



# FM-Delta: Lossless Compression for Storing Massive Fine-tuned Foundation Models

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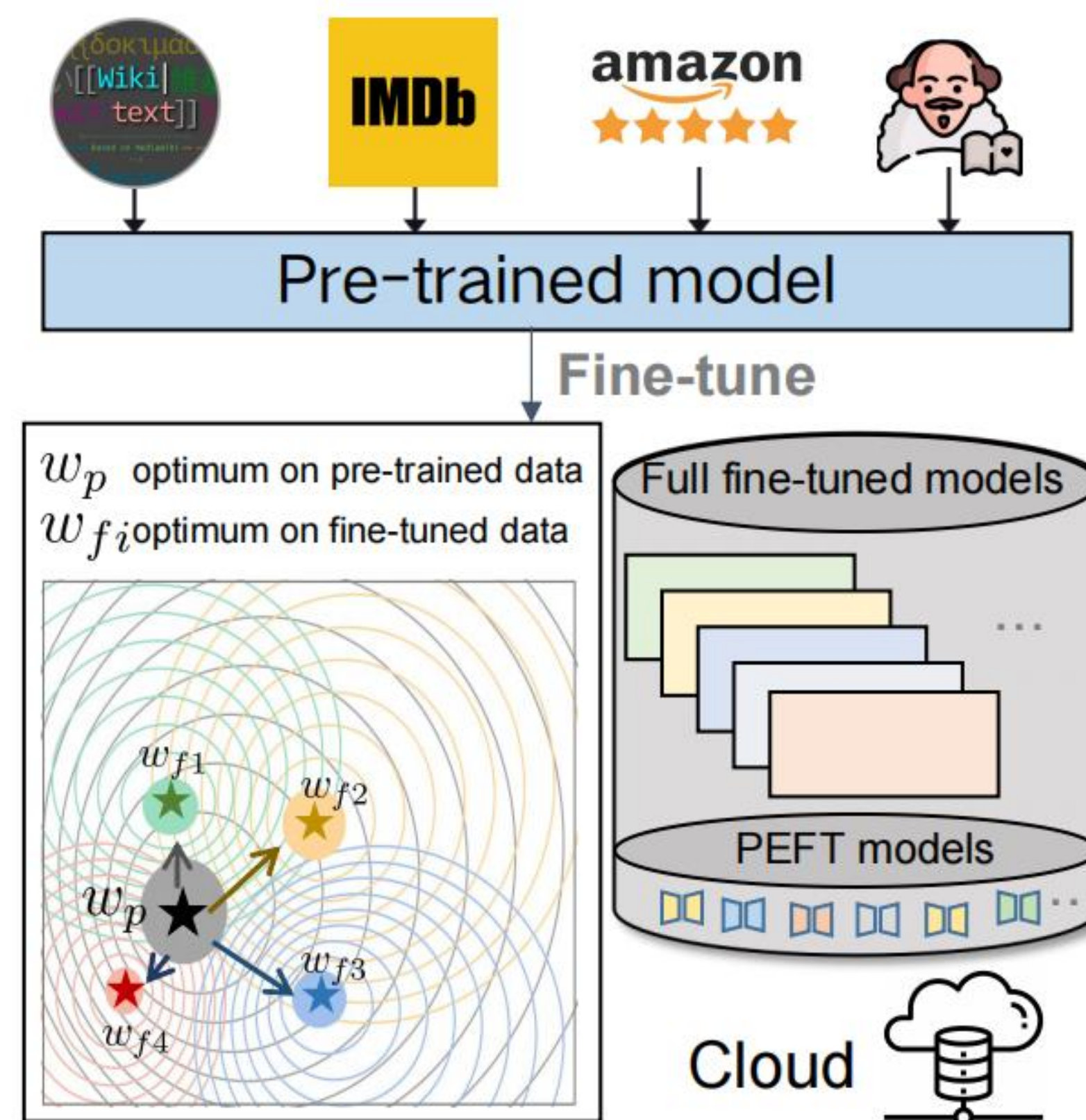
