
GraphMorph: Tubular Structure Extraction by Morphing Predicted Graphs

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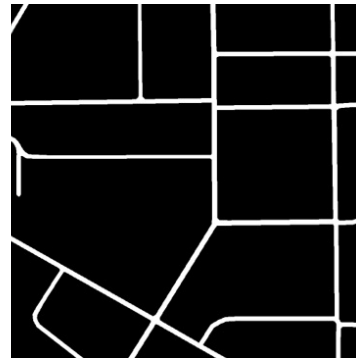
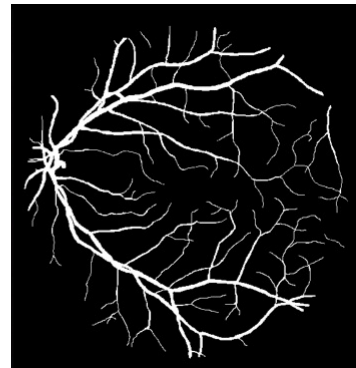
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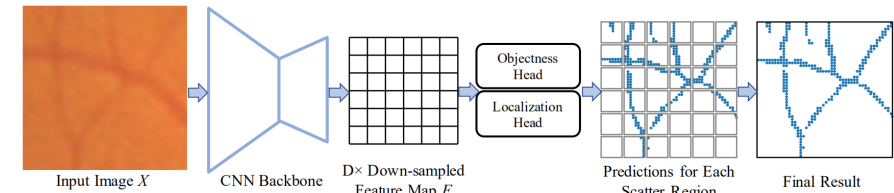
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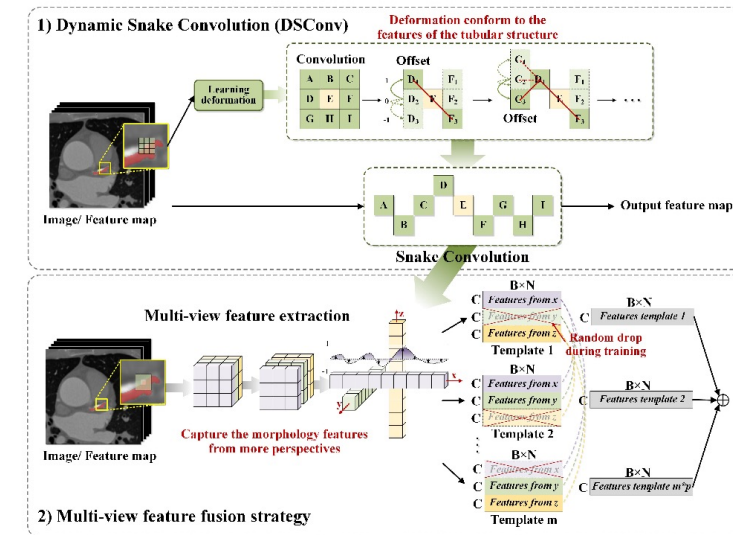
Tubular Structure Extraction



