

# Collaborative Cognitive Diagnosis with Disentangled Representation Learning for Learner Modeling

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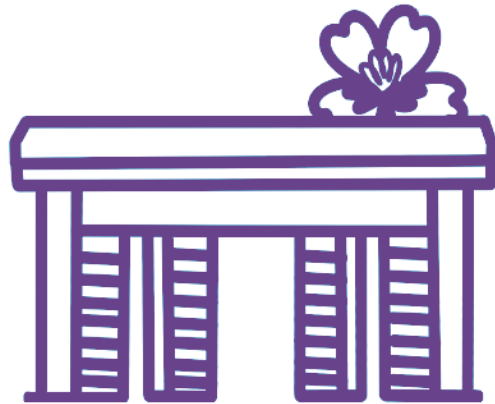
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STATE KEY LABORATORY OF  
COGNITIVE INTELLIGENCE



Reporter: Weibo Gao



# Outline



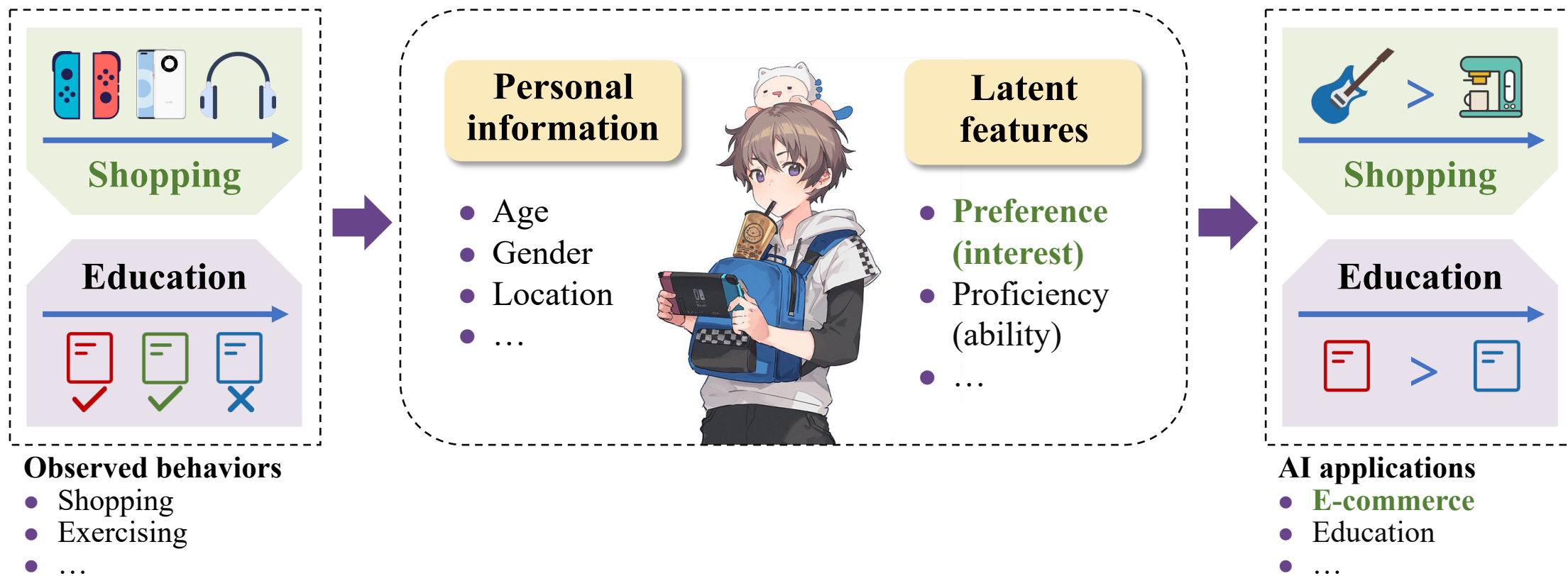
**1 Introduction**

**2 Coral Model**

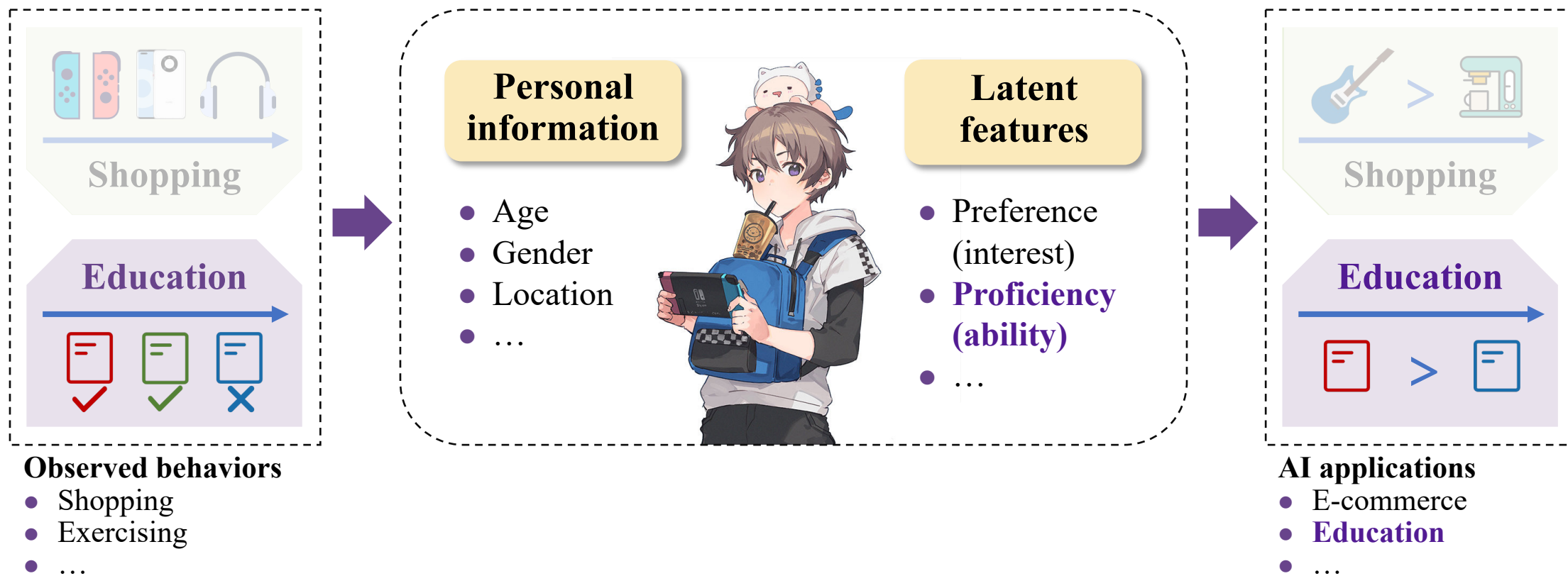
**3 Experiments**

**4 Conclusion**

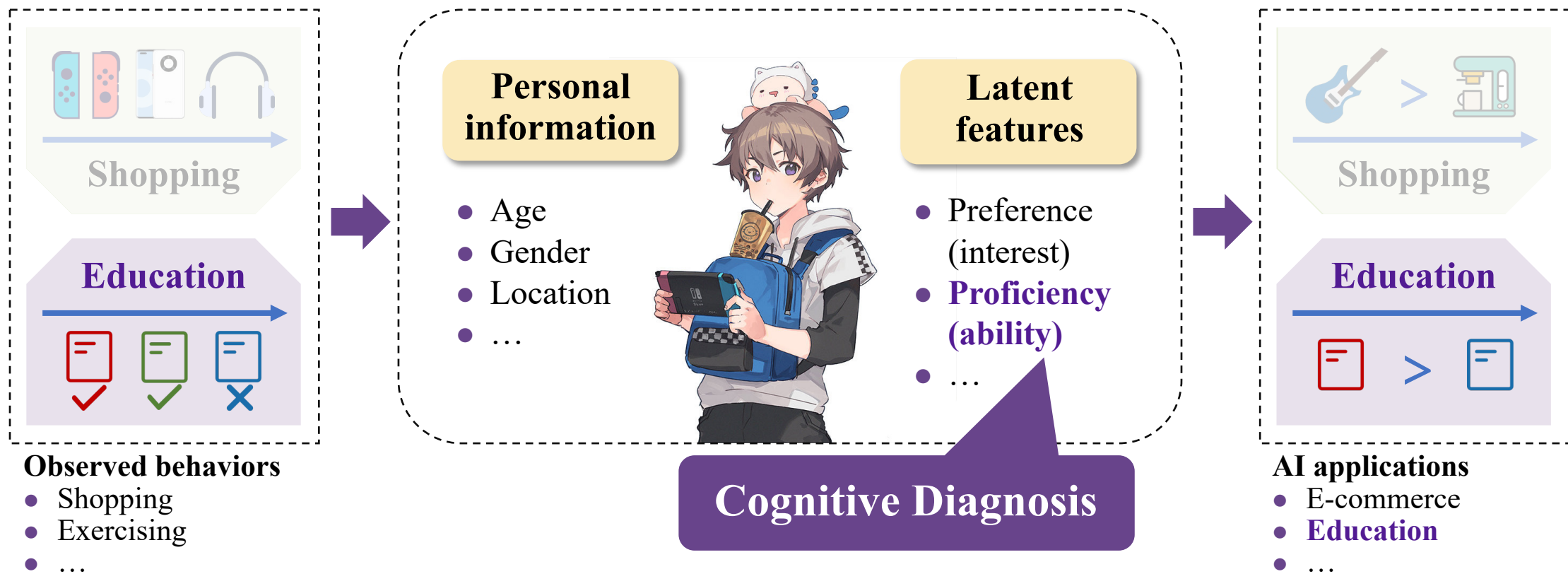
□ In the applications of AI, it needs to characterize the difference of individuals in both personal information and latent features



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## □ Cognitive Diagnosis (CD)

- **Goal:** Diagnosing the **cognitive states** of each learner (i.e., **proficiency** on specific knowledge concepts) by fitting their practice records (i.e., practice correctness)
- **Components:** Learners, questions and knowledge concepts
- **Applications:** Supporting personalized tutoring services

Questions	Knowledge concepts	Bob	Alice	Nancy
q <sub>1</sub>	A	✓	✓	✓
q <sub>2</sub>	B	✗	✓	✓
q <sub>3</sub>	A, B	✓	✓	?
q <sub>4</sub>	C, D	✓	✗	✗
q <sub>5</sub>	C, E	✓	✓	?