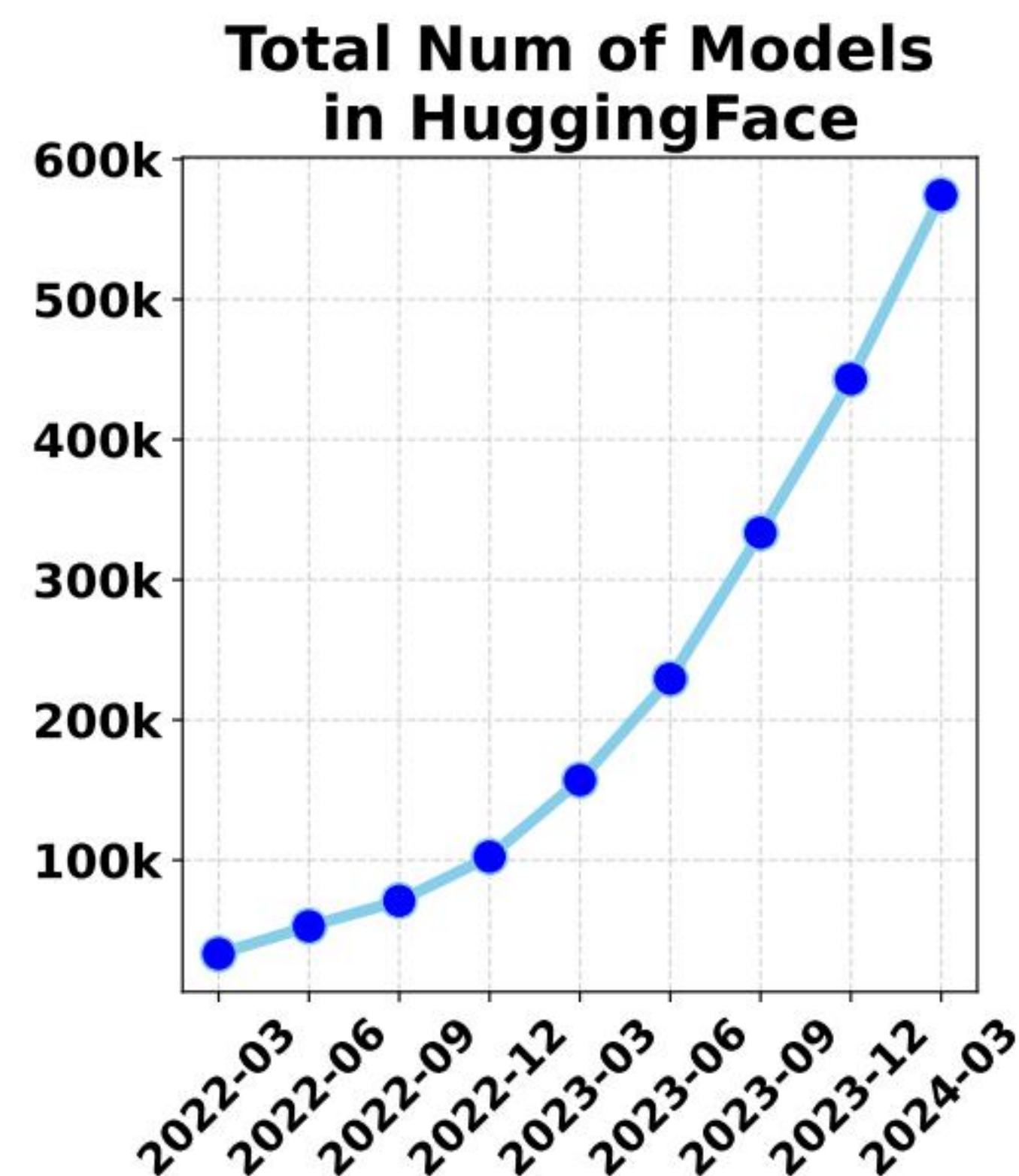
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# Motivation: Storage Overhead in Cloud



