

# Cross-Scale Self-Supervised Blind Image Deblurring via Implicit Neural Representation

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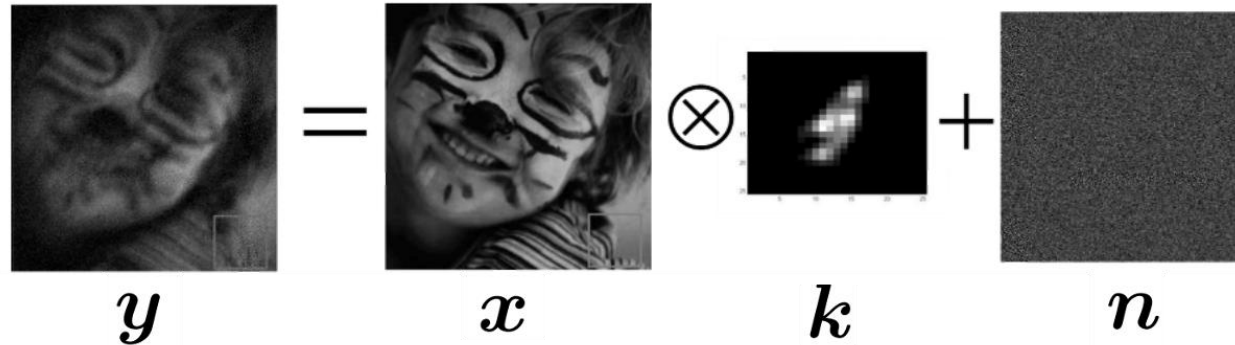
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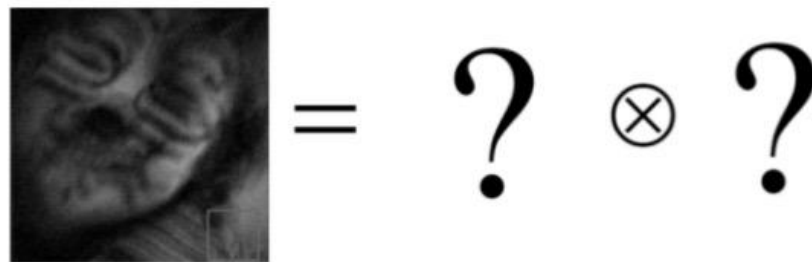
# Background

- Uniform blurring, usually can be described as the convolution:

$$y = k \otimes x + n$$



- Blind image deblurring (BID):  $y \longrightarrow (k, x)$



- Challenge:** solution ambiguity:  $y = k \otimes x = \delta \otimes y$

- DNN-based re-parametrization of latent  $\mathbf{x}/\mathbf{k}$  :

$$\mathbf{x} := \mathcal{G}_{\mathbf{x}}(\cdot; \Theta_{\mathbf{x}}) \quad \mathbf{k} := \mathcal{G}_{\mathbf{k}}(\cdot; \Theta_{\mathbf{k}})$$

- Standard self-supervised reconstruction loss:

$$\mathcal{L}_{sr}(\Theta_{\mathbf{k}}, \Theta_{\mathbf{x}}) := \|\mathcal{G}_{\mathbf{k}}(\cdot; \Theta_{\mathbf{k}}) \otimes \mathcal{G}_{\mathbf{x}}(\cdot; \Theta_{\mathbf{x}}) - \mathbf{y}\|_2^2$$

- **Challenge:** Overfitting due to the lack of ground truth (GT) data.

$$\mathcal{G}_{\mathbf{x}}(\cdot; \hat{\Theta}_{\mathbf{x}}) \rightarrow \mathbf{y} \quad \mathcal{G}_{\mathbf{k}}(\cdot; \hat{\Theta}_{\mathbf{k}}) \rightarrow \delta$$

# Main Idea and Contributions

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Two key questions for self-supervised BID:

**Q1:** How to formulate a better self-supervised loss?

**A1: A cross-scale loss function:**

Leveraging the resolution-independent properties of Implicit Neural Representation (INR) for latent images/kernels.

**Q2:** How can we efficiently train the two NN generators to ensure accurate convergence to the latent images and kernels?

