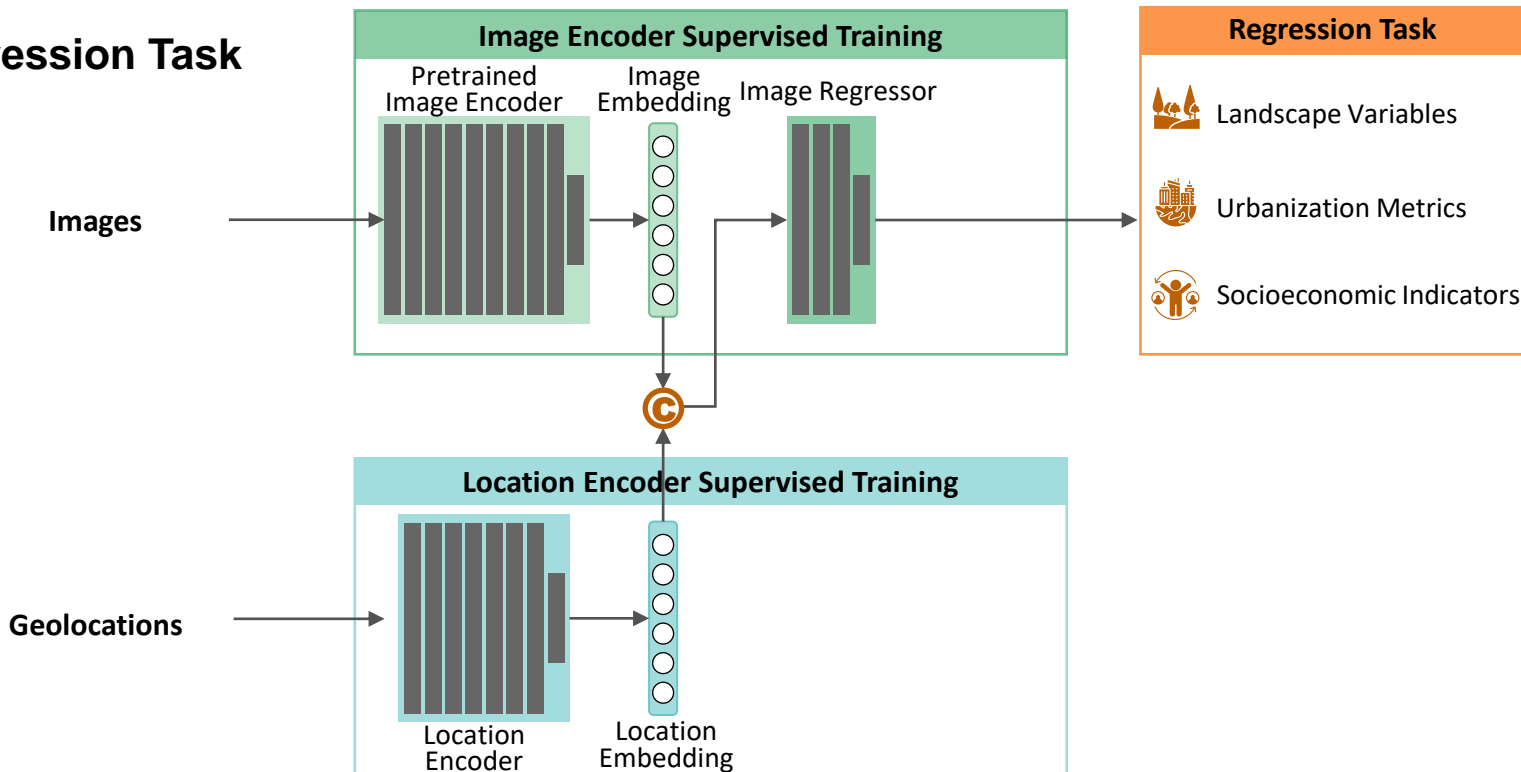
# TorchSpatial Framework – Inference Architecture

- **Classification Task**



# TorchSpatial Framework – Inference Architecture

- Regression Task



# LocBench

## Geo-Aware Image Classification

Classify a given image into its correct category based on the image itself and location metadata.