PointScatter

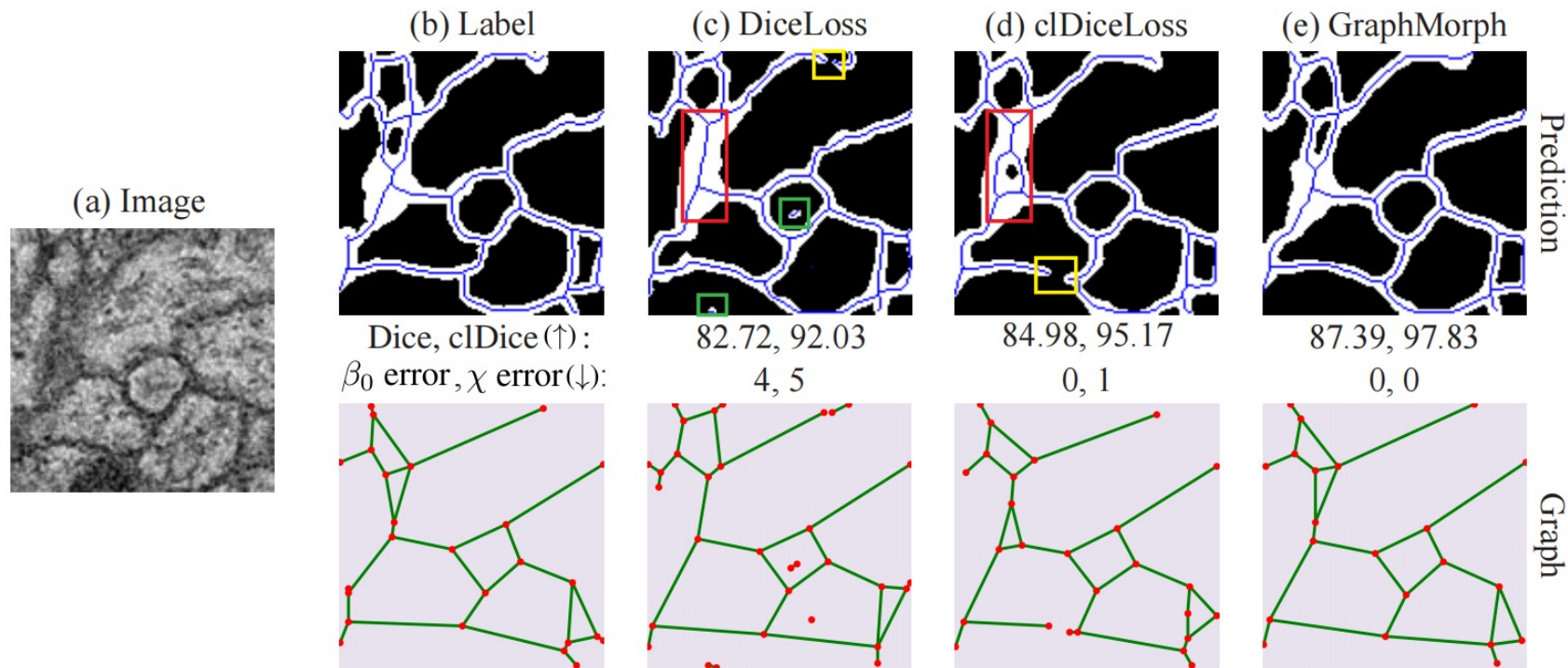


DSCNet

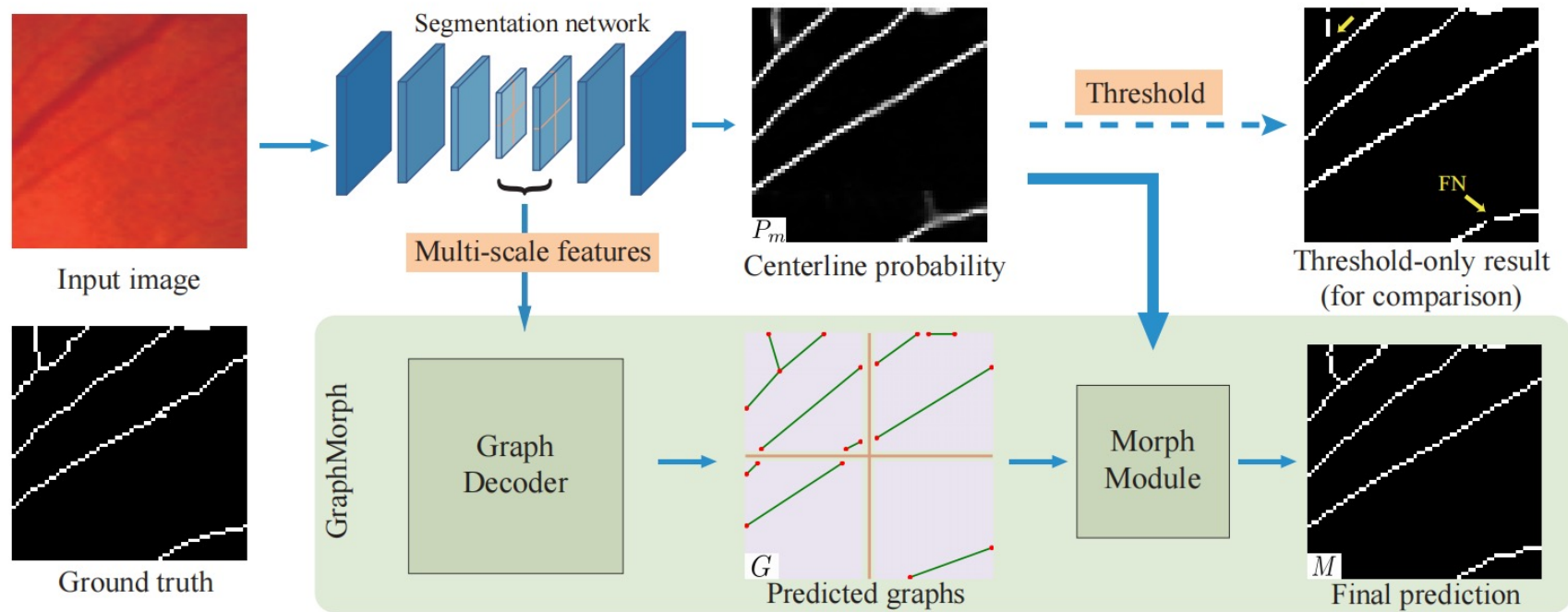


Motivation & Introduction