**A2: A progressive coarse-to-fine scheme:**

Enhancing training efficiency and ensuring the convergence to GT image/kernel.

# Self-supervised cross-scale loss for BID

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- Without GT images, the only readily available loss function to train the generators is the fitting loss:

$$L_{\text{fit}}(\Theta_{\mathbf{k}}, \Theta_{\mathbf{x}}) = \mathcal{M}_f(\mathbf{y} - \mathbf{k} \otimes \mathbf{x}) = \mathcal{M}_{\text{fit}}\left(\Phi_{\mathbf{k}}(\mathbb{I}_{\mathbf{k}}; \Theta_{\mathbf{k}}) \otimes \Phi_{\mathbf{x}}(\mathbb{I}_{\mathbf{x}}; \Theta_{\mathbf{x}}), \mathbf{y}\right)$$

where  $\mathcal{M}_f(\cdot)$  is some distance metric.

- **Such fitting loss clearly is not sufficient to resolve solution ambiguity!**

# Self-supervised cross-scale loss for BID

- To alleviate over-fitting, the down-sampled version of  $\mathbf{y}$ , denoted as  $\mathbf{y}_{\downarrow_s}$  for scale  $s$ , has often been used to initiate the blur kernel estimate.
- However,  $(\mathbf{x} \otimes \mathbf{k})_{\downarrow_2} \neq \mathbf{x}_{\downarrow_2} \otimes \mathbf{k}_{\downarrow_2}$
- We present a cross-scale constraint that accurately characterizes the connection between  $(\mathbf{y}, \mathbf{x}, \mathbf{k})$  at different scales:

**Proposition 1.** *For a kernel (filter)  $\mathbf{k}$ , let  $\mathbf{g}_1, \mathbf{g}_2, \mathbf{g}_3$  denote its associated QMF filters defined by*

$$\mathbf{g}_1[m, n] = (-1)^m \mathbf{k}[m, n], \mathbf{g}_2[m, n] = (-1)^n \mathbf{k}[m, n], \mathbf{g}_3[m, n] = (-1)^{m+n} \mathbf{k}[m, n],$$

*for any  $[m, n] \in \mathbb{I}_{\mathbf{k}}$ . Then, we have the following relation between consecutive two dyadic scales:*

$$(\mathbf{x}_{\downarrow_2}) \otimes (\mathbf{k}_{\downarrow_2}) = \frac{1}{4} \left( (\mathbf{x} \otimes \mathbf{k})_{\downarrow_2} + \sum_{d=1}^3 (\mathbf{x} \otimes \mathbf{g}_d)_{\downarrow_2} \right).$$

# Self-supervised cross-scale loss for BID

- We introduce a scale consistency loss across two consecutive scales:  
 For each scale  $s$  :

$$\begin{aligned}
 L_{\text{cross}}^{(s)}(\Theta_{\mathbf{k}}, \Theta_{\mathbf{x}}) &= \mathcal{M}_c \left( 4(\mathbf{x}^{(s)} \downarrow_2) \otimes (\mathbf{k}^{(s)} \downarrow_2), (\mathbf{x}^{(s)} \otimes \mathbf{k}^{(s)}) \downarrow_2 + \sum_{1 \leq d \leq 3} (\mathbf{x}^{(s)} \otimes \mathbf{g}_d^{(s)}) \downarrow_2 \right) \\
 &= \mathcal{M}_c \left( 4(\mathbf{x}^{(s+1)}) \otimes (\mathbf{k}^{(s+1)}), (\mathbf{x}^{(s)} \otimes \mathbf{k}^{(s)}) \downarrow_2 + \sum_{1 \leq d \leq 3} (\mathbf{x}^{(s)} \otimes \mathbf{g}_d^{(s)}) \downarrow_2 \right)
 \end{aligned}$$

- Ablation study on the  $\mathcal{L}_{\text{cross}}$  in terms of PSNR/SSIM.

Category	Manmade	Natural	People	Saturated	Text	Average
w/o $\mathcal{L}_{\text{cross}}$	21.19/0.778	25.84/0.887	30.74/0.918	17.69/0.682	26.75/0.917	24.44/0.836
Ours	<b>23.24/0.893</b>	<b>26.27/0.933</b>	<b>31.53/0.944</b>	<b>17.76/0.683</b>	<b>27.01/0.930</b>	<b>25.16/0.879</b>

The scale-consistency loss providing additional regularization for training two INR-based generators.