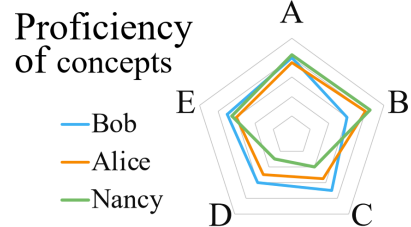
Practice records

Cognitive Diagnosis

**Legend**

A: Function    D: Cube  
 B: Derivative    E: Cone  
 C: Number

✓ / ✗ : Correct / wrong logs



Cognitive states

Applying

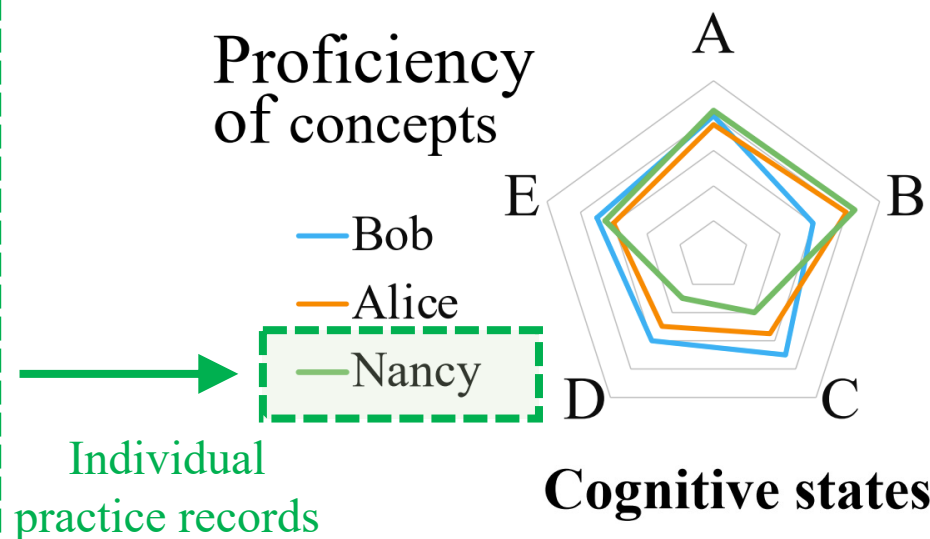
- Question/course recommendation
- Adaptive testing
- ...

Tutoring services

- Current **CD** models mainly focus **inner-learner** modeling, but ignore **inter-learner** information
  - **Inner-learner: Individual** attributions and practice records
  - **Inter-learner: Collaborative** clues between learners with similar cognitive states

Questions	Knowledge concepts	Bob	Alice	Nancy
$q_1$	A	✓	✓	✓
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$q_4$	C, D	✓	✗	✗
$q_5$	C, E	✓	✓	?

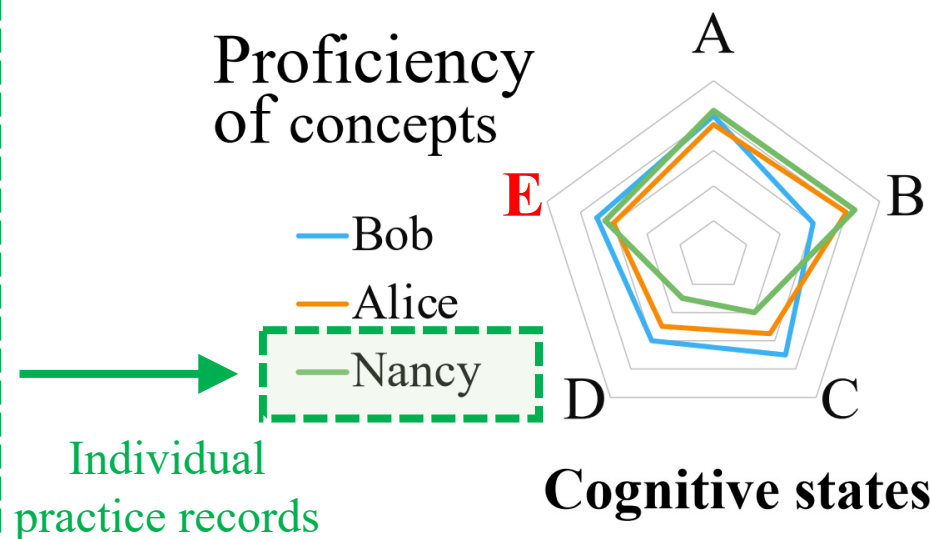
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Practice records

