



# An Expectation-Maximization Algorithm for Training Clean Diffusion Models from Corrupted Observations

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#### **Diffusion Models**



#### **Clean Dataset for Training:** FFHQ

#### What about few clean images for training?

#### **Corrupted Observations are Sufficient**



Clean Image

An example in super-resolution fluorescent microscopy

## EMDiffusion: Learn Generative Image Priors from Corrupted Observations



#### Initialization: Training Diffusion with Limited Clean Data



(e) 50 clean images for training the initial diffusion model

# E-step: Diffusion Posterior Sampling

#### $p(x|y) \propto p(y|x) \ p(x)$



**E-step:** Reconstruct images from corrupted observations using current generative image prior

[1] Diffusion Posterior Sampling for General Noisy Inverse Problems. Hyungjin Chung, et al. ICLR 2023.

# M-step: Updating Diffusion Model's Weights

## $p(x|y) \propto p(y|x) p(x)$



**M-step:** Refining generative image prior using reconstructions

## EMDiffusion: Learn Generative Image Priors from Corrupted Observations



#### **Progressive Learning Process**

## $p(x|y) \propto p(y|x)$ p(x)



## Learned Diffusion Model



Masked Observations

**Generated Samples** 

#### Learned Diffusion Model



**Generated Samples** 

#### Learned Diffusion Model

Diffusion



**Noisy Observations** 



Generated Samples

#### Quantitative Comparison

	<b>CIFAR10-Inpainting</b>			<b>CIFAR10-Denoising</b>			<b>CelebA-Deblurring</b>		
Method	<b>PSNR</b> ↑	LPIPS↓	FID↓	<b>PSNR</b> ↑	LPIPS↓	FID↓	<b>PSNR</b> ↑	LPIPS↓	FID↓
Observations	13.49	0.295	234.47	18.05	0.047	132.59	22.47	0.365	72.83
DPS w/ clean prior	25.44	0.008	7.08	25.91	0.010	7.08	29.05	0.013	10.24
Noise2Self [3]	-	-	-	21.32	0.227	<u>92.06</u>	-	-	-
SURE-Score [1]	15.75	0.182	220.01	22.42	0.138	132.61	22.07	0.383	191.96
AmbientDiffusion [14]	<u>20.57</u>	0.027	28.88	21.37	<u>0.033</u>	114.13	21.16	<u>0.158</u>	83.99
Ours	24.70	0.009	21.08	23.16	0.022	86.47	23.74	0.103	<u>91.89</u>

# Initialization and Annealing of Diffusion Prior

32 24 Inpainting 30 Denoising 22 28 Deblurring 20 26 PSNR UNSA 54 18 22 16 20 14 18 12 16 10 500 ID 100 ID 50 ID 10 ID 50 OOD Data

*ID: In-distribution clean images OOD: Out-of-distribution clean images* 



 $p(x|y) \propto p(y|x) p^{\lambda}(x)$ 

Scaling factor controls the strength of prior

#### **Reset of Diffusion Model Weights**



## Conclusion



EMDiffusion: Learn from Corruption

Without large-scale clean images, Diffusion models can still be **trained** 

- EM-Diffusion: E-step (DPS) + M-step (Diffusion Model Training);
- Training data: large-scale corrupted observations
- Future work: eliminate the initialization dependency on clean data.

 $p(x|y) \propto p(y|x) p(x)$