### Task 1: Fine-Grained Species Recognition

|           |                  |                  |
|-----------|------------------|------------------|
| BirdSnap  | 500 categories   | 19,576 examples  |
| BirdSnap† | 500 categories   | 43,470 examples  |
| NABirds†  | 555 categories   | 23,699 examples  |
| iNat2017  | 5,089 categories | 675,170 examples |
| iNat2018  | 8,142 categories | 461,939 examples |

### Task 2: Flickr Image Classification

|      |                |                 |
|------|----------------|-----------------|
| YFCC | 100 categories | 36,146 examples |
|------|----------------|-----------------|

### Task 3: Remote Sensing Image Classification

|      |               |                  |
|------|---------------|------------------|
| fMoW | 63 categories | 416,612 examples |
|------|---------------|------------------|

## Geo-Aware Image Regression

Given an image and its location information, predict the continuous target label for the image.

### Cat. 1: Landscape Variables Regression

|                      |         |                  |
|----------------------|---------|------------------|
| Task 1: Forest Cover | MOSAIKS | 498,106 examples |
| Task 2: Elevation    | MOSAIKS | 498,115 examples |

### Cat. 2: Urbanization Metrics Regression

|                            |         |                  |
|----------------------------|---------|------------------|
| Task 3: Nightlights        | MOSAIKS | 492,226 examples |
| Task 4: Population Density | MOSAIKS | 425,637 examples |

### Cat. 3: SDGs Indicators Regression

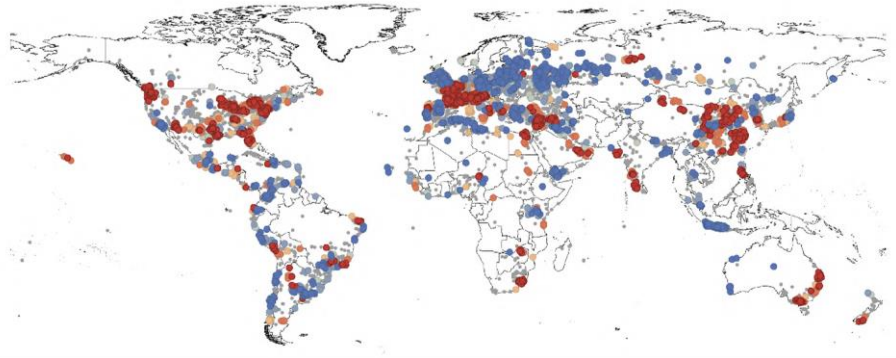
|                              |              |                  |
|------------------------------|--------------|------------------|
| Task 5: Asset Index          | SustainBench | 89,936 examples  |
| Task 6: Women BMI            | SustainBench | 94,866 examples  |
| Task 7: Water Index          | SustainBench | 86,938 examples  |
| Task 8: Child Mortality Rate | SustainBench | 105,582 examples |
| Task 9: Sanitation Index     | SustainBench | 89,271 examples  |
| Task 10: Women Edu           | SustainBench | 117,062 examples |





# Geo-Bias Score

**Geographic bias:** a phenomenon in which an AI model **performs differently across geographic regions** and its **predictions are biased** toward some predominated regions.

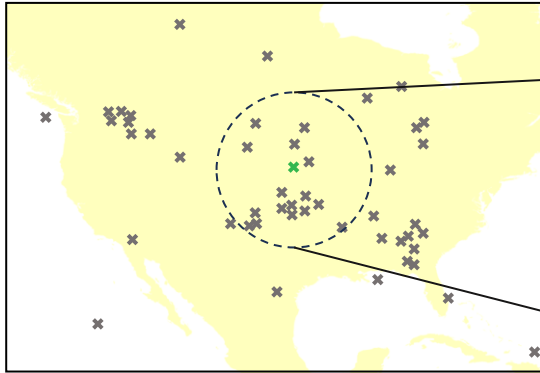


Hot spot analysis of HIT@1 of *space2vec-theory* on fMoW

- We employ the **spatial self-information (SSI)**, using a Gaussian distribution to approximate the probability of observing certain types of spatial patterns.