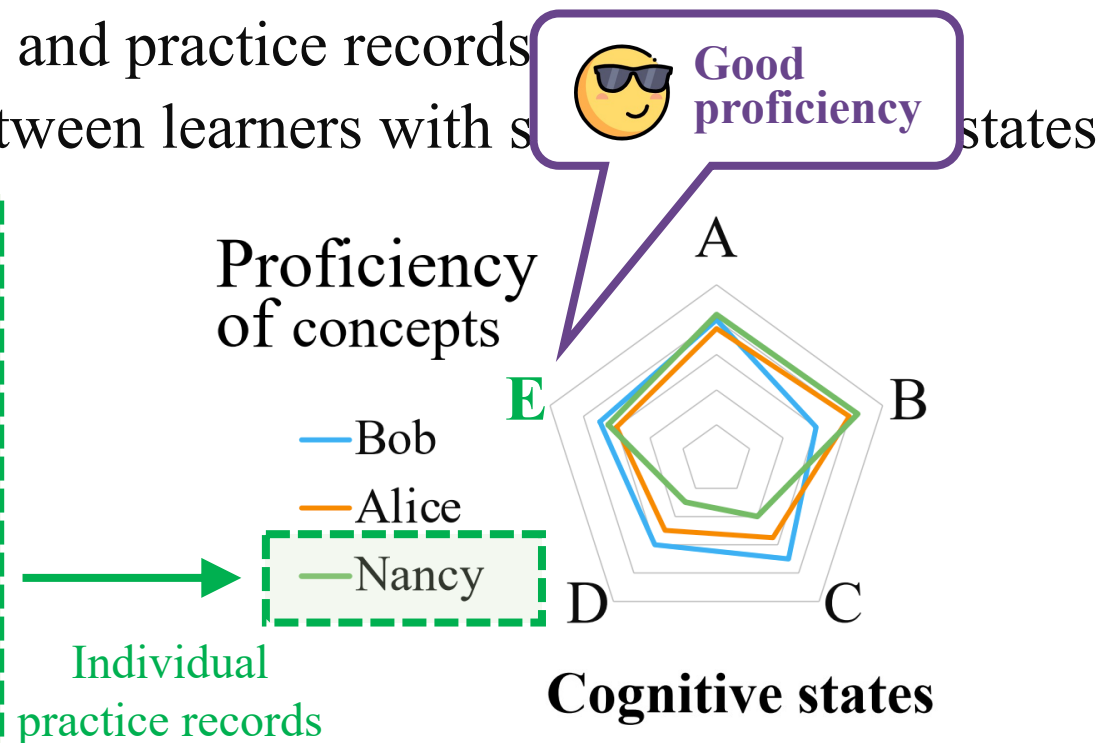




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$q_3$	A, B	✓	✓	?
$q_4$	C, D	✓	✗	✗
$q_5$	C, E	✓	✓	?

Collaborative clues: A dashed purple box highlights the 'Bob' and 'Alice' columns for  $q_5$ . A purple arrow points from this box to a green checkmark below it.





# Motivation



## □ Our research goal

An ideal cognitive diagnosis model should consider both inner- and inter- learner information

# Outline



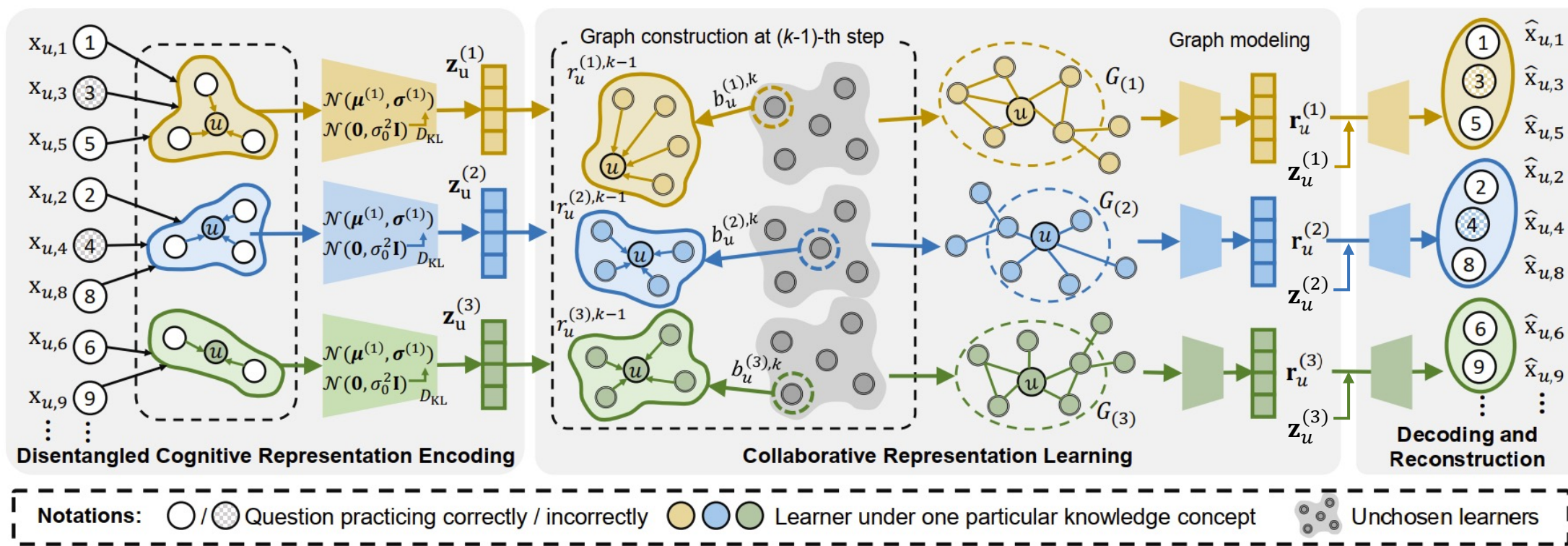
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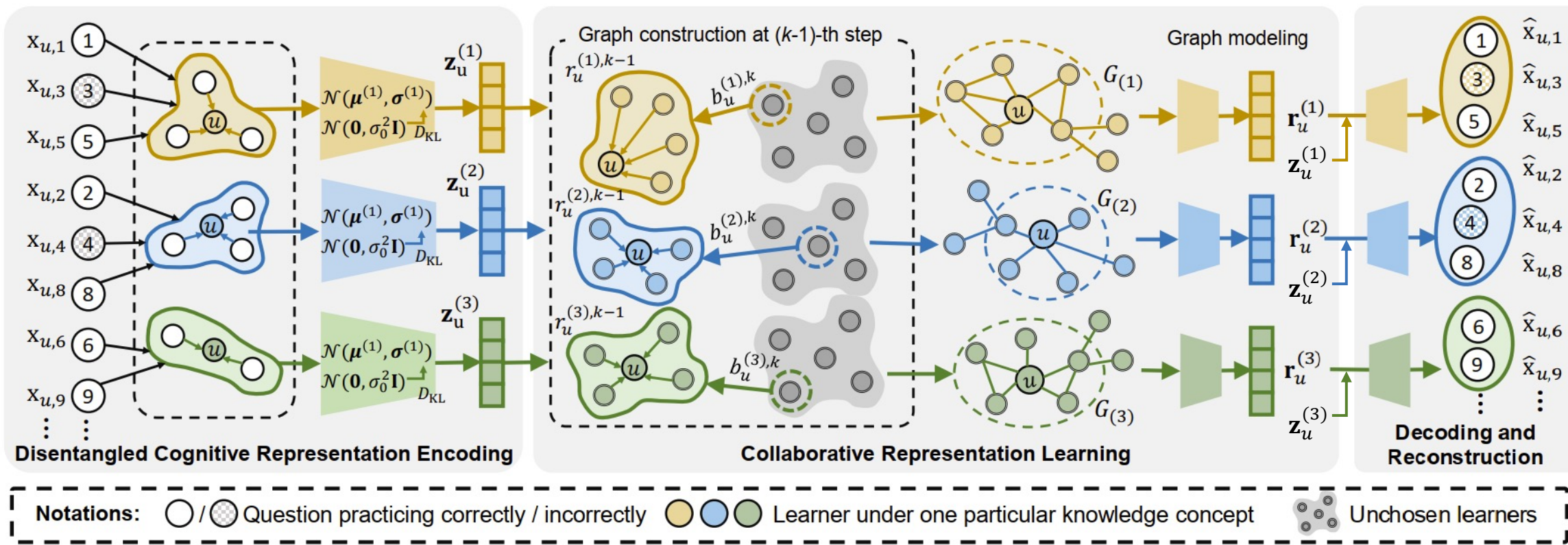
**2** Coral Model

