

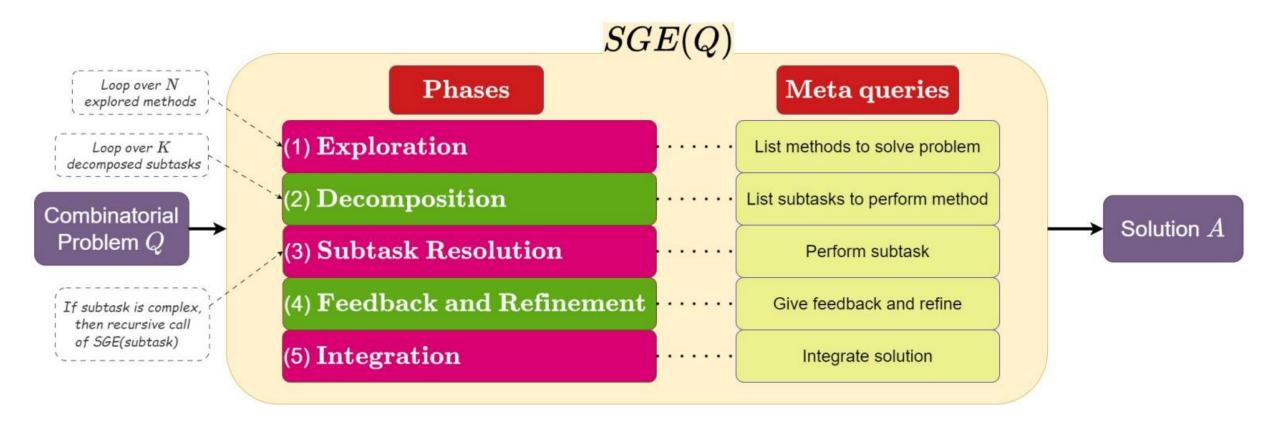




Self-Guiding Exploration for Combinatorial Problems (NeurIPS24)

Zangir Iklassov, Yali Du, Farkhad Akimov, and Martin Takac

SGE - Overview





SGE - Exploration

Example of VRP Exploration

- **Prompt**: [Task Description]. List heuristic methods to solve this problem. Return only method names separated by new lines.
- Exploration Output:
 - Nearest Neighbor Algorithm
 - Savings Algorithm
 - Sweep Algorithm
 - Clarke and Wright Algorithm
 - Genetic Algorithm
 - Simulated Annealing
 - Tabu Search
 - Ant Colony Optimization
 - Particle Swarm Optimization



Methods to Solve VRP. Let's consider first one (NN)

SGE – Decomposition

Example of VRP Decomposition

- **Prompt**: [Task Description]. Nearest Neighbor Algorithm. List the steps to use this heuristic method. Return only the steps, separated by new lines.
- Decomposition Output:
 - **Initialize at the Depot:** The starting point is the depot located at coordinates (50, 50).
 - **Find the Nearest Customer:** Calculate the Euclidean distance from the depot to each customer, and move to the closest one.
 - **Mark the Customer as Visited:** Once a customer is visited, they should not be revisited.
 - **Repeat Finding and Moving:** Continue finding the nearest unvisited customer from the current location until all customers have been visited.
 - **Return to the Depot:** After visiting the last customer, calculate the distance back to the depot to complete the route.
 - **Calculate the Total Length of the Route:** Sum up all the distances traveled from start to finish.



Steps of NN method

Example of Subtask Resolution, Step One

- Prompt: [Task Description]. [Apply the heuristic's step one].
- Subtask Resolution Output:

Initialize at the Depot

- Current location: Depot at (50, 50).





Example of Subtask Resolution, Step Two

- Prompt: [Task Description]. [Apply the heuristic's step two].
- Subtask Resolution Output:

Find the Nearest Customer

- Distance to Customer 1 at (87, 39): $\sqrt{(87-50)^2 + (39-50)^2}$
- Distance to Customer 2 at (1, 90): $\sqrt{(1-50)^2 + (90-50)^2}$
- Distance to Customer 3 at (28, 65): $\sqrt{(28-50)^2 + (65-50)^2}$
- Distance to Customer 4 at (85, 85): $\sqrt{(85-50)^2 + (85-50)^2}$

The initial distances from the depot to each customer are as follows:

- Customer 1: 38.60
- Customer 2: 63.25
- Customer 3: 26.63 (nearest)
- Customer 4: 49.50

NN step 2 output



Example of Subtask Resolution, Step Three

- **Prompt**: [Task Description]. [Apply the heuristic's step three].
- Subtask Resolution Output:

Mark the Customer as Visited. The nearest customer is Customer 3 at coordinates (28, 65). We will visit Customer 3 first.

