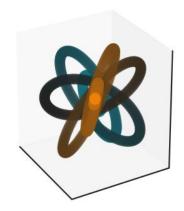
Legendre Memory Units (LMUs)



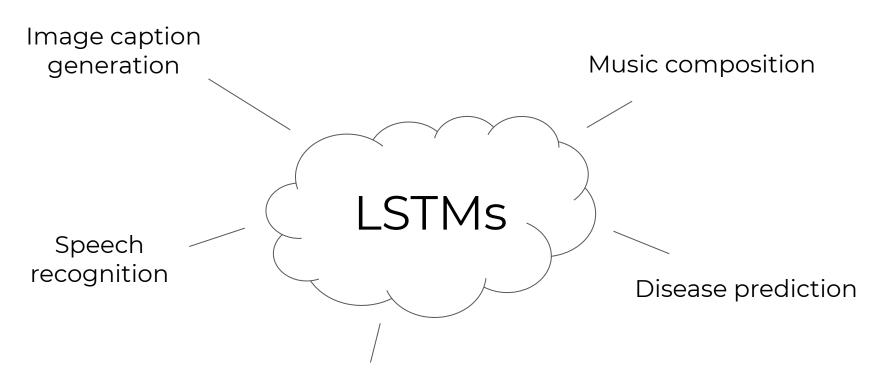
Continuous-Time Representation in Recurrent Neural Networks