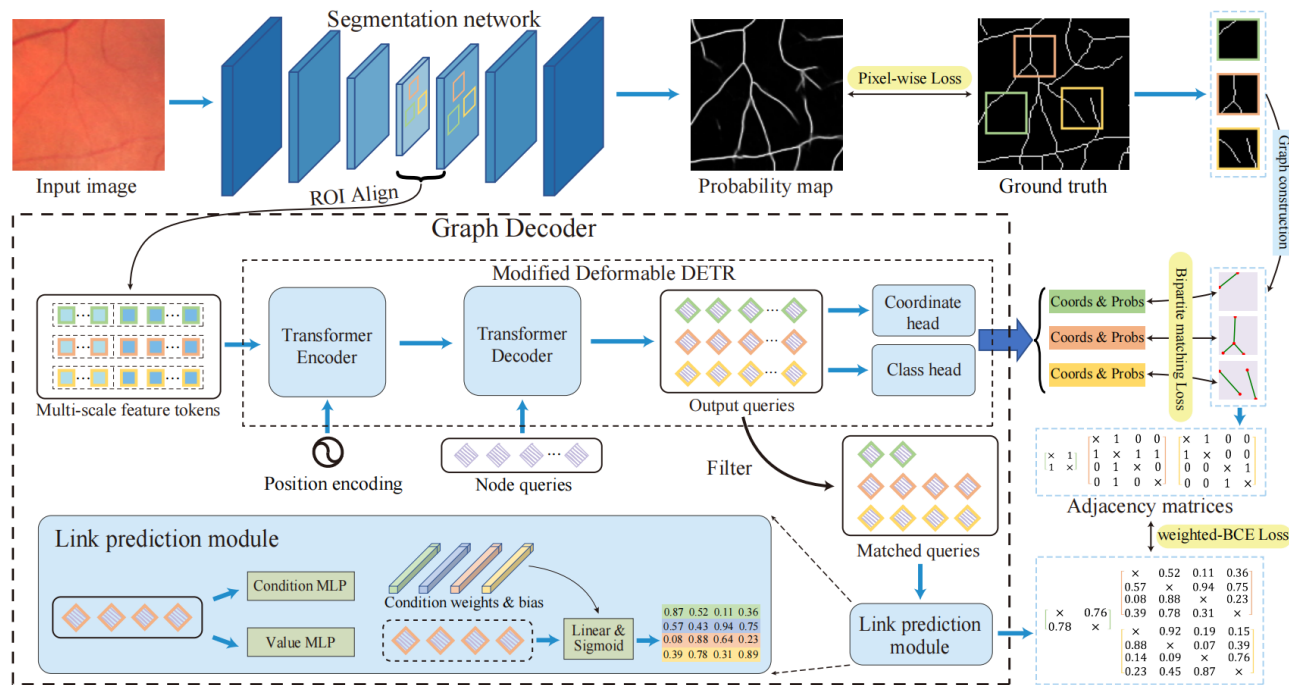
Branch-level features are more essential for accurately capturing the nuances of tubular structures!