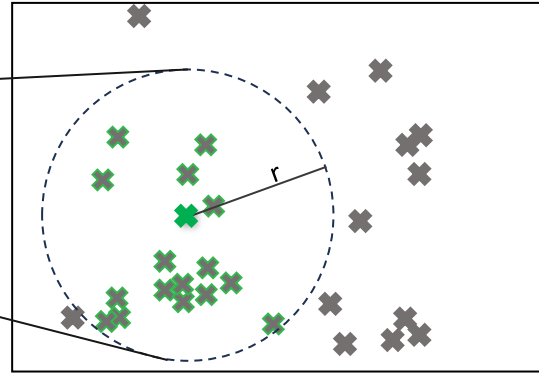
*The lower the SSI, the more likely the current spatial patterns arise randomly, namely less geo-biased.*

# Geo-Bias Score



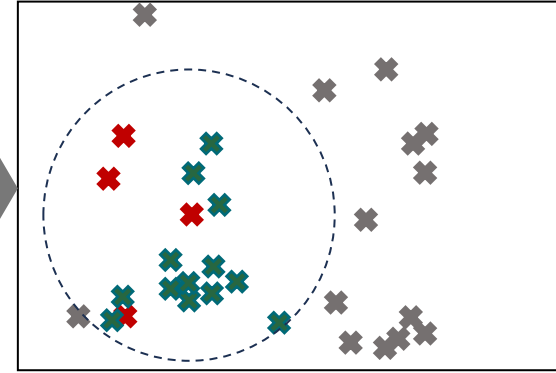
sample point

Extract a low-performance observation's neighborhood by radius  $r$ .



- **Base Geo-Bias Score**

The SSI of low-performance observations **if they are completely randomly distributed**



- **Relative Geo-Bias Score**

**Difference** between the SSI of the low-performance observations (**red** crosses) and the SSI of completely random low-performance observations (**cyan-blue** crosses).

Zhangyu Wang, Krzysztof Janowicz, **Gengchen Mai**, Ivan Majic. [Probing the Information Theoretical Roots of Spatial Dependence Measures](#), In: *Proceedings of the 16th Conference on Spatial Information Theory (COSIT 2024)*, Sep 17 - 20, Québec City, Canada. [[ArXiv](#)]

