

# Can Adversarial Training Be Manipulated By Non-Robust Features?

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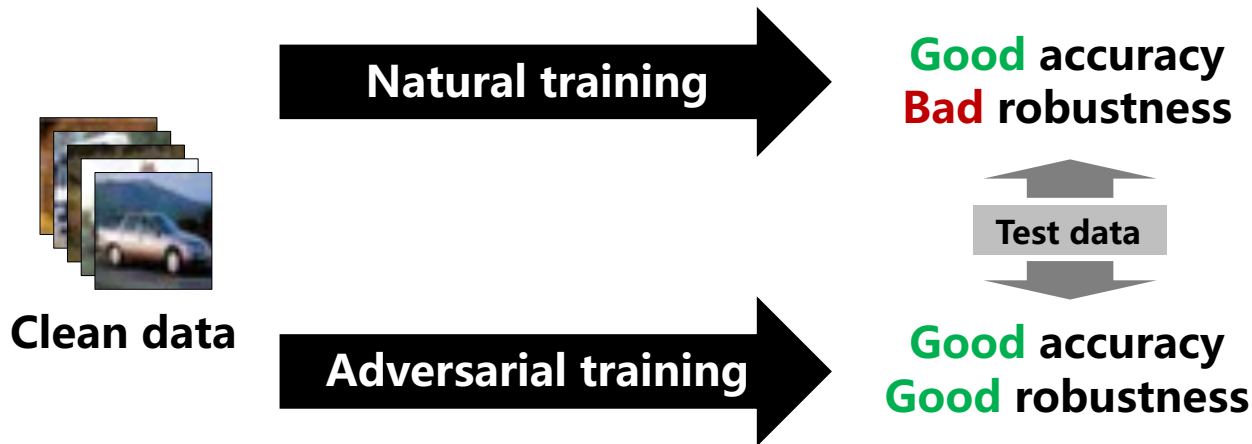
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# Adversarial Training

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- Adversarial training

- Improving test robustness by minimizing the adversarial risk



# Our Contribution

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- ❑ We introduce a novel threat model called **stability attack**
  - aims to degrade the test robustness of adversarially trained models
  - in short, aims to hinder robust availability



# Our Contribution

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- ❑ We introduce a novel threat model called **stability attack**,
  - which aims to degrade test robustness of adversarially trained models
  - in short, hinder robust availability
  
- ❑ Both theoretical and empirical evidences show that **adversarial training may fail to provide test robustness**

# Theoretical Analysis

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**Theorem 1** (Adversarial perturbation is harmless). *Assume that the adversarial perturbation in the training data  $\mathcal{T}_{adv}$  (10) is moderate such that  $\eta/2 \leq \epsilon < 1/2$ . Then, the optimal linear  $\ell_\infty$ -robust classifier obtained by minimizing the adversarial risk on  $\mathcal{T}_{adv}$  with a defense budget  $\epsilon$  is equivalent to the robust classifier (9).*

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**Theorem 2** (Hypocritical perturbation is harmful). *The optimal linear  $\ell_\infty$ -robust classifier obtained by minimizing the adversarial risk on the perturbed data  $\mathcal{T}_{hyp}$  (11) with a defense budget  $\epsilon$  is equivalent to the natural classifier (8).*

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**Theorem 3** ( $\epsilon + \eta$  is necessary). *The optimal linear  $\ell_\infty$ -robust classifier obtained by minimizing the adversarial risk on the perturbed data  $\mathcal{T}_{hyp}$  (11) with a defense budget  $\epsilon + \eta$  is equivalent to the robust classifier (9). Moreover, any defense budget lower than  $\epsilon + \eta$  will yield classifiers that still rely on all the non-robust features.*

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**Theorem 4** (General case). *For any data distribution and any adversary with an attack budget  $\epsilon$ , training models to minimize the adversarial risk with a defense budget  $2\epsilon$  on the perturbed data is sufficient to ensure  $\epsilon$ -robustness.*

# Empirical Evidence

- ❑ Stability attacks are harmful to conventional adversarial training
- ❑ Enlarging the defense budget is essential for hypocritical perturbations

Table 2: Test robustness (%) of PGD-AT using a defense budget  $\epsilon_d = 8/255$  on CIFAR-10.

Attack	Natural	FGSM	PGD-20	PGD-100	CW $_{\infty}$	AutoAttack
None (clean)	82.17	56.63	50.63	50.35	49.37	46.99
DeepConfuse [16]	81.25	54.14	48.25	48.02	47.34	44.79
Unlearnable Examples [28]	83.67	57.51	50.74	50.31	49.81	47.25
NTGA [81]	82.99	55.71	49.17	48.82	47.96	45.36
Adversarial Poisoning [18]	<b>77.35</b>	53.93	49.95	49.76	48.35	46.13
Hypocritical Perturbation (ours)	88.07	<b>47.93</b>	<b>37.61</b>	<b>36.96</b>	<b>38.58</b>	<b>35.44</b>

# Summary

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Thanks !