# A Simple Unified Framework for **Detecting Out-of-Distribution Samples and Adversarial Attacks**

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only if a test sample is reasonably similar to the training samples

• E.g., training data = animal



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Our goal is to design the classifier to say "I don't know"

 Detecting test samples drawn sufficiently far away from the training distribution statistically or adversarially



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• One can consider a posterior distribution, i.e., P(y|x), from a classifier

$$\hat{y} = \text{BLUE} \qquad \hat{y} = \text{OUT} \qquad \hat{y} = \text{RED} \qquad \hat{y} = \text{RE$$

 However, it is well known that the posterior distribution can be easily overconfident even for such abnormal samples [Balaji '17]

 Detecting test samples drawn sufficiently far away from the training distribution statistically or adversarially



• One can consider a posterior distribution, i.e., P(y|x), from a classifier

$$\hat{y} = OUT$$
  
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• For the issue, we consider to model the data distribution, i.e., P(x|y)

### Mahalanobis Distance-based Confidence Score

- Main idea: Post-processing a generative classifier
  - Given a pre-trained softmax classifier, we post-process a simple generative classifier on hidden feature spaces:

$$\mathbf{X} \Rightarrow \mathbf{O} \Rightarrow \mathbf{O} \Rightarrow \mathbf{O} f(\mathbf{x})$$

$$P(f(\mathbf{x})|y=c)$$

$$P(f(\mathbf{x})|\mu_c, \Sigma)$$

$$\mathbf{Class-wise}$$

$$\mathbf{Gaussian}$$

$$\mathbf{Gaussian}$$

$$\mathbf{distribution}$$

- How to estimate the parameters?
  - Empirical class mean and covariance matrix

$$\widehat{\mu}_{c} = \frac{1}{N_{c}} \sum_{i:y_{i}=c} f(\mathbf{x}_{i}), \quad \widehat{\boldsymbol{\Sigma}} = \frac{1}{N} \sum_{c} \sum_{i:y_{i}=c} \left(f(\mathbf{x}_{i}) - \widehat{\mu}_{c}\right) \left(f(\mathbf{x}_{i}) - \widehat{\mu}_{c}\right)^{\mathsf{T}}$$

• Using training data  $\{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_N, y_N)\}$ 

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penultimate  
$$\mathbf{V} = c)$$
  
$$\mathbf{P}(f(\mathbf{x})|y=c)$$
  
$$\mathbf{P}(f(\mathbf{x})|\mu_c, \Sigma)$$
  
$$\mathbf{Class-wise}$$
  
$$\mathbf{Gaussian}$$
  
distribution

• Why Gaussian? the posterior distribution of the generative classifier (with a tied covariance) is equivalent to the softmax classifier



#### Empirical observation

- ResNet-34 trained on CIFAR-10
- Hidden features follow class-conditional unimodal distributions

[T-SNE of penultimate features]

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$$\mathbf{P}(f(\mathbf{x})|y = c)$$
  
$$\mathbf{O} = \mathcal{N}(f(\mathbf{x})|\mu_c, \Sigma)$$

- Why Gaussian? the posterior distribution of the generative classifier (with a tied covariance) is equivalent to the softmax classifier
- Our main contribution: New confidence score
  - Mahalanobis distance between a test sample and a closest class Gaussian

$$M(\mathbf{x}) = \max_{c} \log P(f(\mathbf{x})|y=c)$$
$$= \max_{c} - (f(\mathbf{x}) - \widehat{\mu}_{c})^{\top} \widehat{\Sigma}(f(\mathbf{x}) - \widehat{\mu}_{c})$$

### Experimental Results

- Application to detecting out-of-distribution samples
  - State-of-the-art baseline: ODIN [Liang' 18]
    - Maximum value of a posterior distribution after post-processing
  - DenseNet-110 [Huang '17] trained on the CIFAR-100 dataset
    - Our method outperforms the ODIN
- Application to detecting the adversarial samples
  - State-of-the-art baseline: LID [Ma' 18]
    - KNN based confidence score: Local Intrinsic Dimensionality
  - ResNet-34 [He' 16] trained on the CIFAR-10 dataset
    - Our method outperforms the LID



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### Conclusion

- Deep generative classifiers have been largely dismissed recently
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  - Detecting out-of-distribution samples
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  - Deep discriminative classifiers (e.g., softmax classifier) typically outperform them for fullysupervised classification settings
- We found that the (post-processed) deep generative classifier can outperform the softmax classifier across multiple tasks:
  - Detecting out-of-distribution samples
  - Detecting adversarial samples
- Other contributions in our paper
  - More calibration techniques: input pre-processing, feature ensemble
  - More applications: class-incremental learning
  - More evaluations: robustness of our method
- Poster session: Room 210 & 230 AB #30

#### Thanks for your attention