# Experiments - Image Classification - Top1Acc

|   | Task   | Species Recognition |              |              |              |              |              | Flickr       | RS           |
|---|--|---------------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
|   |  | BirdSnap            | BirdSnap†    | NABirds†     | iNat2017     | iNat2018     | avg          | YFCC         | fMOW         |
|   | Image Classification Dataset                   | Test                | Test         | Test         | Val          | Val          | -            | Test         | Val          |
|   | $P(y x)$ - Prior Type                          |                     |              |              |              |              |              |              |              |
| A | No Prior (i.e. image model)                    | 70.07               | 70.07        | 76.08        | 63.27        | 60.20        | 67.94        | 50.15        | 69.83        |
| B | <i>tile</i> (Tang et al., 2015)                | 70.20               | 70.56        | 75.78        | 62.54        | 56.30        | 67.08        | 50.01        | 69.86        |
|   | <i>wrap</i> (Mac Aodha et al., 2019)           | <b>72.06</b>        | 79.35        | <b>81.78</b> | 68.16        | 73.11        | 74.89        | 51.03        | 70.34        |
|   | <i>wrap + ffn</i> (Mai et al., 2020)           | 71.93               | 79.05        | 81.40        | <b>69.52</b> | 72.29        | 74.84        | 50.71        | 70.11        |
|   | <i>rbf</i> (Mai et al., 2020)                  | 71.79               | 79.58        | 81.74        | 68.24        | 70.03        | 74.28        | 51.22        | <b>70.68</b> |
|   | <i>rff</i> (Rahimi et al., 2007)               | 71.84               | 78.91        | 81.61        | 68.86        | 72.32        | 74.71        | 50.81        | 70.24        |
|   | Space2Vec- <i>grid</i> (Mai et al., 2020)      | 71.75               | <b>80.24</b> | 81.70        | 68.23        | 73.06        | 75.00        | <b>51.25</b> | 70.67        |
|   | Space2Vec- <i>theory</i> (Mai et al., 2020)    | 71.79               | 80.11        | 81.65        | 68.30        | <b>73.52</b> | <b>75.07</b> | 51.24        | 70.49        |
| C | <i>xyz</i> (Mai et al., 2023)                  | 71.88               | 78.96        | 81.15        | 68.65        | 71.44        | 74.42        | 50.87        | 70.16        |
|   | <i>NeRF</i> (Mildenhall et al., 2020)          | 72.10               | 79.93        | 81.62        | 68.74        | 72.91        | 75.06        | 51.27        | 70.60        |
|   | Sphere2Vec- <i>sphereC</i> (Mai et al., 2023)  | 72.10               | 79.97        | 81.91        | 69.34        | 72.93        | 75.25        | <b>51.35</b> | 70.85        |
|   | Sphere2Vec- <i>sphereC+</i> (Mai et al., 2023) | <b>72.15</b>        | <b>80.90</b> | <b>82.13</b> | 68.29        | <b>73.45</b> | <b>75.38</b> | 51.31        | <b>70.93</b> |
|   | Sphere2Vec- <i>sphereM</i> (Mai et al., 2023)  | 71.88               | 79.93        | 81.86        | 68.51        | 72.94        | 75.02        | 51.18        | <b>70.93</b> |
|   | Sphere2Vec- <i>sphereM+</i> (Mai et al., 2023) | 72.06               | 79.09        | 81.67        | 69.18        | 72.06        | 74.81        | 51.27        | 70.19        |
|   | Sphere2Vec- <i>dfs</i> (Mai et al., 2023)      | 71.79               | 78.69        | 81.44        | <b>69.42</b> | 72.16        | 74.70        | 50.65        | 70.27        |
|   | Siren(SH) (Russwurm et al., 2024)              | 71.88               | 78.82        | 81.72        | 67.68        | 71.33        | 74.29        | 50.57        | 70.20        |
| D | GPT-4V   | 55.02               | 48.89        | 73.00*       | 28.00*       | 18.00*       | 44.00*       | 34.00*       | 17.00*       |

# Experiments - Image Regression - R2

|   | Image Regression Dataset                      | Population Density | Forest Cover | Nightlight Luminosity | Elevation   |
|---|---|--------------------|--------------|-----------------------|-------------|
| A | No Prior (i.e. image model)                   | 0.38               | 0.52         | 0.33                  | 0.27        |
| B | <i>tile</i> (Tang et al., 2015)               | 0.04               | 0.46         | 0.18                  | 0.76        |
|   | <i>wrap</i> (Mac Aodha et al., 2019)          | 0.57               | 0.72         | 0.31                  | <b>0.79</b> |
|   | <i>wrap + ffn</i> (Mai et al., 2020)          | 0.47               | 0.67         | 0.28                  | 0.73        |
|   | <i>rbf</i> (Mai et al., 2020)                 | 0.25               | 0.54         | <b>0.32</b>           | 0.39        |
|   | <i>rff</i> (Rahimi et al., 2007)              | 0.57               | <b>0.73</b>  | 0.23                  | 0.77        |
|   | <i>Space2Vec-grid</i> (Mai et al., 2020)      | <b>0.65</b>        | 0.69         | 0.22                  | 0.76        |
|   | <i>Space2Vec-theory</i> (Mai et al., 2020)    | 0.57               | <b>0.73</b>  | 0.21                  | 0.78        |
| C | <i>xyz</i> (Mai et al., 2023)                 | 0.49               | 0.58         | 0.28                  | 0.72        |
|   | <i>NeRF</i> (Mildenhall et al., 2020)         | 0.60               | 0.68         | 0.23                  | 0.76        |
|   | <i>Sphere2Vec-sphereC</i> (Mai et al., 2023)  | 0.63               | 0.73         | 0.28                  | <b>0.82</b> |
|   | <i>Sphere2Vec-sphereC+</i> (Mai et al., 2023) | <b>0.64</b>        | <b>0.75</b>  | 0.27                  | <b>0.82</b> |
|   | <i>Sphere2Vec-sphereM</i> (Mai et al., 2023)  | 0.62               | 0.71         | 0.23                  | <b>0.82</b> |
|   | <i>Sphere2Vec-sphereM+</i> (Mai et al., 2023) | 0.53               | 0.67         | 0.32                  | 0.74        |
|   | <i>Sphere2Vec-dfs</i> (Mai et al., 2023)      | 0.52               | 0.62         | <b>0.35</b>           | 0.66        |
|   | <i>Siren(SH)</i> (Russwurm et al., 2024)      | 0.62               | 0.72         | 0.34                  | 0.80        |