Aaron Voelker, Ivana Kajić, Chris Eliasmith

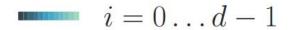


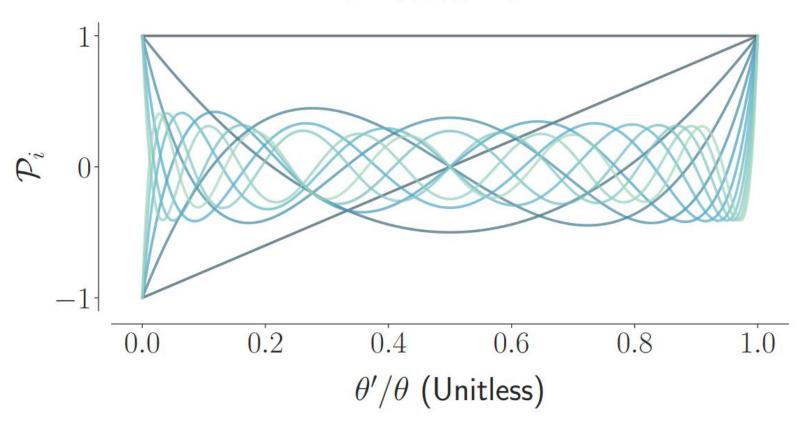


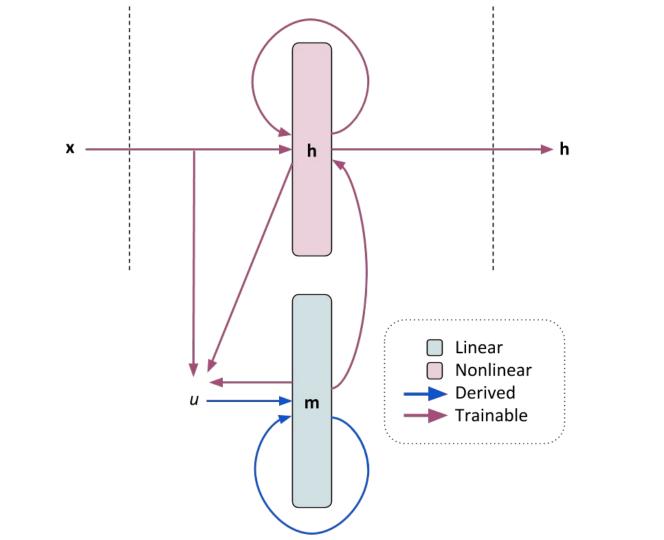


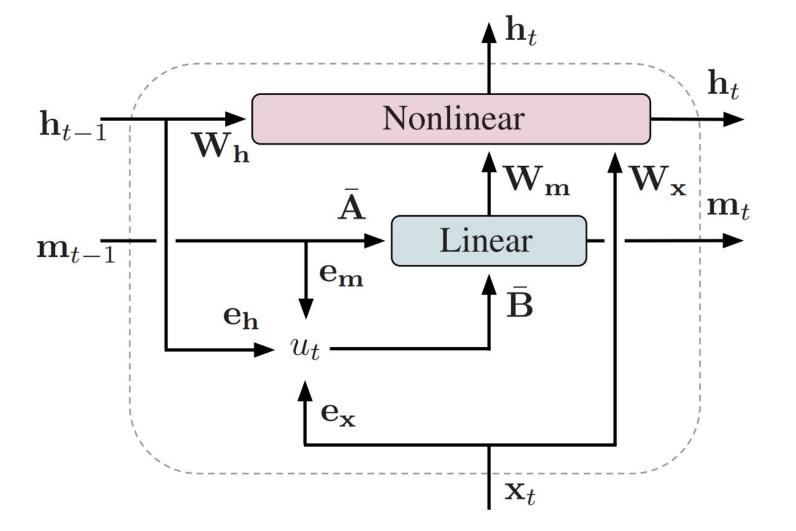


Machine translation





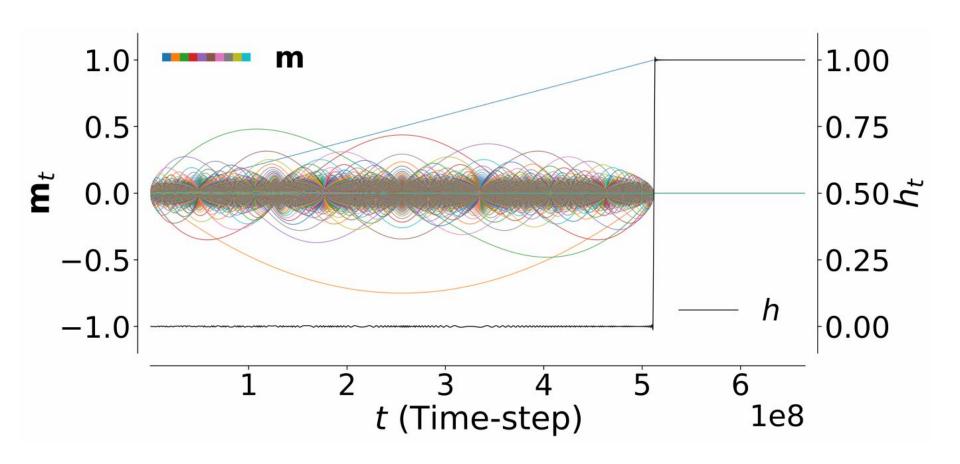




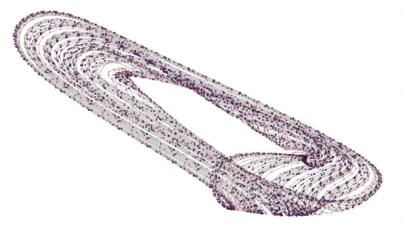
-	Model	Validation	Test	
-	RNN-orth	88.70	89.26	
	RNN-id	85.98	86.13	
	LSTM	90.01	89.86	
	LSTM-chrono	88.10	88.43	
	GRU	92.16	92.39	
	JANET	92.50	91.94	
	SRU	92.79	92.49	
	GORU	86.90	87.00	
	NRU	95.46	95.38	
	Phased LSTM	88.76	89.61	
	LMU	96.97	97.15	
	FF-baseline	92.37	92.65	Extended from Chandar et al. (2019)

Memory Capacity of Recurrent Architectures 10^{-1} LMU-0 (T=100) LMU-0 (T=1000) 10^{-2} LMU-0 (T=10000) LMU-0 (T=100000) 10^{-3} LSTM (T=25) Test MSE 10⁻⁴ LSTM (T=100) LSTM (T=400) LSTM (T=1600) 10^{-6} 10^{-7} 10^{-8} 10⁰ 10^{2} 10^{3} 10^{5} 10^{1} 10^{4} Delay Length (# Time-steps)