**3** Experiments

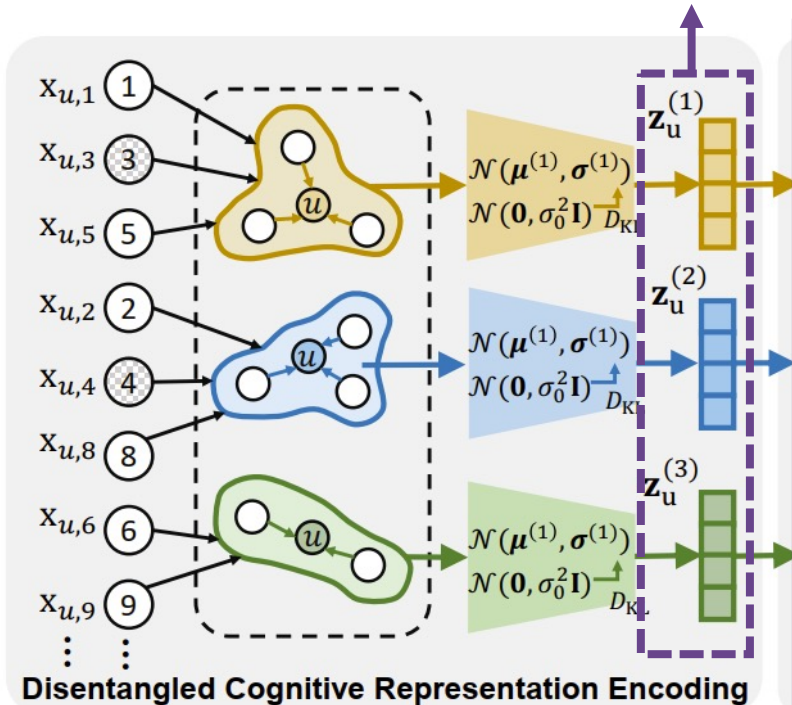
**4** Conclusion

We propose **Coral**, a **Collaborative** cognitive diagnosis model with **disentangled** representation Learning for both **inner-** and **inter-** learner information Modeling





## Disentangled inner-learner cognitive states



## Inner-learner modeling:

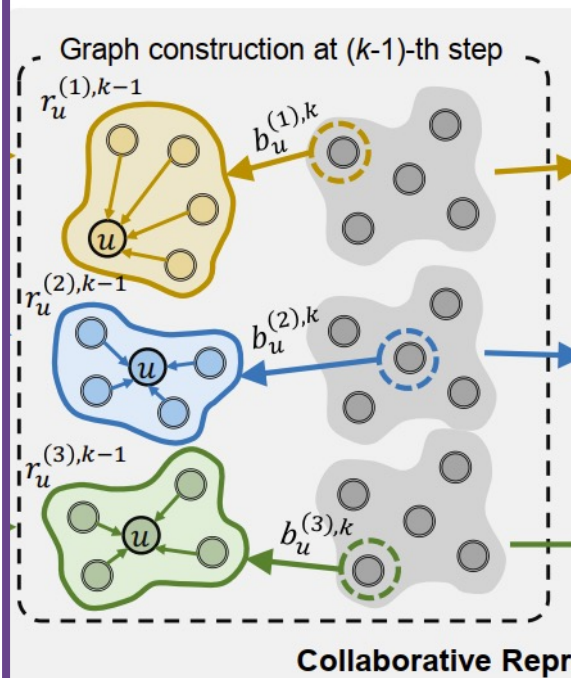
- Disentangle the learner's cognitive state into multiple components
- Optimize disentangled cognitive states by **fitting their practice performance**

$$p_{\Theta}(\mathbf{x}_u) = \mathbb{E}_{p(\mathbf{C})} \left[ \int p_{\Theta}(\mathbf{x}_u | \mathbf{z}_u, \mathbf{C}) p_{\Theta}(\mathbf{z}_u) d\mathbf{z}_u \right]$$

