# **Selective Generation for Controllable Language Models**

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**Motivation**



▶ Selective classification is a **certified** risk control method, which rejects instances as needed, to grant a **desired risk**  $\varepsilon$  with **high probability**  $1 - \delta$ .

#### **Motivation**



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**Motivation**



#### **Motivation**

## **Inference Phase**

#### **IDK...**



**Motivation**

#### **Classification**



**Motivation**

#### **Classification**



**Motivation**



**Motivation**



**Motivation**



▶ **Selective prediction** is also important to be applied to **generative tasks**. ▶ However, unlike exact match (EM) in **classification**, it is difficult to define a **correctness metric**.

 $\implies$  We employ **textual entailment**:  $E_{\text{true}}(\mathbf{y}) := {\hat{\mathbf{y}}} \in \mathcal{Y} | \hat{\mathbf{y}}$  implies  $\mathbf{y}$ .

# **Why Semi-Supervised Learning?**

#### **Motivation**



 $\triangleright$  We can avoid *metric misalignment* in generation by leveraging entailment. ▶ However, labeling is expensive.

# **Why Semi-Supervised Learning?**

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▶ We can avoid *metric misalignment* in generation by leveraging entailment. ▶ However, labeling is expensive.

> $\implies$  We leverage question-answering pairs without entailment via **semi-supervised learning** (SSL).

**Method**



With the previously defined **textual entailment**  $E_{true}(\mathbf{y})$ , We can define **FDR-E**, the false discovery rate with respect to the textual entailment relation, as follows:

$$
\mathbb{P}\{G(\mathbf{x}) \notin E_{\text{true}}(\mathbf{y}) \mid \hat{S}(\mathbf{x}) \neq \text{IDK}\}\
$$

**Method**



$$
\underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{G(\mathbf{x}) \notin E_{\text{true}}(\mathbf{y})\}}_{(A)} = \underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{v=1\}}_{(B)} \underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{e=0\}}_{(C)} + \underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{v=0\}}_{(D)} \underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{e=0\}}_{(E)}
$$

**Method**



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$$

**Method**



$$
\underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{\mathbf{G}(\mathbf{x})\mathbf{F}_{\hat{D}_{\hat{S}}}\{\mathbf{E}=\mathbf{0}\}}_{\mathbf{E}}(y)\}=\underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{v=1\}}_{\mathbf{B}}\underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{e=0\}}_{\mathbf{B}}+\underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{v=0\}}_{\mathbf{D}}
$$

**Method**



#### **Lemma 1**

(E) is decomposed as follows:

$$
\underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{e=0\}}_{(E)} = \underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{e=0,\hat{e}=1\}}_{\text{FER}} - \underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{e=1,\hat{e}=0\}}_{\text{FNER}} + \underbrace{\mathbb{P}_{\mathcal{D}_{\hat{S}}}\{\hat{e}=0\}}_{\text{NER}}.
$$

**Method**



**Method**

#### **Entailment Set Learning**

 $A_{\text{FER}}$  returns  $\hat{E}$  which controls the FER of pseudo-labeled examples, *i.e.*,

$$
\mathbb{P}\{\mathcal{R}_{\mathsf{FER}}(\hat{E}) \le \varepsilon_E\} \ge 1 - \delta_E.
$$

▶ We use  $\hat{E}$  as a pseudo-labeling function for SSL – see our paper!

#### **Lemma 2**

If  $\hat{E} \coloneqq \mathcal{A}_{\text{FER}}(\hat{\mathbf{Z}}_E)$  satisfies the above guarantee, we have

$$
\mathbb{P}_{\mathcal{D}}\{e=0\} \leq \varepsilon_E-L_{\mathsf{Binom}}(\hat{k};|\hat{\mathbf{Z}}_E|, \delta_E'/2) + U_{\mathsf{Binom}}(\hat{l};|\hat{\mathbf{Z}}_U|, \delta_S')=:U_{\mathsf{SSL}}
$$

 $\blacktriangleright$  We find an optimal  $\varepsilon_E$  that minimizes  $U_{\sf SSL}$ , resulting  $U_{\sf SSL}^{\sf OPT}$  – see our paper!

# **Controllable Guarantee**

#### **Method**

# **Algorithm** Our  ${\sf semi-supervised}$  method  ${\cal A}^{\sf Semi}_{{\sf SGen}}$  solves the following optimization problem:  $\text{find}_{\hat{S} \in \mathcal{H}} \; \hat{S}$  subj. to  $w_{\textsf{SL}} U_{\textsf{SL}} + w_{\textsf{SSL}} U_{\textsf{SSL}}^{\textsf{OPT}} \leq \varepsilon_S$

#### **Theorem 1**

 ${\cal A}^{{\sf Semi}}_{{\sf SGen}}$  satisfies the following controllable guarantee on the <code>FDR-E</code>, i.e.,

$$
\mathbb{P}\left\{\mathbb{P}\left\{G(\mathbf{x}) \notin E_{\text{true}}(\mathbf{y}) \mid \hat{S}(\mathbf{x}) \neq \text{IDK}\right\} \leq \hat{U}\right\} \geq 1 - \delta.
$$

## **Experiment**





 $\blacktriangleright$  SGen<sup>Semi</sup> can capture correctness better than SGen<sub>EM</sub>.

#### **Experiment**



▶ More unlabeled samples are beneficial to achieving better efficiency.

#### **Experiment**



**▶** The FDR-E for  $\hat{S}$  is well controlled below  $\varepsilon_S$ , desired FDR-E, under the test environment.

#### **Conclusion**

▶ We leverage logical **entailment** and propose a novel **semi-supervised** learning approach for **selective generation**, demonstrating its theoretical and empirical efficacy.