\* (A) No Prior indicates image-only models; (B) geo-aware models with 2D location encoders; (C) geo-aware models with 3D location encoders.



# Experiments - Image Regression - R2

|   | Image Regression Dataset                      | Asset Index | Women BMI   | Water Index | Child Mortality Rate | Sanitation Index | Women Edu   |
|---|---|-------------|-------------|-------------|----------------------|------------------|-------------|
| A | No Prior (i.e. image model)                   | 0.40        | 0.27        | 0.26        | 0.02                 | 0.33             | 0.22        |
| B | <i>tile</i> (Tang et al., 2015)               | 0.00        | 0.00        | 0.00        | 0.00                 | 0.00             | 0.00        |
|   | <i>wrap</i> (Mac Aodha et al., 2019)          | 0.47        | 0.64        | 0.31        | 0.33                 | 0.42             | 0.50        |
|   | <i>wrap + ffn</i> (Mai et al., 2020)          | 0.45        | 0.63        | 0.29        | 0.32                 | 0.39             | 0.49        |
|   | <i>rbf</i> (Mai et al., 2020)                 | 0.56        | <b>0.66</b> | 0.40        | <b>0.36</b>          | 0.56             | 0.51        |
|   | <i>rff</i> (Rahimi et al., 2007)              | 0.50        | 0.64        | 0.33        | 0.34                 | 0.46             | 0.53        |
|   | <i>Space2Vec-grid</i> (Mai et al., 2020)      | 0.66        | <b>0.66</b> | 0.49        | 0.32                 | 0.59             | 0.64        |
|   | <i>Space2Vec-theory</i> (Mai et al., 2020)    | <b>0.70</b> | 0.65        | <b>0.52</b> | 0.33                 | <b>0.61</b>      | <b>0.66</b> |
| C | <i>xyz</i> (Mai et al., 2023)                 | 0.44        | 0.62        | 0.28        | 0.31                 | 0.38             | 0.48        |
|   | <i>NeRF</i> (Mildenhall et al., 2020)         | 0.65        | 0.68        | 0.50        | 0.34                 | 0.60             | 0.64        |
|   | <i>Sphere2Vec-sphereC</i> (Mai et al., 2023)  | <b>0.69</b> | <b>0.69</b> | 0.52        | <b>0.37</b>          | 0.62             | <b>0.66</b> |
|   | <i>Sphere2Vec-sphereC+</i> (Mai et al., 2023) | <b>0.69</b> | 0.68        | <b>0.53</b> | <b>0.37</b>          | <b>0.64</b>      | <b>0.66</b> |
|   | <i>Sphere2Vec-sphereM</i> (Mai et al., 2023)  | 0.67        | 0.68        | 0.52        | <b>0.37</b>          | 0.63             | <b>0.66</b> |
|   | <i>Sphere2Vec-sphereM+</i> (Mai et al., 2023) | 0.45        | 0.62        | 0.29        | 0.31                 | 0.39             | 0.48        |
|   | <i>Sphere2Vec-dfs</i> (Mai et al., 2023)      | 0.45        | 0.63        | 0.30        | 0.32                 | 0.40             | 0.49        |
|   | <i>Siren(SH)</i> (Russwurm et al., 2024)      | 0.52        | 0.65        | 0.35        | 0.35                 | 0.47             | 0.54        |