Notations: ○ / ⊗ Question practicing correctly / incorrectly    ● ● ● Learner under one particular knowledge concept    ⊙ ⊙ ⊙ Unchosen learners

## Inter-learner modeling (1/2):

- Find  $K$  collaborative neighbors with similar cognitive states for each learner
- Theoretically** derive the optimal condition ( $\max \log p_{\Theta}(G | V, \mathbf{Z})$ ) for **building the collaborative graph of learners**



## Property 3.

$\max \log p_{\Theta}(G | V, \mathbf{Z})$  is bounded as follows:

$$\max \log p_{\Theta}(G | V, \mathbf{Z}) \geq - \sum_{c=1}^C \sum_{u=1}^M \sum_{k=1}^K \mathcal{L}_u^{(c),k}$$

$$\mathcal{L}_u^{(c),k} = - \frac{\exp \left( f_{(c)} \left( b_u^{(c),k}; r_u^{(c),k-1} \right) \right)}{\sum_{v \in V_u^{(c)}} \exp \left( f_{(c)} \left( v; r_u^{(c),k-1} \right) \right)}$$

From steps 1 to  $K$ , **iteratively** search for the  **$k$ -th** collaborative neighbor with **the most similar cognitive state** to the current **context** (existing  **$(k-1)$ -th** neighbors).

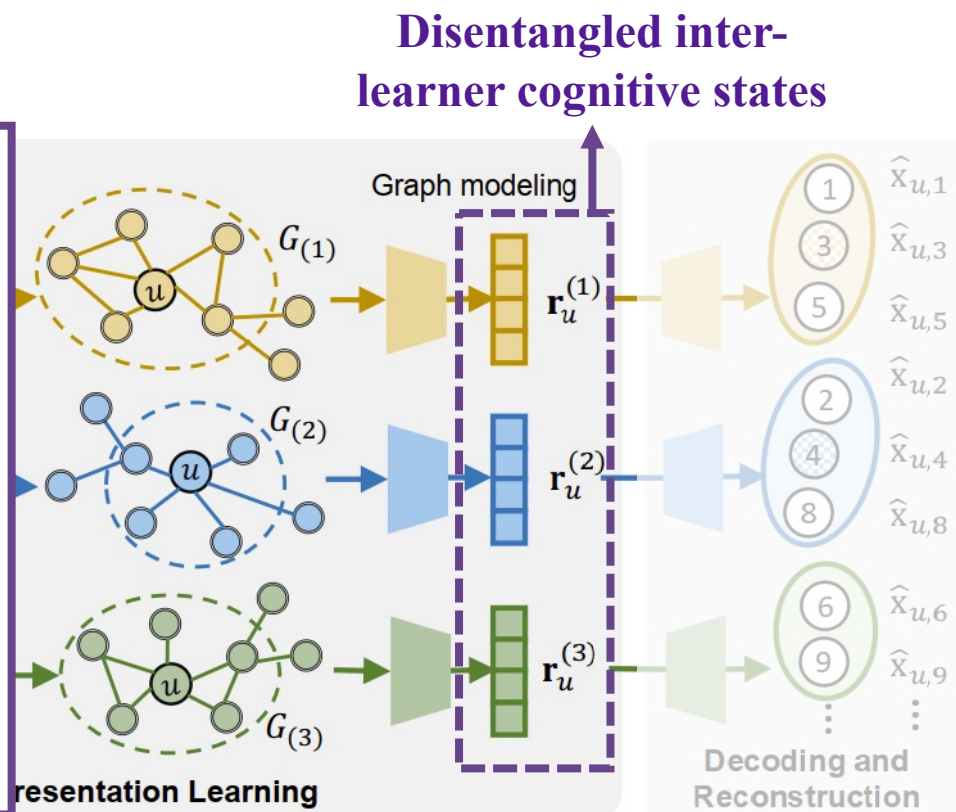
Notations:  $\bigcirc / \bigotimes$  Question practicing correctly / incorrectly  $\bigcirc / \bigotimes$  Learner under o

## Inter-learner modeling (2/2):

- Based on learner collaborative graphs at each disentangled component, we design a **context-aware GCN** to learn **collaborative learner cognitive states**

$$\mathbf{r}_u^{(c)} = \frac{1}{|\mathcal{N}_u^{(c)}|} \sum_{v \in \mathcal{N}_u^{(c)}} s_{u,v}^{(c)} \cdot \hat{\mathbf{z}}_v^{(c)}$$

$$s_{u,v}^{(c)} = \frac{\hat{\mathbf{z}}_u^{(c)T} \cdot \hat{\mathbf{z}}_v^{(c)}}{\sum_{j \in \mathcal{N}_u^{(c)}} \hat{\mathbf{z}}_u^{(c)T} \cdot \hat{\mathbf{z}}_j^{(c)}} + \frac{f_{(c),v}}{\sum_{k=1}^K f_{(c),v_k}}$$



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## Inner- and inter- view alignment