Overview of GraphMorph



Graph Decoder



Loss functions

$$\mathcal{L}_{\text{Hungarian}}(y, \hat{y}) = \sum_{r=1}^R \sum_{i=1}^K \left[\lambda_{\text{class}} \cdot \mathcal{L}_{\text{focal}}(\hat{s}_{\hat{\sigma}(i)}^r, c_i^r) + \lambda_{\text{coord}} \cdot \mathbb{1}_{\{c_i^r \neq \emptyset\}} \mathcal{L}_{\text{coord}}(\hat{v}_{\hat{\sigma}(i)}^r, v_i^r) \right]$$

$$\mathcal{L}_{\text{Adjacency}}(y, \hat{y}) = \sum_{r=1}^R \left\{ \frac{0.5}{N_{\text{pos}}} \sum_{i \neq j}^{P_r} \sum_{j=1}^{P_r} (A_{ij}^r \log \tilde{A}_{ij}^r) + \frac{0.5}{N_{\text{neg}}} \sum_{i \neq j}^{P_r} \sum_{j=1}^{P_r} [(1 - A_{ij}^r) \log(1 - \tilde{A}_{ij}^r)] \right\}$$

Morph Module

Algorithm 1 Morph Module

Input: Node set V , Edge set E , Probability map P_m

Output: Centerline mask M

Initialize M as a zero matrix with the same size as P_m

Initialize C_m where $C_m[i][j] = 1 - P_m[i][j]$ for each element

for all edges (u, v) in E **do**

$path \leftarrow \text{SkeletonDijkstra}(u, v, C_m, p_{thresh})$

for all points p in $path$ **do**

Set $M[p.x][p.y] = 1$

end for

end for

return M

Algorithm 2 SkeletonDijkstra Algorithm

Input: Start point s , End point e , Cost map C , Path threshold p_{thresh}

Output: Minimum cost path from s to e under threshold p_{thresh}

Initialize priority queue Q with $(0, [s])$

Initialize visited set Vis

while not Q empty **do**

$(cost, path) \leftarrow Q.pop()$

$curr \leftarrow$ last element of $path$

Add $curr$ to Vis

if $curr = e$ **then**

$avg \leftarrow cost / \text{length}(path)$

if $avg > p_{thresh}$ **then**

return \emptyset

end if

return $path$

end if

for each n in neighbors of $curr$ **do**

if n in Vis **then**

continue

end if

$neis_in_path \leftarrow$ count of n 's neighbors in $path$

if $neis_in_path \leq 1$ **then**

$path \leftarrow path$ concatenated with $[n]$

$cost \leftarrow cost + C[n.x][n.y]$

$Q.push((cost, path))$

end if

end for

end while

Evaluation

Datasets

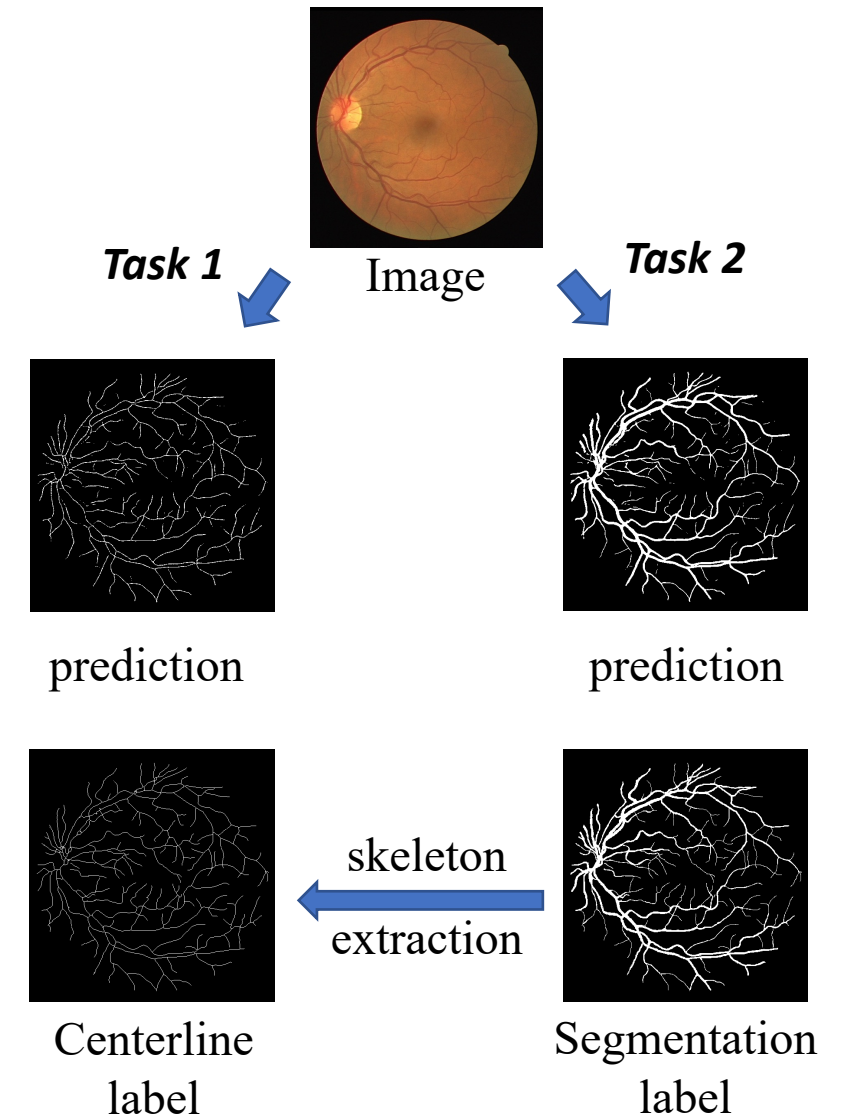
- Medical datasets: ***DRIVE, STARE and ISBI12***
- Satellite dataset: ***Massachusetts Roads***

