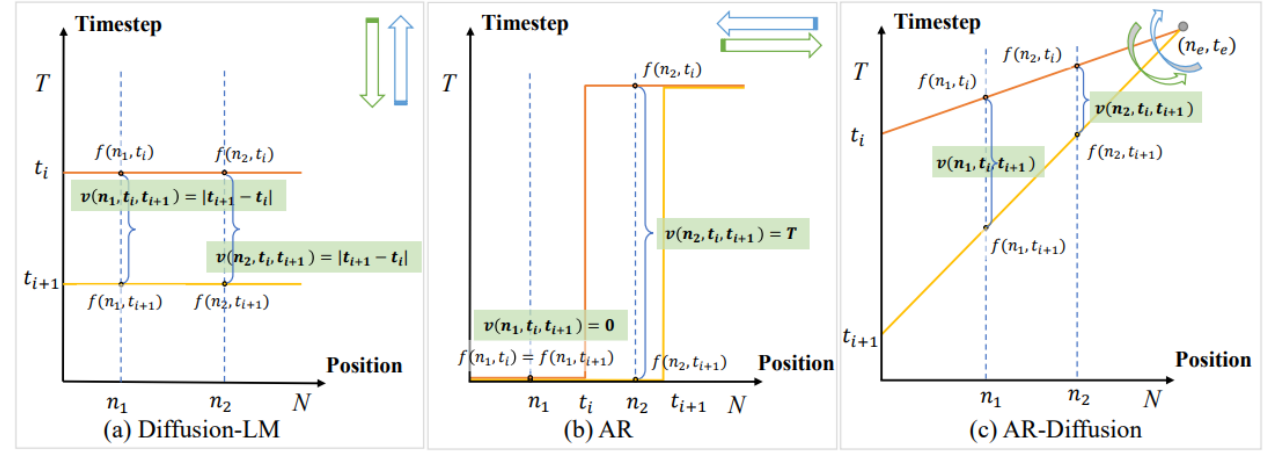
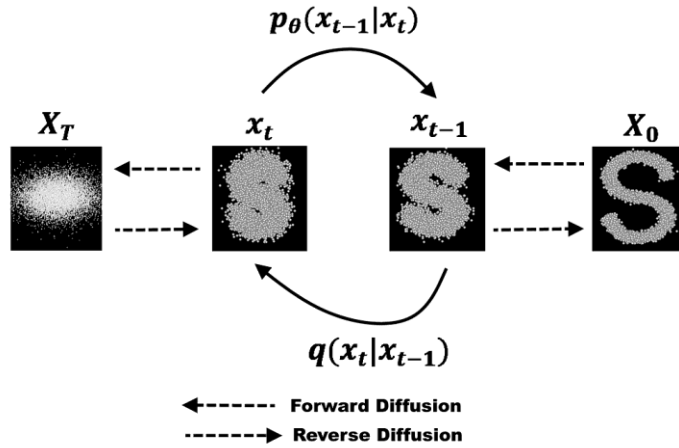


AR-Diffusion: Auto-Regressive Diffusion Model for Text Generation

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Diffusion Models for Language Generation



Blue arrow: Forward Diffusion Process
 Green arrow: Reverse Diffusion Process
 Orange line: Token-Level Diffusion Timestep Function

12.0
14.0
16.0
18.0
20.0

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How AR-Diffusion works?

Algorithm 1 Training Process of AR-DIFFUSION.

Input: Dataset $\{(\mathbf{x}, \mathbf{y})\}$, maximum timestep number T and maximum target length N .

Output: Optimized model parameters θ .

- 1: Define an anchor point (n_e, t_e) ⁵.
- 2: **repeat**
- 3: Sample (\mathbf{x}, \mathbf{y}) from the dataset and embed \mathbf{y} into \mathbf{z}_0 .
- 4: Sample a sentence-level timestep t from the interval $[0, N + T]$, then the start point is determined by the following equation:

$$(n_s, t_s) = (\text{clip}(N - t, 0, N), \text{clip}(t - N, 0, T)) \quad (6)$$

- 5: Use the point-slope linear function to determine the token-level timestep $f(n, t)$ in position n :

$$f(n, t) = \text{clip}\left(\frac{t_e - t_s}{n_e - n_s}(n - n_s) + t_s, 0, T\right) \quad (7)$$

- 6: Sample $\mathbf{z}_{f(n,t)}^n$ for each n in different positions with Gaussian reparameterization.
- 7: According to equation (3) and equation (9), employ gradient descent to optimize the objective:

$$\min_{\theta} \left[-\log p_{\theta}(\mathbf{y} \mid \mathbf{z}_0; \mathbf{x}) + \sum_{n=1}^N \|\mathbf{g}_{\theta}(\mathbf{z}_{f(n,t)}^n, f(n, t); \mathbf{x}) - \mathbf{z}_0\|^2 \right] \quad (8)$$

- 8: **until** converged
-

Algorithm 2 Inference Process of AR-DIFFUSION with the Skipping Mechanism.

Input: Source condition \mathbf{x} , number of decoding steps M and model parameters θ .

Output: Predicted target embedding $\hat{\mathbf{y}}$.