# Experiments - Image Classification - Geo-Bias

| Task                         |   | Species Recognition |               |               |               |                |               |               |               |               |               | Flickr |      | RS     |        |
|------------------------------|---|---------------------|---------------|---------------|---------------|----------------|---------------|---------------|---------------|---------------|---------------|--------|------|--------|--------|
| Image Classification Dataset |   | BirdSnap            |               | BirdSnap†     |               | NABirds†       |               | iNat2017      |               | iNat2018      |               | YFCC   |      | fMOW   |        |
| $P(y x)$ - Prior Type        |   | Test                |               | Test          |               | Test           |               | Val           |               | Val           |               | Test   |      | Val    |        |
| Geo-Bias Score               |   | base                | rel           | base          | rel           | base           | rel           | base          | rel           | base          | rel           | base   | rel  | base   | rel    |
| A                            | No Prior (i.e. image model)                   | 28.22               | 33.11         | 8.22          | 7.06          | 39.71          | 31.33         | 26.60         | 20.37         | 18.20         | 13.38         | 8.05   | 4.45 | 375.73 | 319.66 |
|                              | <i>tile</i> (Tang et al., 2015)               | 27.65               | 32.10         | 8.53          | 7.37          | 38.43          | 30.26         | 26.08         | 19.91         | 16.80         | 12.22         | 8.41   | 4.77 | 375.43 | 319.77 |
|                              | <i>wrap</i> (Mac Aodha et al., 2019)          | 27.76               | 32.98         | <b>17.17</b>  | <b>16.60</b>  | <b>57.37</b>   | <b>41.99</b>  | <b>34.83</b>  | <b>27.50</b>  | <b>30.78</b>  | <b>24.31</b>  | 7.99   | 4.41 | 380.20 | 323.67 |
|                              | <i>wrap + ffn</i> (Mai et al., 2020)          | 29.50               | 34.99         | 8.25          | 7.07          | <b>57.03</b>   | <b>42.43</b>  | <b>35.73</b>  | <b>28.20</b>  | <b>27.68</b>  | <b>21.57</b>  | 7.77   | 4.21 | 377.41 | 321.20 |
| B                            | <i>rbf</i> (Mai et al., 2020)                 | 17.24               | 19.75         | 9.37          | 8.52          | <b>58.05</b>   | <b>43.05</b>  | <b>34.05</b>  | <b>26.80</b>  | 20.48         | 15.28         | 7.37   | 3.86 | 380.64 | 324.46 |
|                              | <i>rff</i> (Rahimi et al., 2007)              | 28.03               | 33.61         | <b>13.70</b>  | <b>12.80</b>  | <b>57.71</b>   | <b>42.63</b>  | <b>34.45</b>  | <b>27.21</b>  | <b>28.63</b>  | <b>22.45</b>  | 7.87   | 4.29 | 377.94 | 317.65 |