Tasks

- ***Centerline extraction (Task 1)***
- ***Tubular structure segmentation (Task 2)***

Metrics

- ***Volumetric metrics:*** Dice, Accuracy, AUC, cIDice, etc.
- ***Topology-based metrics:*** β_0 error, β_1 error, χ error



Experimental Results

Centerline extraction

- *Graph Decoder during training enables the network to learn branch-level features, leading to enhanced performance in both volumetric and topological metrics.*
- *The combined use of **Graph Decoder** and **Morph Module** showcases the ability to preserve the crucial topological characteristics.*

Table 1: Centerline extraction performance on four public datasets based on UNet.

Dataset	Method	Volumetric metrics (\uparrow)			Topological metrics (\downarrow)		
		Dice	AUC	ACC	β_0 error	β_1 error	χ error
DRIVE	softDice [26]	0.7353 \pm 0.0127	0.9333 \pm 0.0089	0.9768 \pm 0.0013	2.169 \pm 0.112	1.590 \pm 0.107	2.537 \pm 0.139
	PointScatter [40]	0.7381 \pm 0.0133	0.9401 \pm 0.0078	0.9775 \pm 0.0013	3.259 \pm 0.153	2.080 \pm 0.120	3.500 \pm 0.176
	softDice [26] + Graph Decoder	0.7506 \pm 0.0127	0.9481 \pm 0.0082	0.9783 \pm 0.0012	1.552 \pm 0.094	1.382 \pm 0.106	1.899 \pm 0.125
	softDice [26] + Graph Decoder + Morph Module	0.7496 \pm 0.0118	/	0.9776 \pm 0.0012	0.555 \pm 0.038	1.074 \pm 0.073	0.893 \pm 0.061
ISBI12	softDice [26]	0.6428 \pm 0.0104	0.8937 \pm 0.0063	0.9737 \pm 0.0013	4.045 \pm 0.191	2.696 \pm 0.112	4.294 \pm 0.205
	Pointscatter [40]	0.6546 \pm 0.0089	0.9104 \pm 0.0057	0.9747 \pm 0.0013	6.398 \pm 0.277	3.156 \pm 0.124	6.548 \pm 0.290
	softDice [26] + Graph Decoder	0.6486 \pm 0.0095	0.9240 \pm 0.0061	0.9742 \pm 0.0012	4.013 \pm 0.179	2.732 \pm 0.110	4.249 \pm 0.193
	softDice [26] + Graph Decoder + Morph Module	0.6687 \pm 0.0092	/	0.9742 \pm 0.0014	0.665 \pm 0.049	1.207 \pm 0.070	0.858 \pm 0.059
STARE	softDice [26]	0.7119 \pm 0.0392	0.9290 \pm 0.0283	0.9889 \pm 0.0012	1.874 \pm 0.139	1.209 \pm 0.112	2.063 \pm 0.162
	Pointscatter [40]	0.7224 \pm 0.0414	0.9494 \pm 0.0179	0.9896 \pm 0.0012	2.080 \pm 0.149	1.365 \pm 0.116	2.213 \pm 0.166
	softDice [26] + Graph Decoder	0.7298 \pm 0.0428	0.9506 \pm 0.0208	0.9898 \pm 0.0011	1.467 \pm 0.113	1.074 \pm 0.104	1.654 \pm 0.132
	softDice [26] + Graph Decoder + Morph Module	0.7291 \pm 0.0387	/	0.9894 \pm 0.0011	0.482 \pm 0.042	0.799 \pm 0.077	0.653 \pm 0.059
MassRoad	softDice [26]	0.6339 \pm 0.0169	0.9718 \pm 0.0047	0.9942 \pm 0.0009	1.672 \pm 0.056	1.627 \pm 0.087	1.968 \pm 0.097
	Pointscatter [40]	0.6405 \pm 0.0149	0.9694 \pm 0.0042	0.9942 \pm 0.0009	3.333 \pm 0.124	1.553 \pm 0.086	3.429 \pm 0.149
	softDice [26] + Graph Decoder	0.6289 \pm 0.0175	0.9731 \pm 0.0045	0.9941 \pm 0.0009	1.933 \pm 0.065	1.729 \pm 0.088	2.229 \pm 0.105
	softDice [26] + Graph Decoder + Morph Module	0.6388 \pm 0.0168	/	0.9942 \pm 0.0009	0.620 \pm 0.021	1.355 \pm 0.083	1.122 \pm 0.075