- The blur kernel and the latent image are re-parameterized by two INR models:

$$\begin{cases} \mathbf{k}[\mathbb{I}_{\mathbf{k}}] = \Phi_{\mathbf{k}}(\mathbb{I}_{\mathbf{k}}; \Theta_{\mathbf{k}}) & : \quad \mathbf{k}[i, j] = \Phi_{\mathbf{k}}([i, j]), [i, j] \in \mathbb{I}_{\mathbf{k}}; \\ \mathbf{x}[\mathbb{I}_{\mathbf{x}}] = \Phi_{\mathbf{x}}(\mathbb{I}_{\mathbf{x}}; \Theta_{\mathbf{x}}) & : \quad \mathbf{x}[i, j] = \Phi_{\mathbf{x}}([i, j]), [i, j] \in \mathbb{I}_{\mathbf{x}}, \end{cases}$$

- Let  $\mathbf{k}^{(0)} = \mathbf{k}$ ,  $\mathbf{x}^{(0)} = \mathbf{x}$  denotes the original scale, we can form both the kernel and the image in a dyadic pyramid:

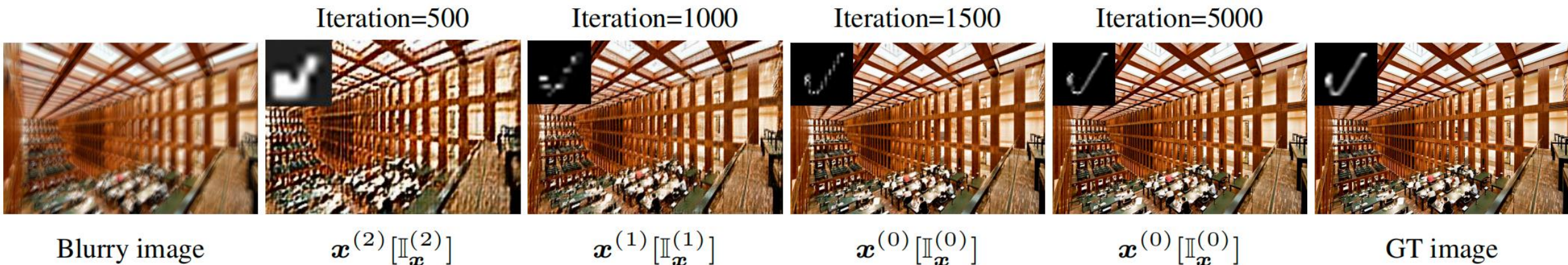
$$\mathbf{k}^{(s)} = (\mathbf{k}^{(s-1)}) \downarrow_2 \quad \text{and} \quad \mathbf{x}^{(s)} = (\mathbf{x}^{(s-1)}) \downarrow_2, \quad \text{for } 1 \leq s \leq S_0.$$

- INR enables the model to generate the prediction with higher/lower resolutions from the same learned model, facilitating multi-scale processing and cross-scale interaction.



# Progressively coarse-to-fine training

- **First stage** (Initialization): at the scale  $S_0$   
Training the NNs with only the fitting loss  $\mathcal{L}_{\text{fit}}^{(S_0)}$ .
- **Second stage:** progressive refines the training from the scale  $S_0$  to 0  
Training the NNs at the scale  $s$  with the loss  $\mathcal{L}_{\text{fit}}^{(s)} + \lambda \mathcal{L}_{\text{cross}}^{(s)}$ .
- **Final stage:** tuning at the scale 0  
Training the NNs at scale 0 with only the fitting loss  $\mathcal{L}_{\text{fit}}^{(0)}$ .



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 Training the NNs at scale 0 with only the fitting loss  $\mathcal{L}_{\text{fit}}^{(0)}$ .
- Ablation study on the cross scale and progressive training in terms of PSNR/SSIM.