|                              | <i>Space2Vec-grid</i> (Mai et al., 2020)      | 22.26               | 25.10         | <b>16.27</b>  | <b>15.42</b>  | <b>58.96</b>   | <b>43.38</b>  | <b>34.10</b>  | <b>26.87</b>  | <b>31.12</b>  | <b>24.71</b>  | 7.99   | 4.43 | 380.23 | 323.17 |
|                              | <i>Space2Vec-theory</i> (Mai et al., 2020)    | <b>36.78*</b>       | <b>42.98*</b> | <b>15.27</b>  | <b>14.36</b>  | <b>59.62</b>   | <b>44.38*</b> | <b>34.12</b>  | <b>26.87</b>  | <b>31.68*</b> | <b>24.92</b>  | 7.99   | 4.41 | 382.49 | 324.52 |
|                              | <i>xyz</i> (Mai et al., 2023)                 | 29.64               | 35.02         | <b>14.22</b>  | <b>13.38</b>  | <b>220.96*</b> | 34.09         | <b>34.89</b>  | <b>27.53</b>  | <b>26.33</b>  | <b>20.44</b>  | 7.79   | 4.24 | 379.84 | 323.12 |
|                              | <i>NeRF</i> (Mildenhall et al., 2020)         | 29.66               | 35.16         | <b>16.13</b>  | <b>15.53</b>  | <b>57.86</b>   | <b>42.61</b>  | <b>34.93</b>  | <b>27.62</b>  | <b>30.46</b>  | <b>23.90</b>  | 7.81   | 4.26 | 375.81 | 320.30 |
|                              | <i>Sphere2Vec-sphereC</i> (Mai et al., 2023)  | 28.84               | 34.02         | <b>14.78</b>  | <b>13.94</b>  | <b>59.26</b>   | <b>43.68</b>  | <b>35.77*</b> | <b>28.21*</b> | <b>31.61</b>  | <b>24.96*</b> | 7.67   | 4.16 | 377.07 | 320.78 |
| C                            | <i>Sphere2Vec-sphereC+</i> (Mai et al., 2023) | 30.43               | 36.48         | <b>19.99*</b> | <b>19.24*</b> | <b>59.13</b>   | <b>43.47</b>  | <b>33.14</b>  | <b>26.02</b>  | <b>31.55</b>  | <b>24.85</b>  | 8.22   | 4.66 | 379.92 | 323.04 |
|                              | <i>Sphere2Vec-sphereM</i> (Mai et al., 2023)  | 31.49               | 37.02         | <b>16.75</b>  | <b>16.70</b>  | <b>58.68</b>   | <b>43.10</b>  | <b>33.97</b>  | <b>26.75</b>  | <b>31.66</b>  | <b>24.95</b>  | 8.06   | 4.51 | 377.26 | 321.56 |
|                              | <i>Sphere2Vec-sphereM+</i> (Mai et al., 2023) | 27.55               | 33.04         | <b>14.35</b>  | <b>13.46</b>  | <b>53.71</b>   | <b>40.03</b>  | <b>35.44</b>  | <b>27.97</b>  | <b>26.88</b>  | <b>20.83</b>  | 8.13   | 4.56 | 376.64 | 321.21 |
|                              | <i>Sphere2Vec-dfs</i> (Mai et al., 2023)      | 26.39               | 30.93         | <b>13.57</b>  | <b>12.50</b>  | <b>55.43</b>   | <b>40.75</b>  | <b>35.52</b>  | <b>28.05</b>  | <b>26.00</b>  | <b>20.13</b>  | 7.87   | 4.30 | 380.82 | 323.78 |
|                              | <i>Siren(SH)</i> (Russwurm et al., 2024)      | 27.67               | 32.91         | <b>14.87</b>  | <b>14.50</b>  | <b>57.57</b>   | <b>42.60</b>  | <b>35.47</b>  | <b>28.07</b>  | <b>26.24</b>  | <b>20.26</b>  | 7.68   | 4.15 | 377.23 | 321.15 |
| D                            | GPT-4V  | 28.58               | 34.01         | 7.06          | 6.21          | -              | -             | -             | -             | -             | -             | -      | -    | -      | -      |



