Changing the Training Data Distribution to Reduce Simplicity Bias Improves In-distribution Generalization

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- However, some global minima generalize better than others!

batch size	train accuracy	test accuracy	train loss
1	100.0 (100.0 - 100.0)	77.2 (77.7 - 76.4)	$\begin{array}{c} 0.00 & (0.00 - 0.00) \\ 0.00 & (0.00 - 0.00) \\ 0.00 & (0.00 - 0.00) \\ 0.00 & (0.02 - 0.00) \end{array}$
8	100.0 (100.0 - 100.0)	76.5 (76.7 - 75.9)	
256	100.0 (100.0 - 100.0)	63.2 (63.4 - 61.3)	
2048	100.0 (100.0 - 99.8)	60.2 (60.6 - 58.6)	

Table 1. Train and test accuracy on CIFAR10, taken from [2].

[1] Belkin, Mikhail, et al. "Reconciling modern machine-learning practice and the classical bias–variance trade-off." Proceedings of the National Academy of Sciences 116.32 (2019): 15849-15854.

[2] https://www.dropbox.com/scl/fi/7lk8jkchj82oe7smh7b4w/Hossein_Mobahi_SAM_CSML_Talk.pdf?rlkey=1mc56v58cvcy480bflexfuioq&e=1&dl=0

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Improving ID generalization via data modification

Can we improve the ID performance by changing the data distribution of a clean dataset?

We do not assume any redundant, noisy, or harmful examples in the data.

Thus, we do not want to filter such examples!

The superior ID generalization of SAM

• Sharpness-aware minimization (SAM) [3] minimizes both loss and sharpness.

$$L_{\text{SAM}}(w) = \max_{\|\epsilon\|_2 \le p} L(w+\epsilon) = \underbrace{L(w)}_{\text{loss}} + \underbrace{[\max_{\|\epsilon\|_2 \le p} L(w+\epsilon) - L(w)]}_{\text{sharpness}}$$

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• SAM finds flatter local minima that generalize better than SGD!



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Can we get insights from SAM to change the data distribution to improve ID generalization?





Figure 1. (left) Sharp minima of SGD (right) wide minima of SAM [3].

[3] Foret, Pierre, et al. "Sharpness-aware minimization for efficiently improving generalization." arXiv preprint arXiv:2010.01412 (2020).

SAM learns features more evenly than GD

We theoretically prove that SAM is less reliant on simplicity bias compared to GD.

[Informal] Consider a two-layer nonlinear CNNs, and a data with a fast-learnable and a slow-learnable feature. Then, starting from the same initialization, SAM learns the fast-learnable and slow-learnable features at a more uniform speed than GD, i.e., for every iteration $t \in [1, T_0]$:

$$\mathrm{SAM}_{fast}^{(t)} - \mathrm{SAM}_{slow}^{(t)} < \mathrm{GD}_{fast}^{(t)} - \mathrm{GD}_{slow}^{(t)}$$

Feature learning gap in SAM

Feature learning gap in GD

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Figure 2. CIFAR10 images

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- Step 2: Upsample examples that are not in the cluster of points containing fast-learnable features.
- Step 3: Restart training on the modified data distribution.



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Experimental results

Our method improves the performance of both SGD and SAM, achieving SOTA results in a variety of settings.



Figure 3. Test classification errors of ResNet18 on different datasets.

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Figure 4. Test classification errors of different architectures on CIFAR10.



Thank you! Please come visit our poster at Session 5: Fri 13 Dec 11 AM - 2 PM PST

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