> NN step 3 output. Steps 4 and 5 are similar just done in loop



Example of Subtask Resolution, Step Six

- Prompt: [Task Description]. [Apply the heuristic's step six].
- Subtask Resolution Output:

Calculate the Total Length of the Route.

The complete route, following the Nearest Neighbor Algorithm from the depot, visiting all customers, and returning to the depot, totals a distance of approximately 232.22 units.

Here's a summary of the route taken:

- Start at Depot (50, 50)
- Visit Customer 3 (28, 65)
- Visit Customer 2 (1, 90)
- Visit Customer 4 (85, 85)
- Visit Customer 1 (87, 39)
- Return to Depot (50, 50)

NN step 6 output Candidate solution



SGE – Feedback

Example of Feedback Prompting

- Prompt: [Task Description]. [Nearest Neighbor candidate solution]. Give feedback to the proposed solution.
- Feedback Output:

Implement route optimization post-processing, such as 2-opt or 3-opt techniques, which iteratively refine the route by removing crossings and reducing travel distance.

Feedback to the candidate solution



SGE – Refinement

Example of Refinement Prompting

- Prompt: [Task Description]. [Nearest Neighbor candidate solution]. [Feedback]. Improve the solution given feedback.
- Refinement Output:
 - we'll apply a 2-opt optimization to the route. This will involve swapping segments of the route to find a shorter path. Given the route '1 -> 2 -> 3 -> 4', we'll try different swaps and see if we can reduce the total distance further.
 - Let's simulate the 2-opt optimization on this route.
 - After applying the 2-opt optimization technique, the final optimized route has been adjusted to: Customer 1 -> Customer 3 -> Customer 2 -> Customer 4, then returning to the depot. This rearrangement was made to minimize the total distance traveled.



Candidate solution refined according to feedback

SGE – Integration

Example of Solution Integration

- **Prompt**: [Task Description]. [All candidate solutions]. Integrate all previous findings and provide the final answer. Return the answer only as a Python list of elements.
- Refinement Output: [1, 3, 2, 4]