Model	Model size	Full num.	PEFT num.	Inact.
Falcon-40B	40B	79	48	82%
GPT-NeoX	20B	51	22	84%
GPT-J	6B	284	75	88%
LLaMA-7B	7B	5112	1170	91%
Bert-large	336M	260	159	88%
Stable Diff.	860M	1606	65	64%
Approx. disk storage		159TB	4TB	89%

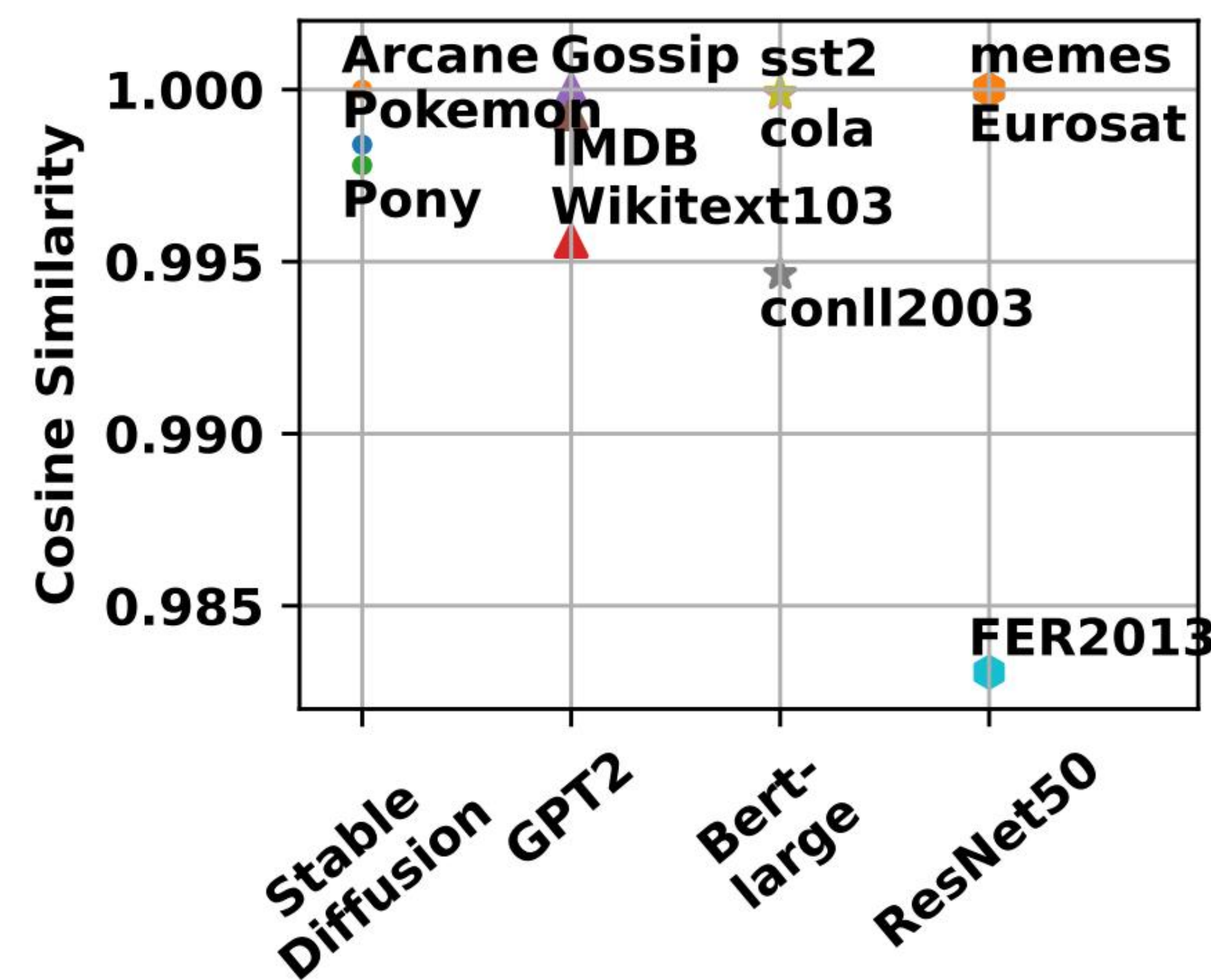
**\$9,540**

- **heavy storage overhead** for cloud providers such as HuggingFace.
- key pain point --- **full fine-tuned models**.
- premise --- protect users' intellectual property of users (i.e., **no changes to models**)