# Experiments - Image Regression - Geo-Bias

|   | Image Regression Dataset                      | Population Density |       | Forest Cover |       | Nightlight Luminosity |              | Elevation    |              |
|---|---|--------------------|-------|--------------|-------|-----------------------|--------------|--------------|--------------|
|   | Geo-Bias Score                                | base               | rel   | base         | rel   | base                  | rel          | base         | rel          |
| A | No Prior (i.e. image model)                   | 5.93*              | 2.53  | 6.71         | 2.73  | 7.47                  | 0.71         | 6.71         | 2.92         |
| B | <i>tile</i> (Tang et al., 2015)               | 5.40               | 2.34  | 5.73         | 2.38  | 7.60                  | 0.54         | 6.62         | 2.87         |
|   | <i>wrap</i> (Mac Aodha et al., 2019)          | 4.86               | 2.01  | 5.17         | 2.27  | 7.36                  | <b>1.08</b>  | 5.71         | 2.74         |
|   | <i>wrap + ffn</i> (Mai et al., 2020)          | 5.04               | 1.90  | 5.55         | 2.40  | 7.61                  | 0.27         | 6.12         | 2.90         |
|   | <i>rbf</i> (Mai et al., 2020)                 | 5.39               | 2.02  | 5.83         | 2.28  | 7.69                  | 0.42         | <b>7.28</b>  | <b>3.37</b>  |
|   | <i>rff</i> (Rahimi et al., 2007)              | 5.09               | 2.27  | 5.13         | 2.04  | 7.55                  | 0.50         | 5.51         | 2.61         |
|   | <i>Space2Vec-grid</i> (Mai et al., 2020)      | 5.48               | 2.42  | 5.25         | 2.11  | 7.64                  | 0.80         | 6.22         | 2.65         |
|   | <i>Space2Vec-theory</i> (Mai et al., 2020)    | 5.00               | 1.97  | 5.46         | 2.33  | 7.55                  | 0.75         | 5.07         | 2.24         |
| C | <i>xyz</i> (Mai et al., 2023)                 | 5.64               | 2.38  | 5.65         | 2.37  | 7.55                  | 0.54         | 5.96         | 2.97         |
|   | <i>NeRF</i> (Mildenhall et al., 2020)         | 5.90               | 2.80* | 5.64         | 2.60  | 7.70                  | 0.54         | 4.94         | 2.03         |
|   | <i>Sphere2Vec-sphereC</i> (Mai et al., 2023)  | 5.69               | 2.35  | 6.72*        | 2.24  | 7.73*                 | 0.36         | <b>8.83*</b> | <b>4.16*</b> |
|   | <i>Sphere2Vec-sphereC+</i> (Mai et al., 2023) | 5.34               | 2.37  | 5.08         | 2.18  | 7.50                  | 0.74         | 5.49         | 2.51         |
|   | <i>Sphere2Vec-sphereM</i> (Mai et al., 2023)  | 5.21               | 2.39  | 5.12         | 2.31  | 7.58                  | 0.78         | 5.01         | 2.21         |
|   | <i>Sphere2Vec-sphereM+</i> (Mai et al., 2023) | 5.20               | 2.51  | 5.45         | 2.31  | 7.54                  | 0.67         | 6.55         | 3.13         |
|   | <i>Sphere2Vec-dfs</i> (Mai et al., 2023)      | 5.45               | 2.59  | 6.08         | 2.94* | 7.53                  | <b>1.10</b>  | 6.03         | 2.58         |
|   | <i>Siren(SH)</i> (Russwurm et al., 2024)      | 5.10               | 2.29  | 5.82         | 2.46  | 7.48                  | <b>1.21*</b> | 5.39         | 2.35         |

**Bold** numbers indicate that the scores that are significantly larger (>30%) than the No Prior model; \* indicates the scores that are the largest among all models for this dataset.

# *Thank You*

*Contact:*

*Nemin Wu*

[Nemin.Wu@uga.edu](mailto:Nemin.Wu@uga.edu)

*Qian Cao*

[Qian.Cao1@uga.edu](mailto:Qian.Cao1@uga.edu)



UNIVERSITY OF  
GEORGIA



SPATIALLY  
EXPLICIT AI



TEXAS

The University of Texas at Austin