Integration of all candidate solutions



Setup

Tasks

Assignment Problem

Knapsack Problem

Bin Packing Problem

Traveling Salesman Problem

Vehicle Routing Problem

Job Scheduling Problem

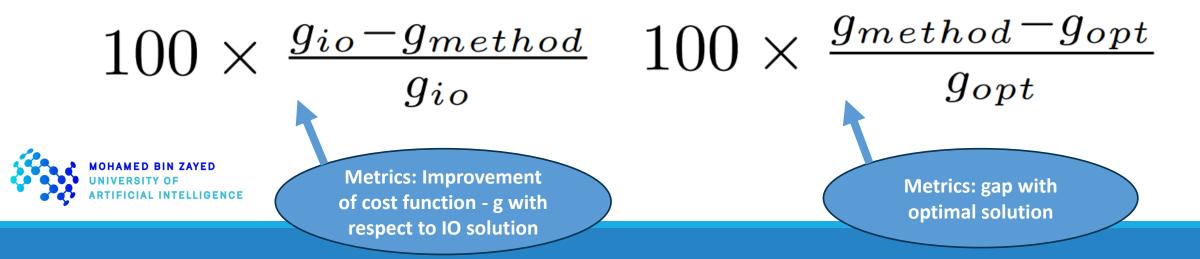
Baselines

Input-Output (IO) Direct Prompting

Chain-of-Thought Prompting

Self-Refine (Refine) Prompting

Decomposition Prompting



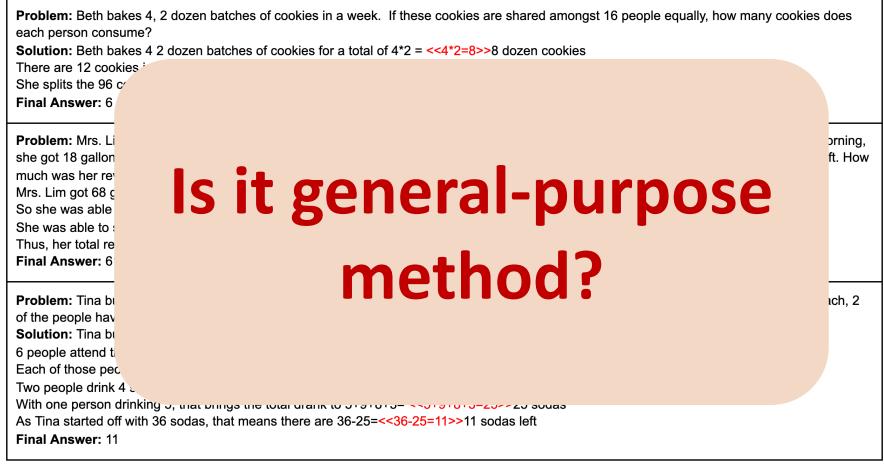
Results on CP

	GPT-4				Gemini-1.5								
Task	CoT	Refine	Decomp	Ours	CoT	Refin	e Deco	omp Ours	-				
Assignment	11.46	14.47	33.80	41.33	11.66	13.9	8 31	1.94 40.4	6				
Knapsack	15.37	17.16	51.95	70.39	13.85	16.8	5 48	8.62 65.8	7	On	timali	tv ga	n.
Bin Packing	14.06	17.12	39.57	74.72	11.89	15.4	3 35	5.74 67.6	3 (The low			
Travelling Salesman	13.64	15.75	38.49	72.10	14.34	15.9	0 36	5.36 68.0	9 🔪			, uie	Delle
Vehicle Routing	14.27	16.94	36.73	71.92	11.88	15.1	3 33	3.59 68.0	2				
Job Scheduling	13.84	16.37	38.20	75.33	13.41	15.7		5.36 67.8					
U									_				
	1												
						Size	MethodIO	Assignment 45.45	Knapsack 90.10	Bin Packing 108.2		VRP 102.0	JSP 105.3
						ES	CoT	39.33	90.10 66.88	78.24		78.17	
						NODES	Refine	36.42	61.98	77.40	71.62		
							Decomp	14.66	21 56	40.00	10 (0	10 65	44 15
Improvement of cost w.r.t IO.							Decomp	14.00	21.56	40.00	43.62	40.05	44.15
Inprovenie	nt of co	st w.r.t l	0.			S	Ours	2.500	8.050	9.060	8.27	11.92	9.300
							Ours IO	2.500 46.84	8.050 103.5	9.060 112.8	8.27 116.9	11.92 116.3	9.300 108.2
The higher							Ours IO CoT	2.500 46.84 39.70	8.050 103.5 73.84	9.060 112.8 85.08	8.27 116.9 89.01	11.92 116.3 89.48	9.300 108.2 85.21
							Ours IO CoT Refine	2.500 46.84 39.70 37.32	8.050 103.5 73.84 72.62	9.060 112.8 85.08 86.25	8.27 116.9 89.01 85.59	11.92 116.3 89.48 83.31	9.300 108.2 85.21 78.43
						8 NODES 2	Ours IO CoT Refine Decomp	2.500 46.84 39.70 37.32 18.49	8.050 103.5 73.84 72.62 26.43	9.060 112.8 85.08 86.25 52.73	8.27 116.9 89.01 85.59 53.48	11.92 116.3 89.48 83.31 54.43	9.300 108.2 85.21 78.43 49.81
						8 NODES	Ours IO CoT Refine Decomp Ours	2.500 46.84 39.70 37.32 18.49 8.290	8.050 103.5 73.84 72.62 26.43 14.88	9.060 112.8 85.08 86.25 52.73 20.95	8.27 116.9 89.01 85.59 53.48 15.19	11.92116.389.4883.3154.4319.65	9.300 108.2 85.21 78.43 49.81 21.26
						8 NODES	Ours IO CoT Refine Decomp Ours IO	2.500 46.84 39.70 37.32 18.49 8.290 49.11	8.050 103.5 73.84 72.62 26.43 14.88 101.5	9.060 112.8 85.08 86.25 52.73 20.95 120.7	8.27 116.9 89.01 85.59 53.48 15.19 121.6	11.92 116.389.4883.3154.43 19.65 118.5	9.300 108.2 85.21 78.43 49.81 21.26 117.6
						8 NODES	Ours IO CoT Refine Decomp Ours IO CoT	2.500 46.84 39.70 37.32 18.49 8.290 49.11 41.70	8.050 103.5 73.84 72.62 26.43 14.88 101.5 79.33	9.060 112.8 85.08 86.25 52.73 20.95 120.7 93.84	8.27 116.9 89.01 85.59 53.48 15.19 121.6 86.84	11.92 116.389.4883.3154.43 19.65 118.590.05	9.300 108.2 85.21 78.43 49.81 21.26 117.6 89.29
						NODES	Ours IO CoT Refine Decomp Ours IO	2.500 46.84 39.70 37.32 18.49 8.290 49.11 41.70 40.35	8.050 103.5 73.84 72.62 26.43 14.88 101.5	9.060 112.8 85.08 86.25 52.73 20.95 120.7	8.27 116.9 89.01 85.59 53.48 15.19 121.6	11.92 116.3 89.48 83.31 54.43 19.65 118.5 90.05 88.40	9.300 108.2 85.21 78.43 49.81 21.26 117.6 89.29 87.02