Category	Manmade	Natural	People	Saturated	Text	Average
Single-scale	22.04/0.803	25.93/0.890	30.33/0.933	17.68/0.688	24.76/0.886	24.14/0.840
w/o Progressive	20.36/0.742	23.91/0.829	26.35/0.821	17.22/0.675	22.88/0.857	22.14/0.790
<b>Ours</b>	<b>23.24/0.893</b>	<b>26.27/0.933</b>	<b>31.53/0.944</b>	<b>17.76/0.683</b>	<b>27.01/0.930</b>	<b>25.16/0.879</b>

# PSNR results on blind uniform deblurring

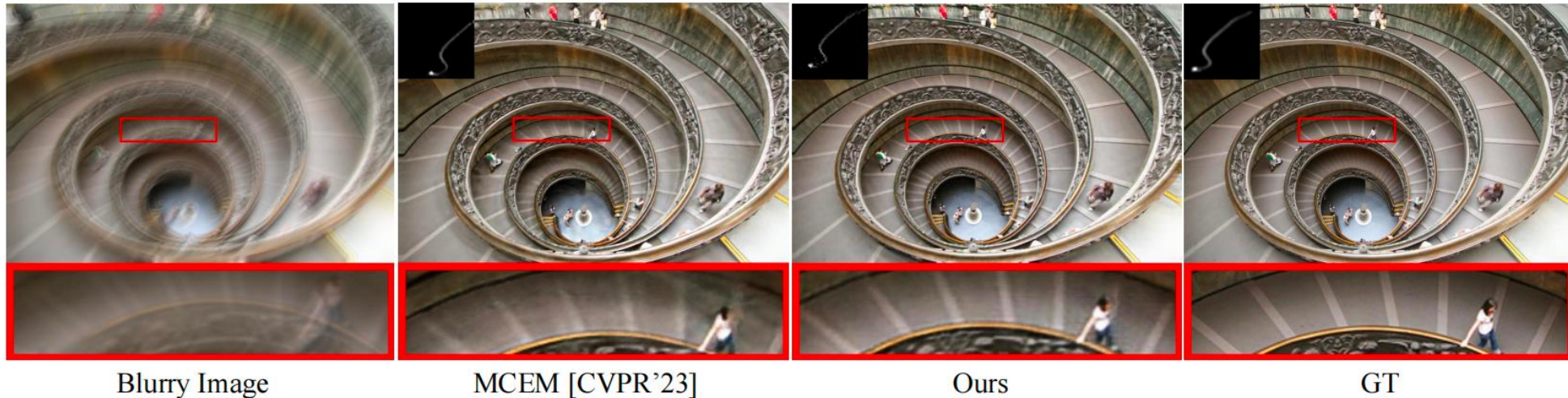
- [Lai et al.'s Dataset]: 100 images categorized into five groups, and covers 4 different kernels whose size ranges from  $31 \times 31$  to  $75 \times 75$ .

Methods	Non-learning		Supervised		Self-Supervised Method			
	Yan et al. [CVPR'17]	Yang & Ji [CVPR'19]	MPRNet [CVPR'21]	Restormer [CVPR'22]	SelfDeblur [CVPR'20]	DEBID [TCSVT'23]	MCEM [CVPR'23]	Ours
Manmade	19.32	19.99	17.39	17.87	20.35	22.14	23.06	<b>23.24</b>
Natural	23.69	24.33	20.53	21.07	22.05	26.18	26.00	<b>26.27</b>
People	27.01	27.22	22.85	23.15	25.94	31.25	31.02	<b>31.53</b>
Saturated	16.46	17.04	15.35	15.58	16.35	<b>18.43</b>	17.21	17.76
Text	17.42	20.35	16.01	16.67	20.16	23.00	25.46	<b>27.01</b>
Average	19.89	21.79	18.42	18.89	20.97	24.29	24.55	<b>25.16</b>



# Visual Results

- Visual results on blind uniform deblurring [Lai Dataset].



- Visual results on real blurry image.



# Limitations and Future work

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**Limitation1:** Computational cost for processing a large number of images as the method requires training the model for each individual sample.

**Potential solution:** **Meta-learning or Testing-time adaptation.**

**Limitation2:** Only applicable to handle uniform blurring, as it relies on the convolution model.

**Future work:** **Extending this approach to handle non-uniform blur.**

**Thank you for your attention!**