

Learning non-Markovian Decision-Making from State-only Sequences

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Thirty-seventh Conference on Neural Information Processing Systems (NeurIPS-2023)

Introduction

- The expressivity of Markov reward has been proved to be limited.
- We develop a Maximum Likelihood Estimation for generative modeling of *non-Markovian Decision Process (nMDP)*, where TD-learning-based imitation is unreliable.
- The novel EM-like algorithm recover the unobserved decisions and underlying value functions from pure observations *without action labels*.



Graphical model of policy and transition in standard MDP and $\mathbf{n}\mathbf{M}\mathbf{D}\mathbf{P}$

Abel, David, et al. "On the expressivity of markov reward." Advances in Neural Information Processing Systems 34 (2021): 7799-7812.

Modeling and Learning

• Trajectory joint distribution:

$$p_{\theta}(\zeta) = p(s_0) \prod_{t=0}^{T-1} p_{\alpha}(a_t | s_{0:t}) p_{\beta}(s_{t+1} | s_t, a_t)$$

• Transition as single-mode Gaussian

$$\mathcal{N}(g_{\beta}(s_t, a_t), \sigma^2)$$

- Policy as multi-mode Energy-Based Model (EBM) $p_{\alpha}(a_t|s_{0:t}) = \frac{1}{Z(\alpha, s_{0:t})} \exp\left(f_{\alpha}(a_t; s_{0:t})\right)$
- MLE learning, the gradient is:

$$\nabla_{\theta} \log p_{\theta}(\xi) = \mathbb{E}_{p_{\theta}(A|S)} \left[\sum_{t=0}^{T-1} \left(\underbrace{\nabla_{\alpha} \log p_{\alpha}(a_t|s_{0:t})}_{\text{policy/prior}}, \underbrace{\nabla_{\beta} \log p_{\beta}(s_{t+1}|s_t, a_t)}_{\text{transition}} \right) \right]$$

Sampling

• Policy term involves both posterior and prior samples:

$$\delta_{\alpha,t}(S) = \mathbb{E}_{p_{\theta}(A|S)} \left[\nabla_{\alpha} \log p_{\alpha}(a_t|s_{0:t}) \right]$$
$$= \mathbb{E}_{p_{\theta}(A|S)} \left[\nabla_{\alpha} f_{\alpha}(a_t;s_{0:t}) \right] - \mathbb{E}_{p_{\alpha}(a_t|s_{0:t})} \left[\nabla_{\alpha} f_{\alpha}(a_t;s_{0:t}) \right]$$

• Short run Langevin MCMC for prior samples:

$$a_{t,k+1} = a_{t,k} + s\nabla_{a_{t,k}} f_\alpha(a_{t,k}; s_{0:t}) + \sqrt{2s}\epsilon_k$$

• Importance sampling for posterior samples:

$$p_{\theta}(a_t|s_{0:t+1}) = \frac{p_{\beta}(s_{t+1}|s_t, a_t)}{\mathbb{E}_{p_{\alpha}(a_t|s_{0:t})} \left[p_{\beta}(s_{t+1}|s_t, a_t) \right]} p_{\alpha}(a_t|s_{0:t})$$

Theoretical Analysis

- We construct a sequential decision-making problem, whose objective yields the same optimal policy as MLE.
- We witness the automatic emergence of the entire family of maximum (inverse) RL.
- We derive the posterior probability of action sequences given any goal state, involving the intermediate transitions.

Decision-making as inference: policy as prior, planning as inference.

Experiments: Curve Planning

• Policy of cubic curve planning is necessarily non-Markovian, since the historical states are needed to estimate the higher-order derivatives.



Experiments: MuJoCo

- Our model demonstrates steeper learning curves than state-only baselines.
- Our model matches or surpasses the performance of action-label baselines.