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Experimental Results

Tubular structure segmentation

➤ *GraphMorph* achieves best results across all methods thanks to the utilization of branch-level features.

Table 3: Comparison with SOTA methods on the segmentation task. Best results are in bold; second-best are underlined. Our approach secures all leading scores and most secondary peaks.

Dataset	Backbone	Method	Volumetric metrics (\uparrow)			Distribution metrics		Topological metrics (\downarrow)		
			Dice	clDice	ACC	ARI(\uparrow)	VOI(\downarrow)	β_0 error	β_1 error	χ error
DRIVE	UNet	softDice 26	0.8148 \pm 0.0093	0.8128 \pm 0.0169	0.9535 \pm 0.0023	0.767 \pm 0.011	0.348 \pm 0.012	1.191 \pm 0.069	1.078 \pm 0.074	1.467 \pm 0.083
	UNet	clDice 37	0.8150 \pm 0.0078	<u>0.8322 \pm 0.0163</u>	0.9520 \pm 0.0021	0.765 \pm 0.009	0.357 \pm 0.012	0.910 \pm 0.056	0.998 \pm 0.070	1.181 \pm 0.071
	UNet	PointsScatter 40	0.8155 \pm 0.0081	0.8277 \pm 0.0179	0.9525 \pm 0.0020	0.766 \pm 0.009	0.353 \pm 0.010	1.360 \pm 0.080	1.276 \pm 0.083	1.663 \pm 0.094
	UNet	TopoLoss 141	<u>0.8187 \pm 0.0075</u>	0.8194 \pm 0.0160	<u>0.9540 \pm 0.0020</u>	<u>0.771 \pm 0.009</u>	0.345 \pm 0.010	0.821 \pm 0.050	0.997 \pm 0.072	1.100 \pm 0.067
	DSCNet 33	softDice	0.8118 \pm 0.0083	0.8107 \pm 0.0172	0.9527 \pm 0.0021	0.763 \pm 0.010	0.352 \pm 0.011	1.267 \pm 0.075	1.110 \pm 0.076	1.550 \pm 0.087
	TransUNet 41	softDice	0.8153 \pm 0.0094	0.8139 \pm 0.0182	0.9538 \pm 0.0020	0.768 \pm 0.010	<u>0.344 \pm 0.009</u>	1.125 \pm 0.066	1.184 \pm 0.082	1.420 \pm 0.082
	DC-UNet 221	softDice	0.8086 \pm 0.0103	0.8018 \pm 0.0163	0.9526 \pm 0.0024	0.760 \pm 0.012	0.351 \pm 0.011	1.227 \pm 0.074	1.061 \pm 0.074	1.499 \pm 0.087
	UNet	softDice+Ours	0.8238 \pm 0.0091	0.8278 \pm 0.0166	0.9557 \pm 0.0023	0.778 \pm 0.011	0.336 \pm 0.012	<u>0.692 \pm 0.047</u>	<u>0.932 \pm 0.068</u>	<u>0.951 \pm 0.062</u>
	UNet	clDice+Ours	0.8168 \pm 0.0076	0.8467 \pm 0.0146	0.9520 \pm 0.0021	0.767 \pm 0.009	0.357 \pm 0.012	0.619 \pm 0.043	0.924 \pm 0.065	0.857 \pm 0.056