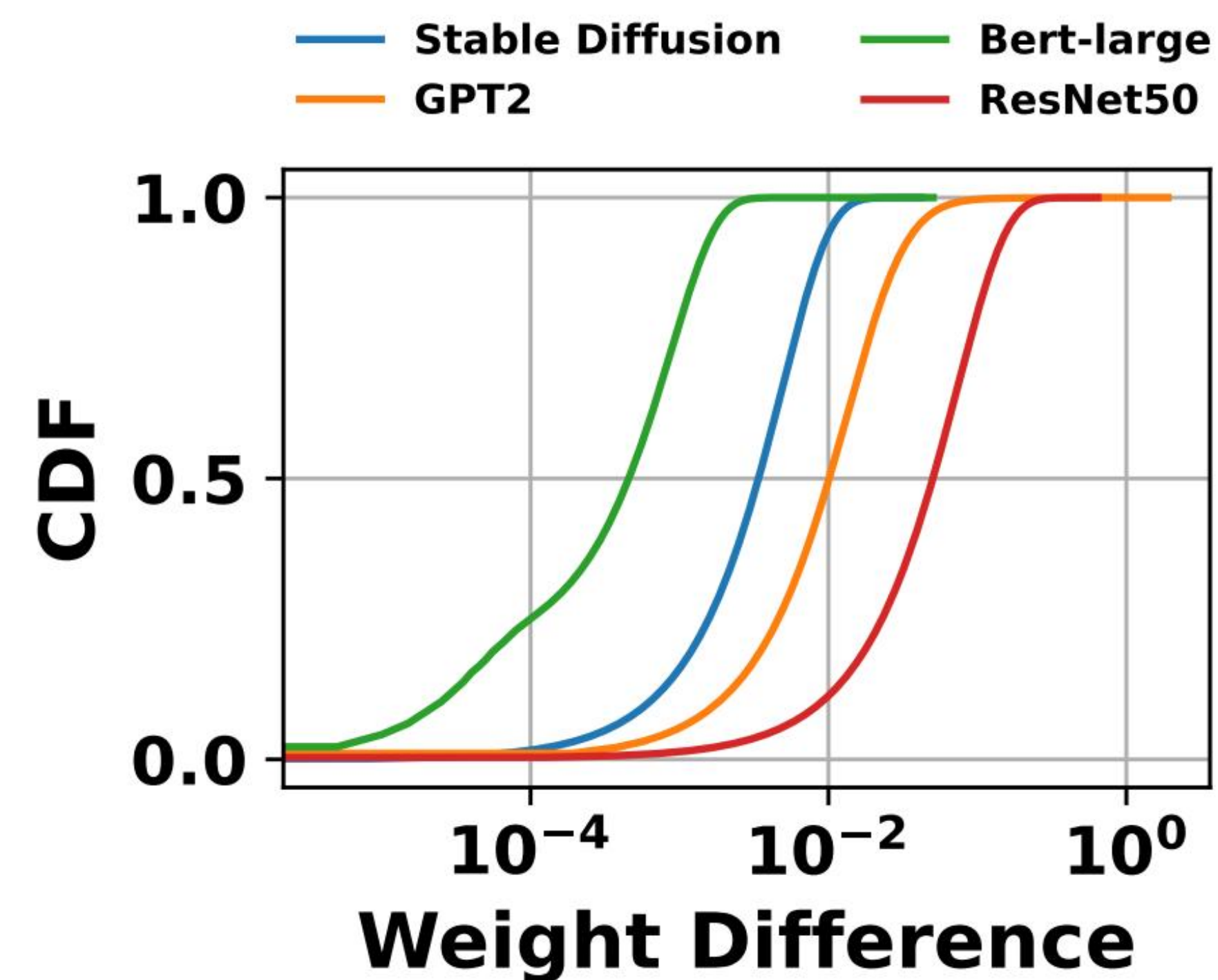


# Finding: Small Delta

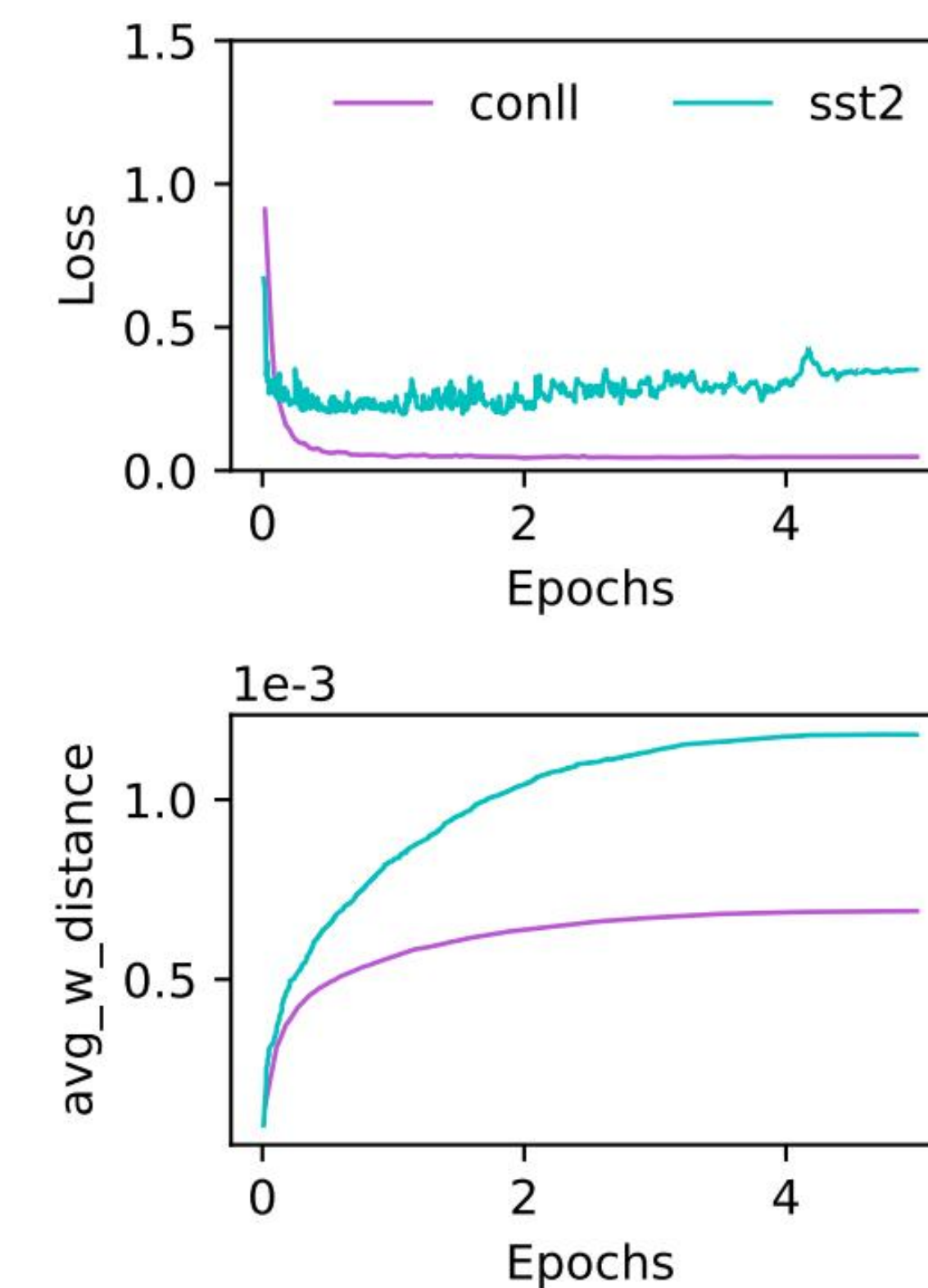
- Empirical analysis: a small difference (**delta**) *between most* fine-tuned and pre-trained models stored in cloud.