Scalable in Time

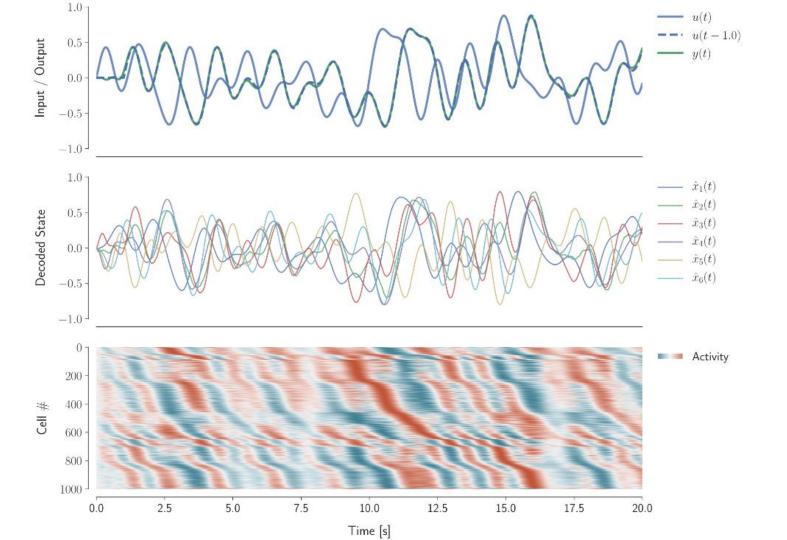


Chaotic Time-Series Prediction

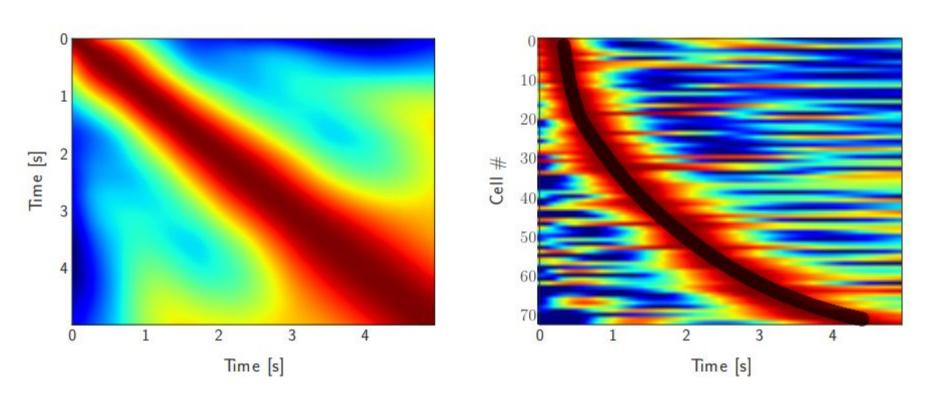


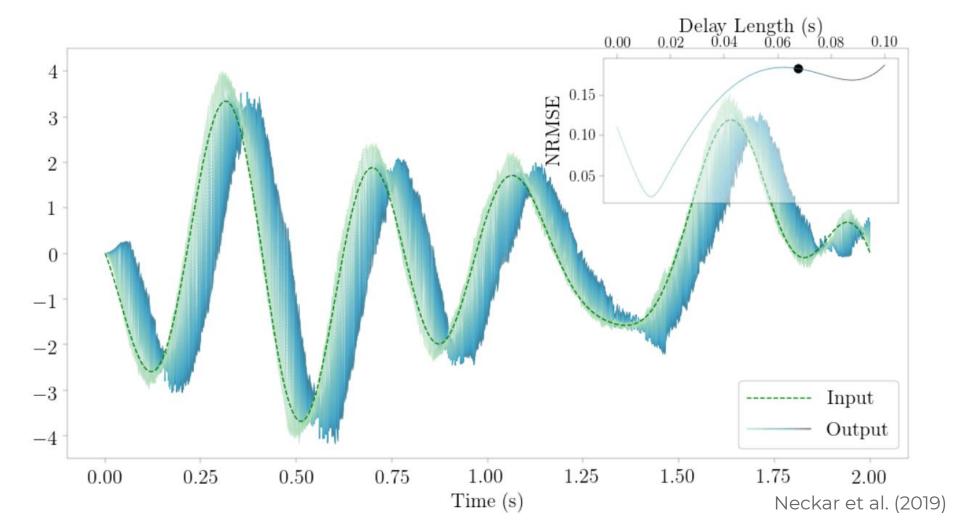
Model	Test NRMSE	Training Time (s/epoch)
LSTM	0.079	20.34 s
LMU	0.054	12.89 s
Hybrid	0.050	16.21 s

Mackey-Glass Dataset



Time Cell Data





Neural Implementation