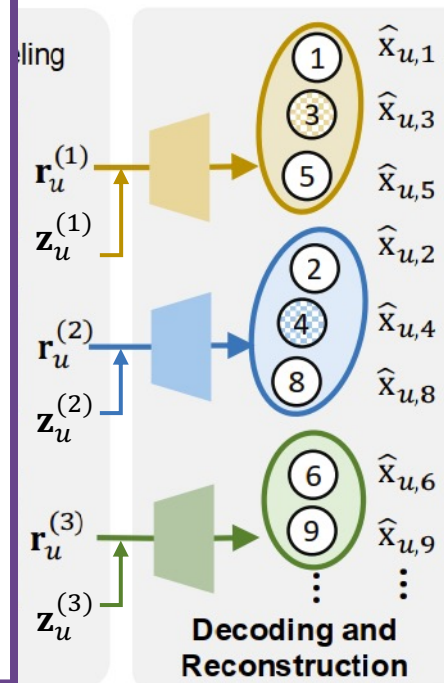
□ Achieve the co-disentanglement of inner- and inter- learner cognitive states

$$\tilde{\mathbf{z}}_u = \mathbf{z}_u + \mathbf{r}_u$$

## Optimization

$$\arg \min \mathcal{L} = \sum_{u=1}^M \left[ \sum_{x_{u,i} \in \mathbf{x}_u} \alpha \cdot BCE(x_{u,i}, p_{\Theta}(x_{u,i} | \mathbf{z}_u, \mathbf{C})) - \beta \cdot D_{\text{KL}}^u + \sum_{x_{u,i} \in \mathbf{x}_u} BCE(x_{u,i}, p_{\Theta}(\hat{x}_{u,i})) \right]$$

s.t.  $\arg \max \sum_C \sum_K \mathcal{L}_u^{(c),k}$



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## □ Dataset

- Each dataset contains learner practice correctness on specific questions

Datasets	ASSIST	Junyi	NeurIPS2020EC
#students	1,256	1,400	1,000
#questions	16,818	674	919
#knowledge concepts	120	40	30
#concepts per exercise	1.21	1	4.02
#records	199,790	70,797	331,187
#records per student	159.07	50.67	331.19
#correct records / #incorrect records	67.08%	77.20%	53.87%

Table 1: The statistics of three datasets.

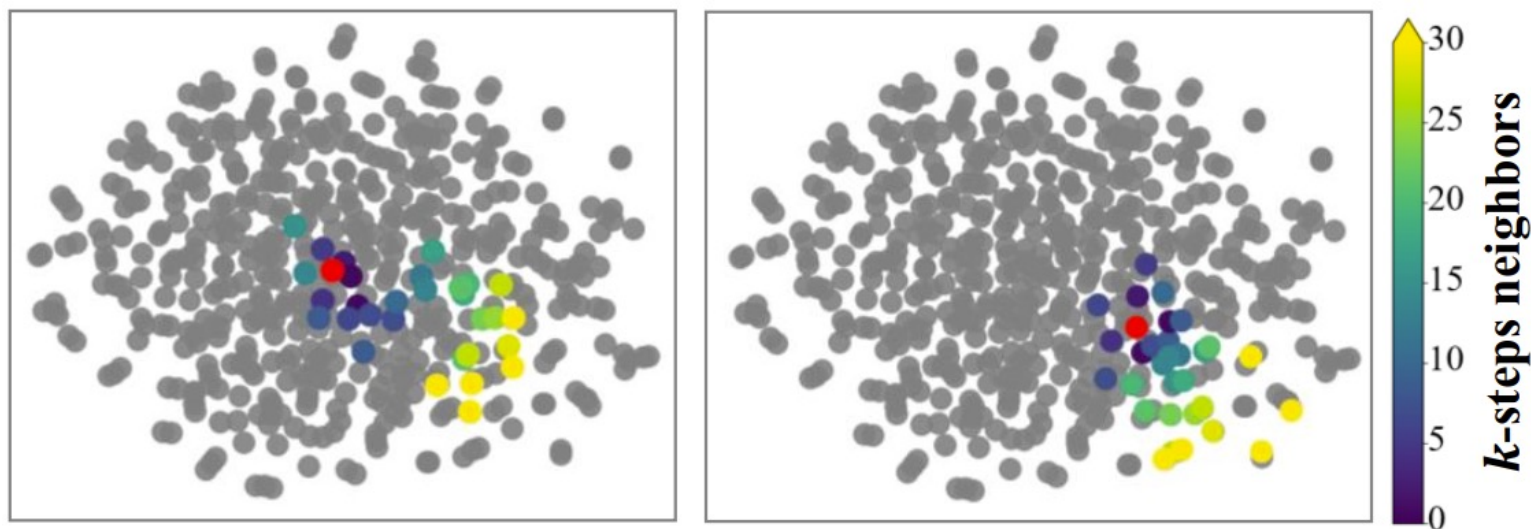
## □ Evaluation of learner practice performance prediction

Dataset	Method	Metric			
		ACC ↑	AUC ↑	F1-score ↑	RMSE ↓
ASSIST	IRT	69.36	69.81	78.14	45.61
	MIRT	71.26	72.59	79.80	44.50
	PMF	71.34	72.27	80.68	48.67
	NCDM	72.27	74.27	79.97	48.67
	KaNCD	<b>72.43</b>	<b>75.38</b>	80.22	48.67
	RCD	72.04	73.14	80.60	43.74
	DCD	70.33	73.98	79.09	43.94
	<b>Coral</b> 🍌	71.53	74.72	<b>81.16</b>	<b>43.66</b>
Junyi	IRT	79.26	76.46	87.54	38.38
	MIRT	77.74	74.46	86.05	40.29
	PMF	79.65	77.17	88.18	44.10
	NCDM	79.91	78.91	87.73	38.35
	KaNCD	<b>81.79</b>	80.93	89.02	36.11
	RCD	81.02	80.22	88.00	37.23
	DCD	79.29	79.55	87.62	37.83
	<b>Coral</b> 🍌	81.15	<b>80.94</b>	<b>89.12</b>	<b>36.08</b>