- High model cosine similarity



- Small element difference  $10^{-4}$ - $10^0$



(b) Bert-large-uncased

- Average difference grows slow over fine-tuning.



# Finding: Small Delta

➤ Theoretical analysis: delta grows slowly as the number of fine-tuning steps  $T$  increases.

*Assumption 1.* For the loss function  $f$ , there exists  $\mathbf{w}^* \in \mathbb{R}^d$  such that  $f(\mathbf{w}) \geq f(\mathbf{w}^*)$ , for all  $\mathbf{w}$ .

*Assumption 2.*  $f$  satisfies that for all  $\mathbf{w}, \mathbf{v} \in \mathbb{R}^d$ ,  $f(\mathbf{w}) - f(\mathbf{v}) \leq (\mathbf{w} - \mathbf{v})^T \nabla f(\mathbf{v}) + \frac{\beta}{2} \|\mathbf{w} - \mathbf{v}\|^2$ .

*Assumption 3.* Given a data distribution  $\mathcal{D}$ , the variance of stochastic gradient is bounded:  
 $\mathbb{E}_{\xi \sim \mathcal{D}} \|G(\mathbf{w}; \xi) - \nabla f(\mathbf{w})\|^2 \leq \sigma^2$ .

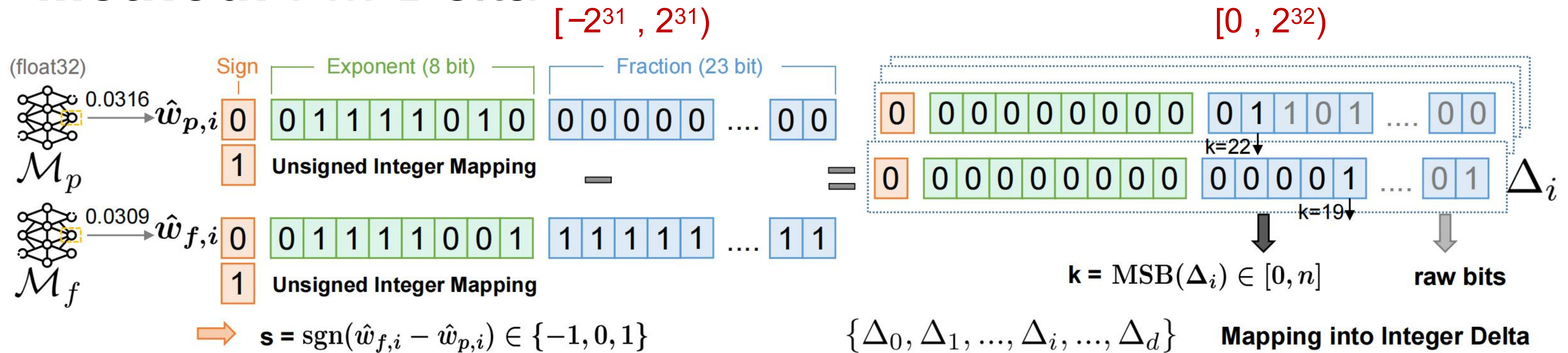
**Theorem 1** (Growth Rate for Model Difference.). *Let  $\mathbf{w}_p$  and  $\mathbf{w}_f$  are the parameters of the pre-trained and fine-tuned models, respectively. The fine-tuning stage involves  $T$  training steps. With learning rate  $\eta_t = \frac{1}{\beta\sqrt{t}}$ ,  $t = 1, 2, \dots, T$ , the distance between  $\mathbf{w}_p$  and  $\mathbf{w}_f$  is*