	ISB112	UNet	softDice 26	0.8043 \pm 0.0092	0.9295 \pm 0.0078	0.9146 \pm 0.0060	0.653 \pm 0.018	0.785 \pm 0.040	0.569 \pm 0.046	0.616 \pm 0.047
UNet		clDice 37	0.8103 \pm 0.0099	0.9353 \pm 0.0084	0.9163 \pm 0.0064	0.660 \pm 0.020	0.775 \pm 0.042	0.422 \pm 0.038	0.563 \pm 0.045	0.576 \pm 0.043
UNet		PointsScatter 40	0.8192 \pm 0.0101	0.9406 \pm 0.0077	0.9189 \pm 0.0063	0.672 \pm 0.020	0.758 \pm 0.042	0.456 \pm 0.041	0.568 \pm 0.046	0.587 \pm 0.047
UNet		TopoLoss 141	0.8104 \pm 0.0090	0.9324 \pm 0.0074	0.9167 \pm 0.0058	0.661 \pm 0.017	0.773 \pm 0.039	0.516 \pm 0.041	0.642 \pm 0.052	0.669 \pm 0.049
DSCNet 33		softDice	0.8152 \pm 0.0087	0.9366 \pm 0.0078	0.9191 \pm 0.0054	0.669 \pm 0.016	0.757 \pm 0.037	0.450 \pm 0.040	0.567 \pm 0.045	0.581 \pm 0.044
TransUNet 41		softDice	0.8056 \pm 0.0080	0.9289 \pm 0.0075	0.9148 \pm 0.0055	0.654 \pm 0.016	0.784 \pm 0.037	0.636 \pm 0.049	0.576 \pm 0.047	0.757 \pm 0.053
DC-UNet 221		softDice	0.8150 \pm 0.0089	0.9366 \pm 0.0084	0.9196 \pm 0.0063	0.671 \pm 0.019	0.753 \pm 0.043	0.511 \pm 0.043	0.586 \pm 0.046	0.652 \pm 0.047
UNet		softDice+Ours	<u>0.8216 \pm 0.0091</u>	<u>0.9449 \pm 0.0069</u>	<u>0.9211 \pm 0.0057</u>	<u>0.678 \pm 0.018</u>	<u>0.745 \pm 0.039</u>	<u>0.361 \pm 0.034</u>	0.520 \pm 0.043	<u>0.488 \pm 0.041</u>
UNet		clDice+Ours	0.8223 \pm 0.0086	0.9459 \pm 0.0066	0.9213 \pm 0.0056	0.679 \pm 0.017	0.744 \pm 0.038	0.353 \pm 0.034	<u>0.539 \pm 0.043</u>	0.482 \pm 0.040
STARE		UNet	softDice 26	0.8170 \pm 0.0402	0.8526 \pm 0.0306	0.9749 \pm 0.0044	0.781 \pm 0.042	0.276 \pm 0.033	0.786 \pm 0.064	0.653 \pm 0.072
	UNet	clDice 37	0.8212 \pm 0.0386	0.8579 \pm 0.0319	0.9752 \pm 0.0041	0.785 \pm 0.040	0.276 \pm 0.032	0.571 \pm 0.049	0.629 \pm 0.069	0.743 \pm 0.065
	UNet	PointsScatter 40	0.8171 \pm 0.0395	0.8533 \pm 0.0331	0.9743 \pm 0.0041	0.780 \pm 0.041	0.285 \pm 0.031	0.844 \pm 0.070	0.781 \pm 0.080	0.997 \pm 0.086
	UNet	TopoLoss 141	0.8175 \pm 0.0449	0.8506 \pm 0.0339	0.9750 \pm 0.0045	0.781 \pm 0.047	0.276 \pm 0.033	0.659 \pm 0.056	0.615 \pm 0.068	0.806 \pm 0.069
	DSCNet 33	softDice	0.7988 \pm 0.0420	0.8341 \pm 0.0348	0.9723 \pm 0.0052	0.759 \pm 0.045	0.296 \pm 0.037	0.823 \pm 0.068	0.707 \pm 0.072	0.988 \pm 0.080