Dataset	Method	Metric			
		ACC ↑	AUC ↑	F1-score ↑	RMSE ↓
NeurIPS2020EC	IRT	70.11	75.60	71.59	44.68
	MIRT	69.95	75.52	71.24	45.51
	PMF	69.85	75.39	72.62	48.33
	NCDM	71.66	78.57	71.36	43.21
	KaNCD	71.28	77.60	72.50	43.71
	RCD	70.43	77.25	72.64	44.01
	DCD	71.53	75.63	71.13	45.60
	<b>Coral</b> 🍌	<b>71.72</b>	<b>78.88</b>	<b>72.82</b>	<b>43.20</b>

The Coral model nearly **outperforms** all baseline models across three datasets

- Visualization of iteratively searching collaborative neighbors
  - Randomly select two learners as examples, and visualize their collaborative neighbors searching processes



Coral organizes neighbors according to **cognitive states** and exemplifying a compelling strategy for neighbor selection that takes into account **cognitive similarity**

## □ Evaluation of the disentanglement effectiveness

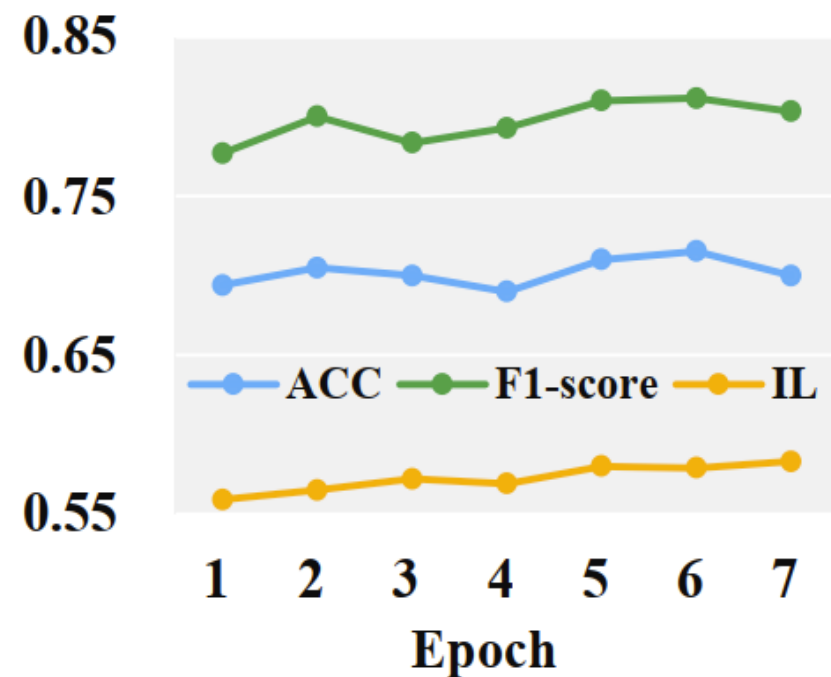
### □ Metric:

$$IL = \sum_{u=1}^M IL(u)$$

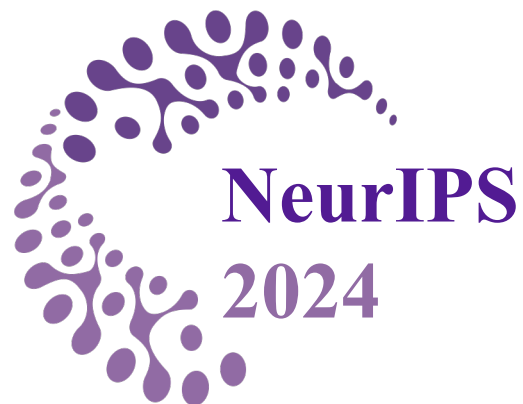
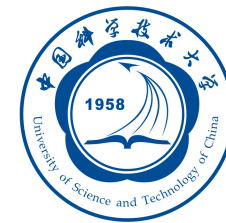
$$IL(u) = \frac{1}{C} \sum_{c=1}^C \frac{2}{d(d-1)} \sum_{1 \leq i, j \leq d} |z_u^{(c)}[i] - z_u^{(c)}[j]|$$

□ The higher the  $IL$ , the higher the degree of disentanglement

- Coral gradually achieves a **high degree of disentanglement** during the training process
- Model performances generally exhibit a **positive correlation with the degree of disentanglement**



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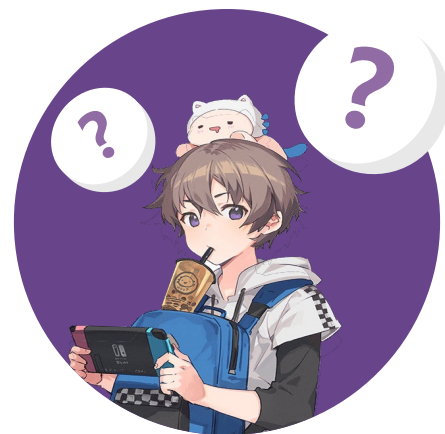
# Conclusion



- Introduce **collaborative modeling** into **cognitive diagnosis (CD)**
  - An ideal cognitive diagnosis model should consider both **inner-** and **inter-** learner information
- Propose the **Coral** model
  - **Inner-view: Disentangle** learners' cognitive states into multiple components
  - **Inter-view:** (1) **Iteratively** construct learner collaborative graphs at each disentangled components; (2) Design the **context-aware GCN** to model collaborative clues
  - **Co-disentanglement: Fuse** both **inner-** and **inter-** learner cognitive states
- Experiments
  - Proving Coral's effectiveness of **collaborative modeling** and **disentanglement**
  - Project homepage: <https://github.com/bigdata-ustc/Coral>



# Thank you



## Q & A



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