$$\mathbb{E} [\|\mathbf{w}_f - \mathbf{w}_p\|] \leq \frac{\sqrt{3}\sigma}{\beta} + C_1(\ln T)^{\frac{1}{2}} + \boxed{C_2 T^{\frac{1}{4}}}. \quad (2)$$

where  $\|\cdot\|$  is  $l_2$ -norm;  $f$  is the  $\beta$ -smooth convex loss function on the fine-tuning dataset;  $\mathbf{w}^*$  is the optimal model parameter on the fine-tuning task;  $C_1$  and  $C_2$  are the constants related to the pre-trained model, which are  $C_1 = \left(\frac{9\sigma^2}{4\beta^2} + \frac{f(\mathbf{w}_p) - f(\mathbf{w}^*)}{2\beta}\right)^{\frac{1}{2}}$  and  $C_2 = \left(\frac{\sigma^2}{\beta^2} + \frac{2(f(\mathbf{w}_p) - f(\mathbf{w}^*))}{\beta}\right)^{\frac{1}{2}}$



# Method: FM-Delta



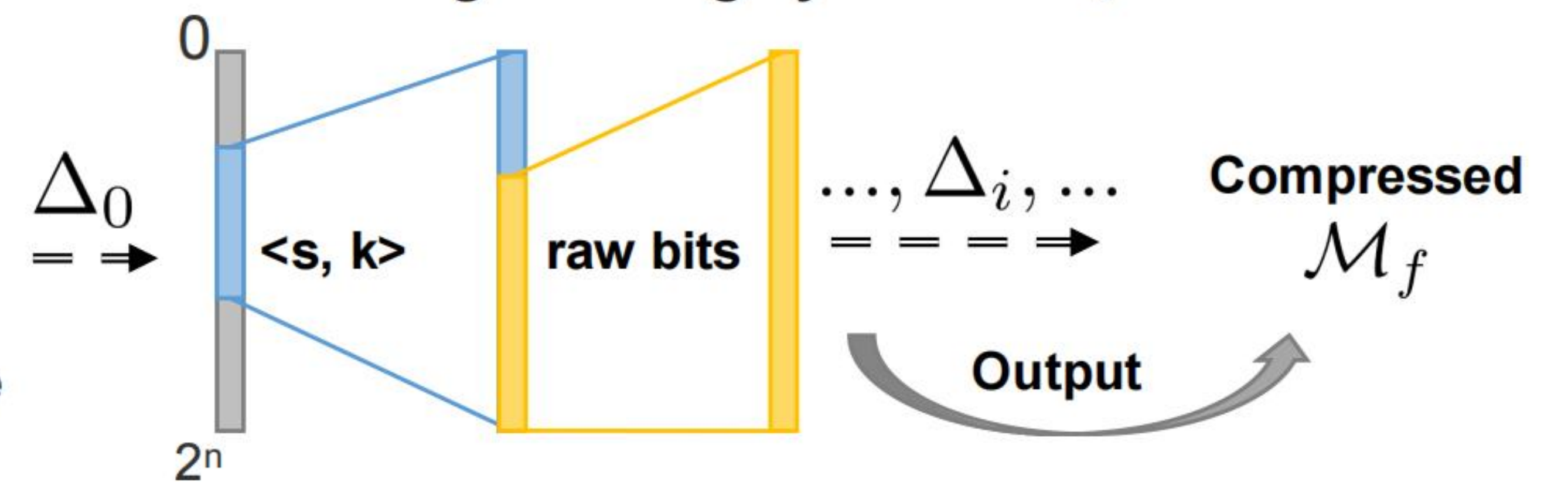
## Probability Modeling

Update symbol probabilities dynamically

	$\langle -1, n \rangle$	...	$\langle -1, 1 \rangle$	$\langle 0, 0 \rangle$	$\langle 1, 1 \rangle$	...	$\langle 1, n \rangle$
Step 0	█		█	█	█		█
Step i	█		█	█	█		█