	TransUNet 41	softDice	0.8046 \pm 0.0474	0.8428 \pm 0.0370	0.9737 \pm 0.0047	0.767 \pm 0.049	0.284 \pm 0.034	0.728 \pm 0.061	0.723 \pm 0.076	0.884 \pm 0.078
	DC-UNet 221	softDice	0.7936 \pm 0.0547	0.8300 \pm 0.0426	0.9728 \pm 0.0052	0.755 \pm 0.057	0.288 \pm 0.034	0.834 \pm 0.071	0.721 \pm 0.075	0.975 \pm 0.082
	UNet	softDice+Ours	<u>0.8210 \pm 0.0464</u>	<u>0.8578 \pm 0.0372</u>	<u>0.9756 \pm 0.0045</u>	<u>0.786 \pm 0.049</u>	<u>0.271 \pm 0.033</u>	<u>0.545 \pm 0.046</u>	0.618 \pm 0.067	0.691 \pm 0.059
	UNet	clDice+Ours	0.8283 \pm 0.0371	0.8747 \pm 0.0284	0.9757 \pm 0.0040	0.792 \pm 0.039	<u>0.274 \pm 0.032</u>	0.450 \pm 0.042	0.582 \pm 0.065	0.598 \pm 0.055
	MassRoad	UNet	softDice 26	0.7808 \pm 0.0146	0.8768 \pm 0.0159	0.9780 \pm 0.0036	0.750 \pm 0.017	0.239 \pm 0.033	0.479 \pm 0.020	0.798 \pm 0.076
UNet		clDice 37	0.7788 \pm 0.0143	0.8773 \pm 0.0156	0.9775 \pm 0.0037	0.747 \pm 0.016	0.244 \pm 0.033	0.512 \pm 0.022	0.964 \pm 0.090	0.962 \pm 0.086
UNet		PointsScatter 40	0.7787 \pm 0.0142	0.8750 \pm 0.0156	0.9778 \pm 0.0035	0.748 \pm 0.016	0.242 \pm 0.033	0.620 \pm 0.027	0.800 \pm 0.076	0.908 \pm 0.074
UNet		TopoLoss 141	0.7797 \pm 0.0150	0.8758 \pm 0.0164	0.9781 \pm 0.0035	0.749 \pm 0.017	0.238 \pm 0.032	0.439 \pm 0.018	0.780 \pm 0.076	0.727 \pm 0.071
TransUNet 41		softDice	0.7620 \pm 0.0169	0.8588 \pm 0.0182	0.9766 \pm 0.0038	0.730 \pm 0.019	0.248 \pm 0.034	0.734 \pm 0.027	0.933 \pm 0.079	1.017 \pm 0.075
LinkNet34 31		softDice	0.7752 \pm 0.0151	0.8747 \pm 0.0161	0.9775 \pm 0.0036	0.744 \pm 0.017	0.243 \pm 0.033	0.489 \pm 0.021	0.773 \pm 0.076	0.771 \pm 0.072
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UNet		softDice+Ours	0.7849 \pm 0.0139	<u>0.8816 \pm 0.0151</u>	0.9783 \pm 0.0035	0.754 \pm 0.016	0.237 \pm 0.033	0.386 \pm 0.016	0.754 \pm 0.076	0.672 \pm 0.070
UNet		clDice+Ours	0.7851 \pm 0.0137	0.8844 \pm 0.0148	0.9779 \pm 0.0036	0.754 \pm 0.016	0.241 \pm 0.033	0.393 \pm 0.018	0.879 \pm 0.085	0.784 \pm 0.082

Experimental Results

Visualization

➤ *GraphMorph reduces false negatives, false positives and topological errors on both tasks.*

