Implicit Gradient Transport NeurIPS 2019 in Vancouver, Canada

Problem

- We're interested in online stochastic optimization.
- Gradient and accelerated methods do not converge due to stochastic gradients.
- SAG & co. are convergent, but not suited for the online setting.
- Can we design a simple method that converges for this setting ?

$\theta_{t+1} = \theta_t - \eta g_t$ $g_t = \nabla_{\theta_t} \mathscr{L}(\theta_t)$

Method

- Yes!
- **Big Idea** Transport the *gradient information* from one parameter iterate to another.
- **Concretely** Compute gradient at a shifted point, and average it with previous gradient estimate.
- You get a variance-reduced stochastic gradient, readily pluggable into any gradient method.
 (e.g. Heavyball, Adam)





- rate of $\mathcal{O}(1/t)$.
- the accelerated rate $\mathcal{O}(\left(\frac{\sqrt{\kappa}-1}{\sqrt{\kappa}+1}\right)^t)$.
- **Caveat** Those results are only proved for quadratic $\mathscr{L}(\theta_t)$.

Theory

Theorem 1 Plugged into SGD, the IGT gradient estimator converges at a

Theorem 2 Plugged into Heavyball, the IGT gradient estimator achieves

Experiments



Thank You

Reducing the variance in online optimization by transporting past gradients.

Learn more at bit.ly/31ySnEC or talk to us at Poster #2887, Tuesday 5:30pm.







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