Update

## Range Coding symbols $\langle s, k \rangle +$ raw bits



## Step 1. Mapping Float into Integer for

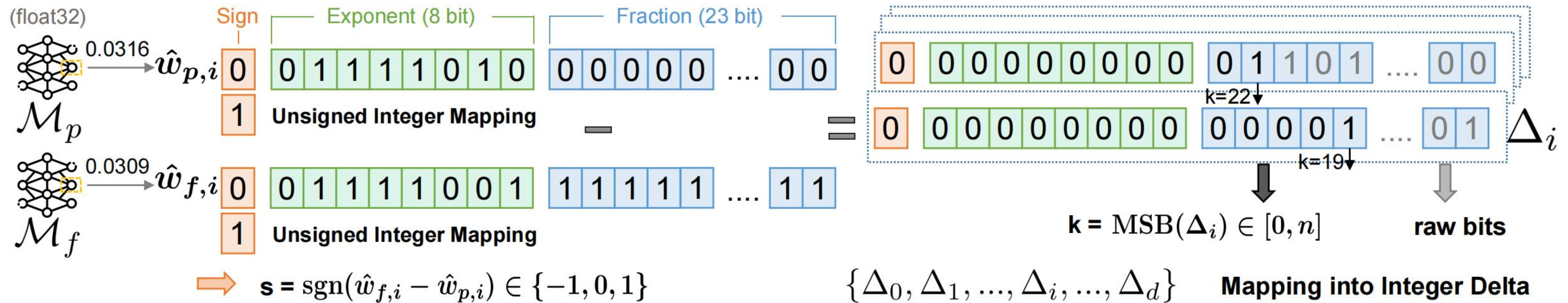
### Delta:

- map floating-points into *unsigned integers*, and performs *integer subtraction*.

		byte number	1 2 3 4
$w_f$	0.0316	$\text{int}(w_p)$	3d 01 6f 00
$w_p$	0.0309	$\text{int}(w_f)$	3c fd 21 ff
$w_f - w_p$	0.0007	$\text{int}(w_f - w_p)$	3a 37 80 34
		$\text{int}(w_f) - \text{int}(w_p)$	00 04 4d 01



# Method: FM-Delta



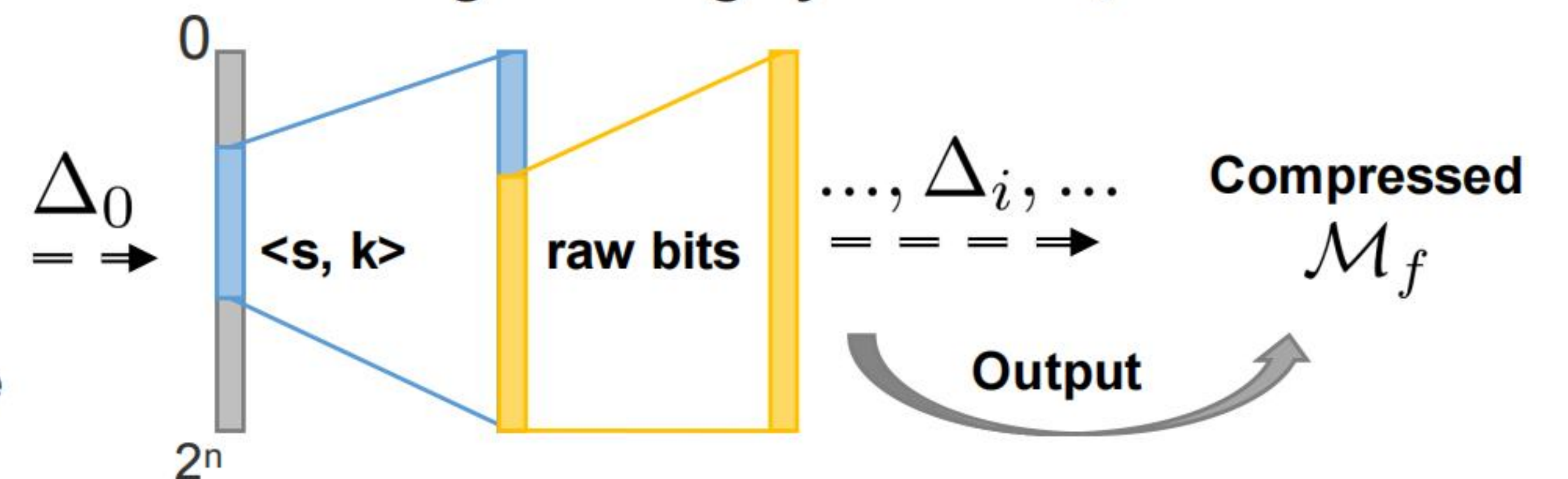
## Probability Modeling

	<-1, n>	...	<-1, 1>	<0, 0>	<1, 1>	...	<1, n>
Step 0	█		█	█	█		█
Step i	█		█	█	█		█