Results on Reasoning Tasks

Artimetic tasks - GSM8K dataset





Results on Reasoning Tasks

Artimetic tasks - GSM8K dataset

Problem: Beth bakes 4, 2 dozen batches of cookies in a week. If these cookies are shared amongst 16 people equally, how many cookies does each person consume?

Solution: Beth bakes 4 2 dozen batches of cookies for a total of 4*2 = <<4*2=8>>8 dozen cookies

There are 12 cookies in a dozen and she makes 8 dozen cookies for a total of 12*8 = <<12*8=96>>96 cookies

She splits the 96 cookies equally amongst 16 people so they each eat 96/16 = <<<u>96/16=6>>6</u> cookies

Final Answer: 6

Problem: Mrs. Lim milks her cows twice a day. Yesterday morning, she got 68 gallons of milk and in the evening, she got 82 gallons. This morning, she got 18 gallons fewer than she had yesterday morning. After selling some gallons of milk in the afternoon, Mrs. Lim has only 24 gallons left. How much was her revenue for the milk if each gallon costs \$3.50?

Mrs. Lim got 68 gallons - 18 gallons = <<68-18=50>>50 gallons this morning.

So she was able to get a total of 68 gallons + 82 gallons + 50 gallons = <<68+82+50=200>>200 gallons.

She was able to sell 200 gallons - 24 gallons = <<200-24=176>>176 gallons.

Thus, her total revenue for the milk is 3.50/gallon x 176 gallons = <<3.50*176=616>>616.

Final Answer: 616

Problem: Tina buys 3 12-packs of soda for a party. Including Tina, 6 people are at the party. Half of the people at the party have 3 sodas each, 2 of the people have 4, and 1 person has 5. How many sodas are left over when the party is over?

Solution: Tina buys 3 12-packs of soda, for 3*12= <<3*12=36>>36 sodas

6 people attend the party, so half of them is 6/2= <<6/2=3>>3 people

Each of those people drinks 3 sodas, so they drink 3*3=<<3*3=9>>9 sodas

Two people drink 4 sodas, which means they drink 2*4=<<4*2=8>>8 sodas

With one person drinking 5, that brings the total drank to 5+9+8+3= <<5+9+8+3=25>>25 sodas

As Tina started off with 36 sodas, that means there are 36-25=<<36-25=11>>11 sodas left

Final Answer: 11



Results on Reasoning Tasks



Method		Arith	metic		Comm	nonsens	Symbolic	Avg.		
	AQUA	GSM8K	SVAMP	ASDiv	StrategyQA	CSQA	ARC	LastLetter	0	
IO Prompting	67.30	87.04	88.34	90.10	78.40	81.14	87.52	81.98	82.73	
CoT Prompting Refine Prompting Decomp Prompting	69.57 69.68 69.99	89.76 89.80 91.85	91.58 91.00 92.16	93.32 93.10 94.08	81.16 81.26 82.08	83.50	90.80 91.09 91.76	84.82	85.69 85.53 86.43	
Ours	74.63	97.35	98.16	97.24	83.49	85.68	93.28	86.96	89.60	
				1						

MOHAMED BIN ZAYED UNIVERSITY OF ARTIFICIAL INTELLIGENCE Accuracy on test data. The higher it is , the better

Thank you!