- 1: Define an anchor point (n_e, t_e) .
- 2: Uniformly select a decreasing sequence of timesteps $\{t_i\}_{i=0}^M$ ranging from $T + N$ to 0.
- 3: Sample $\mathbf{z}_{t_0} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$.
- 4: **for** $i = 0$ to $M - 1$ **do**
- 5: Calculate the start point (n_s, t_s) using equation (6).
- 6: Based on the current sentence-level inference steps t_i and the next one t_{i+1} , assign token-level timesteps $f(n, t_i)$ and $f(n, t_{i+1})$ to token in position n using equation (7).
- 7: Reverse sample $\mathbf{z}_{t_{i+1}} = (\mathbf{z}_{f(1,t_{i+1})}^1, \mathbf{z}_{f(2,t_{i+1})}^2, \dots, \mathbf{z}_{f(N,t_{i+1})}^N)$ from $p_{\theta}(\mathbf{z}_{t_{i+1}} \mid \mathbf{z}_{t_i}; \mathbf{x})$ with the following formulas:

$$p_{\theta}(\mathbf{z}_{t_{i+1}} \mid \mathbf{z}_{t_i}; \mathbf{x}) = \prod_{n=1}^N p_{\theta}(\mathbf{z}_{f(n,t_{i+1})}^n \mid \mathbf{z}_{f(n,t_i)}^n; \mathbf{x}) \quad (10)$$

$$p_{\theta}(\mathbf{z}_{f(n,t_{i+1})}^n \mid \mathbf{z}_{f(n,t_i)}^n; \mathbf{x}) \sim \mathcal{N}(\mathbf{z}_{f(n,t_{i+1})}^n; \lambda \mathbf{z}_{f(n,t_i)}^n + \mu \mathbf{g}_{\theta}(\mathbf{z}_{f(n,t_i)}^n, f(n, t_i); \mathbf{x}), \sigma \mathbf{I}) \quad (11)$$

- 8: **end for**
 - 9: Map \mathbf{z}_{t_M} to the nearest embedding $\hat{\mathbf{y}}$.
-

Experimental Results

Table 1: Results on XSUM test set. The results of NAR and Semi-NAR are from Qi et al. [2021], and the results of AR are from GLGE [Liu et al., 2021].

Methods	Pattern	ROUGE-1	ROUGE-2	ROUGE-L
NAT [Gu et al., 2017]	NAR	24.0	3.9	20.3
iNAT [Lee et al., 2018]		24.0	4.0	20.4
CMLM [Ghazvininejad et al., 2019]		23.8	3.6	20.2
LevT [Gu et al., 2019]		24.8	4.2	20.9
InsT [Stern et al., 2019]	Semi-NAR	17.7	5.2	16.1
iNAT [Lee et al., 2018]		27.0	6.9	22.4
CMLM [Ghazvininejad et al., 2019]		29.1	7.7	23.0
LevT [Gu et al., 2019]		25.3	7.4	21.5
LSTM [Greff et al., 2017]	AR ¹⁰	25.1	6.9	19.9
Transformer [Vaswani et al., 2017]		30.5	<u>10.4</u>	24.2
GENIE [Lin et al., 2023] ($k = 50$)	Diffusion	29.3	8.3	21.9
AR-DIFFUSION ($k = 50$)		<u>31.7</u>	10.1	<u>24.7</u>
AR-DIFFUSION ($k = 500$)		32.2	10.6	25.2

Table 2: Results on CNN/DAILYMAIL test set. The results of AR are from GLGE Liu et al. [2021].

Methods	Pattern	ROUGE-1	ROUGE-2	ROUGE-L
LSTM [Greff et al., 2017]	AR	37.3	15.7	34.4
Transformer [Vaswani et al., 2017]		39.5	<u>16.7</u>	36.7
GENIE [Lin et al., 2023] ($k = 50$)	Diffusion	34.4	12.8	32.1
AR-DIFFUSION ($k = 50$)		<u>39.6</u>	16.3	<u>37.1</u>
AR-DIFFUSION ($k = 500$)		40.2	17.1	37.7

Table 3: Results on IWSLT14 DE→EN test set following the setting of SEQDIFFUSEQ. “NFE” indicates the Number of Function Evaluations [Ye et al., 2023].

Methods	Pattern	BLEU	Steps	NFE (Steps $\times k$)
Transformer [Vaswani et al., 2017]	AR	34.74	-	-
CNAT [Bao et al., 2021]	NAR	29.81	-	-
SeqDiffuSeq [Yuan et al., 2022] ($k = 1$)	Diffusion	29.83	2,000	2,000 ($2,000 \times 1$)
AR-DIFFUSION ($k = 1$)		30.19	20	20 (20×1)
GENIE [Lin et al., 2023] ($k = 50$)	Diffusion	30.08	20	1,000 (20×50)
AR-DIFFUSION ($k = 50$)		<u>34.95</u>	20	1,000 (20×50)
AR-DIFFUSION ($k = 500$)		35.62	20	10,000 (20×500)

Table 4: Results on COMMONGEN dev set. Results of NAR and AR are from Lin et al. [2020].

Methods	Pattern	ROUGE-2/L		BLEU-3/4		METEOR	SPICE
bRNN-CopyNet [Gu et al., 2016]	AR	9.23	30.57	13.60	7.80	17.40	16.90
Trans-CopyNet [Lin et al., 2020]		11.08	32.57	17.20	10.60	18.80	18.00
MeanPooling-CopyNet [Lin et al., 2020]		11.36	34.63	14.80	8.90	19.20	20.20
LevT [Gu et al., 2019]	NAR	12.22	<u>35.42</u>	<u>23.10</u>	<u>15.00</u>	22.10	21.40
ConstLeven [Susanto et al., 2020]		<u>13.47</u>	35.19	21.30	12.30	25.00	<u>23.20</u>
GENIE [Lin et al., 2023] ($k = 50$)	Diffusion	12.89	35.21	22.00	13.30	<u>24.30</u>	23.00
AR-DIFFUSION ($k = 50$)		13.93	37.36	25.60	16.40	25.00	24.20

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