Update symbol probabilities dynamically

Update

## Range Coding symbols <s, k> + raw bits



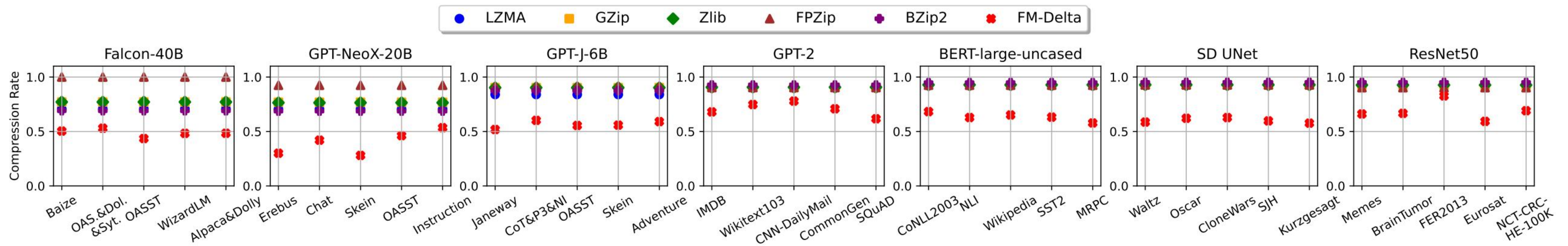
## Step 2. Compression with Range Coding:

- Symbolization: <sign  $s$ , most significant bit  $k$ > of int delta as symbols.
- Probability Model: a **quasi-static probability modeler** to termly update symbol frequencies.
- Encoding: the symbols with the raw bits on all delta elements through range scaling.
- Decoding: map the encoded value back to the original symbol range --> reverse-mapping delta --> original float fine-tuned model



# Results: Compression Rate

Family	Pretrained Size	Finetuned Num.	Original Storage (GB)	Storage after Compression (GB)					
				LZMA	Gzip	Zlib	FPZip	BZip2	FM-Delta
Falcon-40B (fp16)	40B	5	461.6	349.3	373.4	373.4	456.9	342.7	<b>270.8 (59%)</b>
		10	846.3	621.7	669.9	669.9	837.8	608.5	<b>473.9 (56%)</b>
GPT-NeoX (fp16)	20B	5	230.8	162.9	177.2	176.4	213.4	158.6	<b>112.4 (49%)</b>
		10	423.2	298.7	324.9	323.4	391.2	290.7	<b>205.2 (48%)</b>
GPT-J (fp16)	6B	5	68.4	57.2	60.6	60.6	61.2	58.7	<b>44.6 (65%)</b>
		10	125.3	104.8	111	111	112.2	107.6	<b>73.8 (59%)</b>
GPT-2	124M	50	24.2	21.8	22	22	21.9	22.5	<b>15 (62%)</b>
		100	48	43.2	43.5	43.5	43.4	44.5	<b>28.7 (60%)</b>
Bert-large-uncased	336M	50	63.7	58.6	59.1	59.1	58.9	60.4	<b>41.3 (65%)</b>
		100	126.1	116.1	117.1	117.1	116.6	119.6	<b>82.1 (65%)</b>
Stable-Diffusion UNet	860M	5	19.2	17.7	17.8	17.8	17.8	18.3	<b>12.8 (67%)</b>
		10	35.2	32.5	32.7	32.7	32.6	33.5	<b>23.5 (67%)</b>
ResNet50	26M	10	1.1	0.9	0.9	0.9	0.9	0.9	<b>0.7 (68%)</b>
		20	2	1.7	1.7	1.7	1.7	1.8	<b>1.3 (66%)</b>
Avg. Compression Throughput (MB/s)				4.9	36.1	35.6	83.5	12.1	<b>109.7</b>
Avg. Decompression Throughput (MB/s)				24.8	236.6	<b>260.8</b>	80.6	23.8	100.9





# Results: Cloud Cost Analysis

*Is the cost of decompressing models lower than storing them uncompressed in the cloud?*

- regard model download as a binomial distribution

$$P(X = k) = C_n^k \cdot \left( \frac{10}{30 \times 24 \times 60} \right)^k \cdot \left( 1 - \frac{10}{30 \times 24 \times 60} \right)^{n-k}$$

$k$  represents the number of concurrent download requests in a given minute.

**Goal:** maximize loadable models  $n$ , s.t.  $\sum_{k=t}^n P(X = k) \leq 0.01$

$$\Rightarrow n_{\max} = 35300$$

**100% storage vs. 50% storage + server purchase fee  $\longrightarrow$  40% cost reduction**



# Thank you!

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